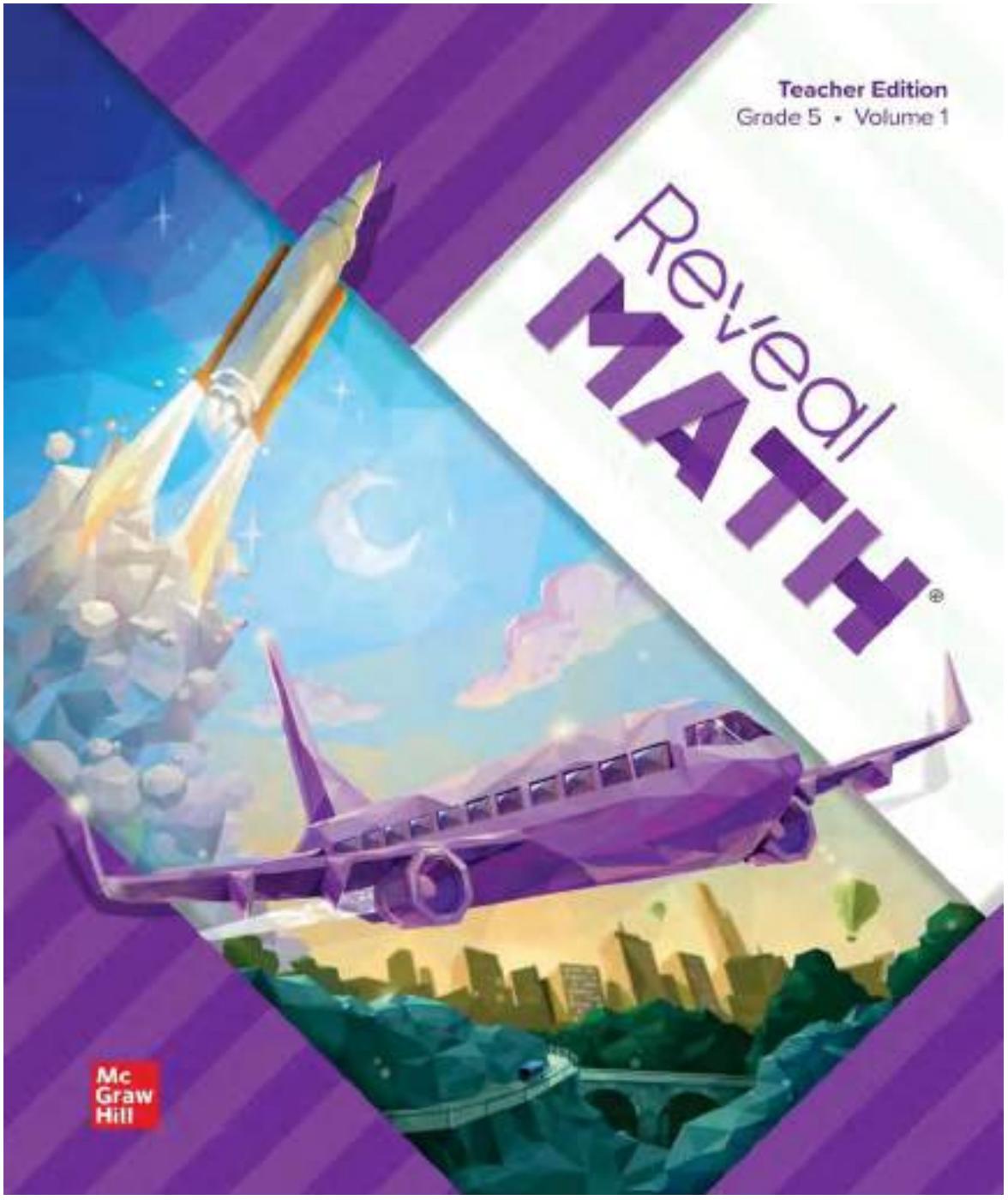


Teacher Edition
Grade 5 • Volume 1

Reveal MATH[®]



Mc
Graw
Hill

Teacher
Edition

Reveal
MATH[®]

Grade 5 • Volume 1





Use the image on the back cover to spark student curiosity about slope. Here are some questions to help guide the conversation as students describe what they notice and wonder about this takeoff.

- What story could you tell about this image?
- What could you use to find out the angle of the plane's take-off?

Back cover: guvendemir/E+/Getty Images

mheducation.com/prek-12



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Welcome to *Reveal Math*

We are excited to share with you the *Reveal Math* program.

In developing *Reveal Math*, we had a clear vision for elementary math instruction. It was important that the program we developed incorporated key findings from recent research on best practices in math instruction. It was also important that the program reflect an emphasis on building students' social and emotional competencies as well ensuring their academic growth.

We also thought extensively about your needs teaching math and your expectations for a high-quality math curriculum. It was important to us that the program provide flexibility in instructional and implementation options to meet the range of instructional settings and the range of learners.

We were purposeful about the organization of concepts and the scope and sequence to make sure students build deep conceptual understanding and develop proficiency with essential concepts and skills.

We are confident that *Reveal Math* incorporates all these goals.

- The lesson model offers two instructional options for each lesson: a guided exploration that is teacher-guided and an activity-based exploration that has students exploring concepts through small group activities and drawing generalizations and understanding from the activities.
- The lesson model incorporates an initial sense-making activity that builds students' proficiency with problem solving. By focusing systematically on sense-making, students develop and refine not just their observation and questioning skills, but the foundation for mathematical modeling.
- Both instructional options focus on fostering mathematical language and rich mathematical discourse by including probing questions and prompts.
- The Math is... unit builds student agency for mathematics. Students consider their strengths in mathematics, the thinking habits of proficient “doers of mathematics,” and the classroom norms that are important to a productive learning environment.
- The scope and sequence reflects the learning progressions recommended by leading mathematicians and mathematics educators. It emphasizes developing deep understanding of the grade-level concepts and fluency with skills, while also providing rich opportunities to apply concepts to solve problems.

Thank you for using *Reveal Math*.
The *Reveal Math* author team

The *Reveal Math* Authorship

McGraw Hill's Learning Scientists teamed up with expert authors to create a program guided by validated academic research and classroom best practices.

Ralph Connelly, Ph.D.

Authority on the development of early mathematical understanding.

Annie Fetter

Advocate for student ideas and student thinking that foster strong problem solvers.

Linda Gojak, M.Ed.

Expert in both theory and practice of strong mathematics instruction.

Sharon Griffin, Ph.D.

Champion for number sense and the achievement of all students.

Susie Katt, M.Ed.

Advocate for the unique needs of our youngest mathematicians.

Ruth Harbin Miles, Ed.S.

Leader in developing teachers' math content and strategy knowledge.

Nicki Newton, Ed.D.

Expert in bringing student-focused strategies and workshops into the classroom.

John SanGiovanni, M.Ed.

Leader in understanding the mathematics needs of students and teachers.

Raj Shah, Ph.D.

Champion of perseverant problem-solvers and student curiosity in mathematics.

Jeff Shih, Ph.D.

Advocate for the importance of student knowledge.

Cheryl Tobey, M.Ed.

Facilitator of strategies that drive informed instructional decisions.

Dinah Zike, M.Ed.

Creator of learning tools that make connections through visual-kinesthetic techniques.



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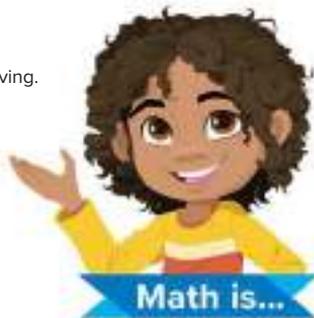
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Math Is...Unit: Establish Classroom Norms for the Year

The first unit in every grade, the Math Is...Unit, aims to help students and teachers see math as problem solving strategies rather than just computation. Students define a productive and positive classroom environment where all students can:

- Share ideas and collaborate freely.
- Find success in math and become doers of mathematics.
- Apply the mathematical thinking and practices to problem solving.
- Take ownership of their personal learning journey.
- Become the creative problem solvers of tomorrow.



Lesson 1 Math Is... Mine

The first lesson aims to help all students see themselves as doers of mathematics, develop a growth mindset, and take ownership of their learning within the math classroom.

Students:

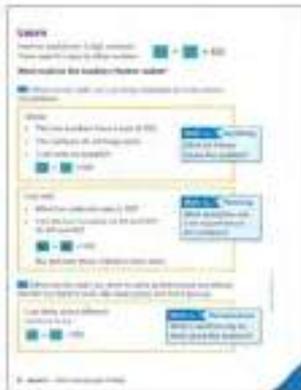
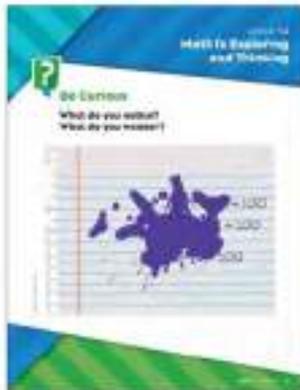
- Learn about the teacher's personal math story.
- Describe their math superpowers.
- Craft their personal math story.



Lessons 2–5 Math Is... A Way of Thinking

The second through fifth lessons focus on thinking habits within the classroom. Each lesson seeks to unpack the thinking habits that are integral to problem solving. Students:

- Become mathematical thinkers.
- Apply the habits of mind of problems solving.
- Communicate effectively about math.



Lesson 6 Math Is... Ours

The sixth lesson recalls the objective of the previous lessons as students learn what a positive and productive classroom environment looks like. Together, the class defines the classroom norms and expectations for the year.

Students:

- Demonstrate a voice and choice in their classroom environment.
- Understand the behaviors and mindsets of the math classroom.



Math Is...Prompts

Math Is...prompts are embedded throughout the Student Edition to help students build proficiency with the thinking habits and classroom norms. These prompts help students to truly own their learning journey throughout the year.

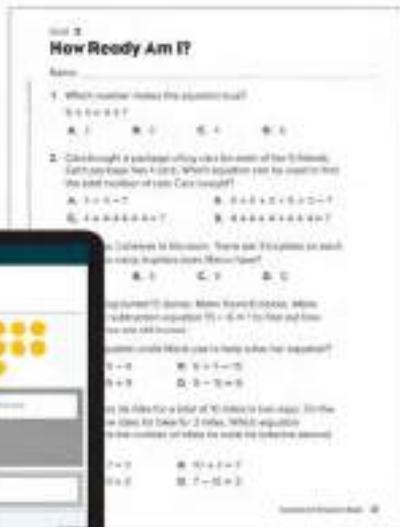
Math Is... Mindset

What can you do to work together with your classmates?



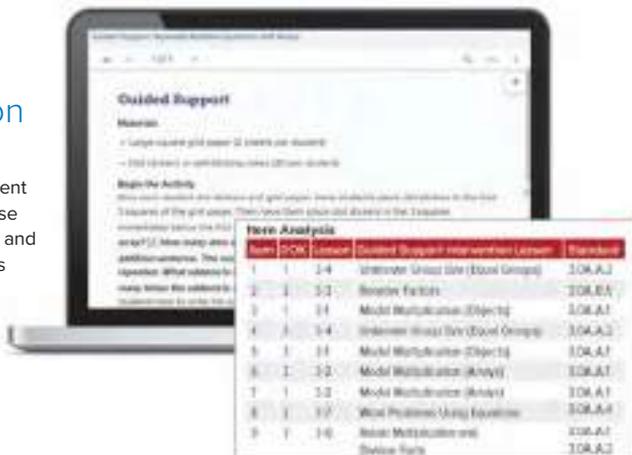
Assessment

The unit begins with a Readiness Diagnostic to assess student's knowledge of essential pre-requisite skills for the unit content. End-of-Unit Assessments are summative assessments for the units and include two forms of the assessment and a Performance Task. A Math Probe is integrated throughout the unit to help identify and address common misconceptions associated with the unit content.



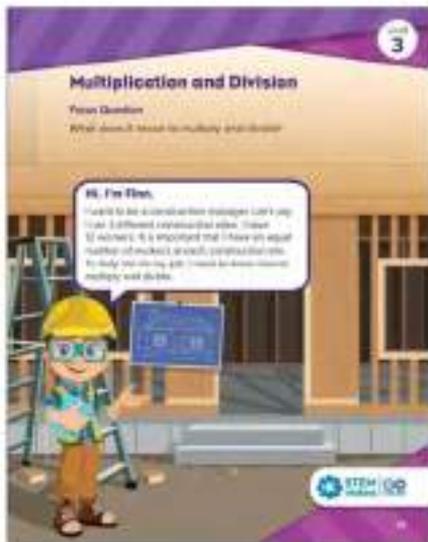
Targeted Intervention

Intervention resources align to the beginning- and end-of-unit assessment items and are available at point of use to quickly correct misunderstanding and target gaps with small group lessons and practice sheets.



STEM-Focused Learning

Each unit highlights a STEM career and shows real-world applications of math to help students see math as a tool to explore the world around them.



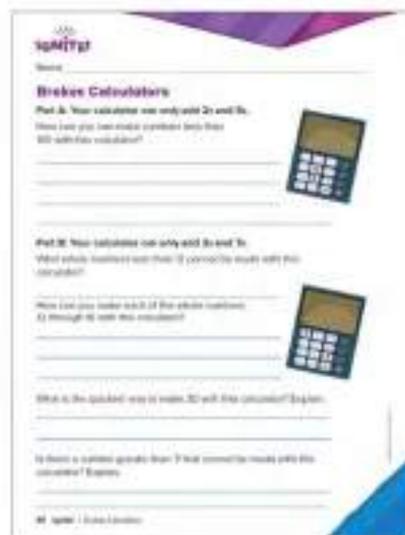
The **STEM Career Kid** video introduces a STEM career and provides an overview of the job responsibilities.



The **Math in Action** videos apply the unit math content with the STEM career focus to bring the content into the real world.

Ignite!

Each unit opens with an Ignite! activity, an interesting problem or puzzle that sparks students' interest and curiosity. With a focus on the problem-solving journey, the activity provides only enough information to open up students' thinking and motivate them to persevere through challenges or setbacks along the problem-solving journey.



The Lesson Model

Reveal Math's lesson model keeps sense-making and exploration at the heart of learning. Every lesson provides two instructional strategies to develop the math content and tailor the lesson to the needs and structure of the classroom.



Launch

Be Curious starts every lesson with the opportunity to be curious about math.

- Students focus on exploration and sense-making.
- Teachers foster students' thinking through meaningful discussion.

Explore & Develop

Explore and Develop unpacks the lesson content through either an activity-based or guided exploration.

- Students explore the lesson concepts and engage in meaningful discourse.
- Teachers implement effective teaching practices to make meaningful connections.

Practice and Reflect

On My Own offers opportunities for students to engage with the math and reflect on their learning.

- Students practice lesson concepts, completing the On My Own exercises.
- Teachers monitor progress and have students reflect on the lesson's learning targets.

Routines

Reveal Math integrates routines within each lesson to help students develop proficiency.

Build Fluency

Number Routines

Support the development of flexibility with numbers and fluency with operations at the start of every lesson.

MLR

Math Language Routines

Promote mathematical language use and development as part of math instruction.



Sense-Making Routines

Build sense-making as a foundation for problem solving and mathematical modeling.



Assess

The **Exit Ticket** includes a daily formative assessment to check for understanding.

- Students complete a short exit ticket and reflect on their learning.
- Teachers use data to inform their daily differentiation.



Differentiate

Daily **Differentiation** helps support every student in their path to understanding.

- Students work on differentiated tasks to reinforce their understanding, build their proficiency, and/or extend their thinking.
- Teachers pull small groups together as needed.



Clear and Comprehensive Objectives

Learning Targets

Every lesson has two learning targets: one based on a skill and one on metacognition.

Objectives

Lessons have three objectives to support the whole child, including:

- Content objective
- Language objective
- Social and emotional learning objective

Rigor

Every lesson identifies the targeted element of rigor.

LESSON 34

Understand Equal Groups

Learning Targets

- I can represent equal groups using equal groups.
- I can explain the meaning of multiplication using equal groups.

Standards

Content
1.OA.A.1 Represent a group of objects (up to 10) as a single addend. For example, describe a group of five birds flying in the sky as five birds flying.

Math Practices and Processes
MP.1 Make sense of problems and persevere in solving them.
MP.2 Reason abstractly.

Vocabulary

Math Terms **Academic Terms**
Equal **Group**
Identical **Number**

Materials

• 10 connecting cubes for each pair
 • 100 chart
 • Counters
 • Chart paper

Focus

Content Objective • Explain equal groups using multiplication.	Language Objectives • Explain the words multiplication and equal groups. • To explain equal groups using multiplication.	Math Objective • Explain the meaning of multiplication using equal groups.
--	---	--

Collaboration

Formative • Ask students to explain their thinking.	Sum • Ask students to explain their thinking.	Sum • Ask students to explain their thinking.
---	---	---

Rigor

Conceptual Understanding • Explain the meaning of multiplication using equal groups.	Procedural Skill and Fluency • Explain the meaning of multiplication using equal groups.	Application • Explain the meaning of multiplication using equal groups.
--	--	---

Number Routine

Would You Rather?

Would you rather have the number of pennies in 4 or 2?

$100 \div 100 = 1000$	$1000 \div 1000$
$100 \div 10 = 1000$	$1000 \div 100$
1000	$100 \div 100$

Daily Focus on Number Sense and Fluency

The Number Routine provides a daily focus on developing fluency and efficiency of strategy. The Number Routine can be completed at any point in the day to build number sense.

Number Routine

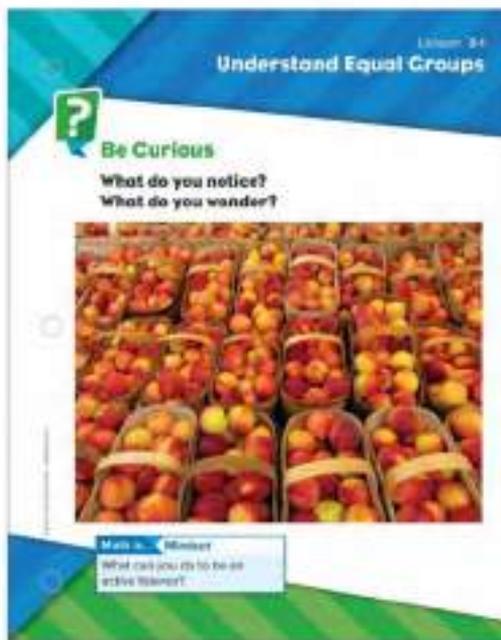
Would You Rather?

Would you rather have the number of pennies in 4 or 2?

$100 \div 100 = 1000$	$1000 \div 1000$
$100 \div 10 = 1000$	$1000 \div 100$
1000	$100 \div 100$

Derive Understanding by Sparking Curiosity

Sense-making routines launch every lesson, creating an equitable classroom culture where all ideas are welcome and respected. Student curiosity and ideas shared in *Be Curious* become the base for the day's lesson.



“All students have ideas about math that are valid and worth talking about.”

Annie Fetter
Contributing Author

Be Curious offers a high-ceiling/low-floor that allows every student to explore and discuss their ideas with multiple entry points and approaches to problem-solving.

Support the Whole Child With Social and Emotional Learning Integration

Every lesson integrates a social and emotional learning objective. These objectives are based on the CASEL Social and Emotional Learning competencies.

Math is... Mindset prompts with teacher supports keep social and emotional learning at the top of students' minds as they interact with classmates at key points during the lesson.



CHOOSE YOUR OPTION

Activity-Based Exploration

Students explore and use equal groups to find the total number of objects.

Materials: counters or other countable manipulatives, jars or string

Directions: Students will explore ways to find the total number of peaches in 5 baskets.

- Let's imagine there are five baskets and the baskets have peaches in them. How can you determine the total number of peaches in the baskets?

Students will use jars or string to represent the baskets and counters to represent the peaches. Students may choose to place the same number of counters in each group or a different number. Have them find the total number of peaches and record their work.

- Support Productive Struggle**
- How many counters are in each group?

Guided Exploration

Students build a understanding of one meaning of multiplication as equal groups.

Use and Connect Mathematical Representations

- **Think About It:** What does each object represent?
• What could be another way to show the number of baskets and the number of peaches in each basket?

Discuss with students the meaning of equal groups. Emphasize that students understand that equal groups have the same number of objects in each group.

- How could you explore to a friend that five peaches are in equal groups?

Identify the multiplication symbol in the equation and explain that it means groups of and can be read as multiplied by. Explain that you

CHOOSE YOUR OPTION

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Directions: Students will explore ways to find the total number of peaches in 5 baskets.

- Let's imagine there are five baskets and the baskets have peaches in them. How can you determine the total number of peaches in the baskets?

Students will use jars or string to represent the baskets and counters to represent the peaches. Students may choose to place the same number of counters in each group or a different number. Have them find the total number of peaches and record their work.

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Activity-Based Exploration allows students to explore concepts, develop and test hypotheses, and—most importantly—engage in productive struggle as they problem solve and generalize learning.

Guided Exploration follows a teacher-facilitated exploration and collaboration to promote rich discourse about the concept.



Exit Ticket: Use Data to Inform Differentiation

Every lesson closes with an Exit Ticket. Differentiation recommendations reside in the Teacher Edition to make the Exit Ticket data actionable.

Exit Tickets can be completed in print or in the Digital Student Center.

LEARN 3.14
Exit Ticket

Name _____

1. How many? Fill in the blanks.



_____ equal groups of _____

2. Connor makes 6 equal-sized loaves. Each loaf has 16 slices of cheese. How many slices of cheese does Connor get to make the 6 loaves?
Write a multiplication equation.

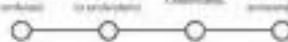
3. Study and give each student 4-60 equal groups. Which set of groups is shown here every loaves? Write a Division of 60.



A. 3 equal groups of 20 B. 4 equal groups of 15
C. 6 equal groups of 10 D. 12 equal groups of 5

Reflect On Your Learning

How confident I am with this skill



100% Confident 50% Confident Learning I need to practice



Question 3 of 9

Question 3

Choose the multiplication equation that goes with the model.



$4 \cdot 4 = 16$

$4 \cdot 3 = 12$

$4 \cdot 2 = 8$

$2 \cdot 3 = 6$

Save and Continue Submit Assignment

Reflect On Your Learning allows students to reflect on their learning daily and communicate their confidence level with the teacher.



Create Purposeful Learning Moments Driven by Data

Differentiation within *Reveal Math* provides a variety of engaging, multi-modal activities in different delivery options that any student can access based on the area they need to focus on most for each lesson.

Workstations

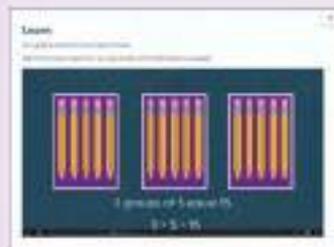
Reinforce Understanding



Small Group Instruction

Teacher-facilitated small group mini-lesson that uses concrete modeling and discussion to reteach and build conceptual understanding.

Online Activities



Build Proficiency



Digital Station

Digital Games encourage proficiency through a fun and engaging practice environment.

Game Station

A hands-on way to engage with the lesson content and collaborate with classmates.



Extend Thinking



Application Station

Opportunity to apply unit content to real-world problems and projects through one of three categories of application cards: STEM Projects, Cross-Curricular Connections, or Real World Problem-Solving Cards.

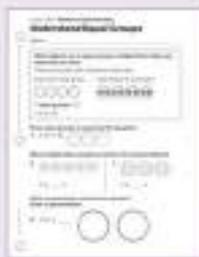


Independent Practice

Take Another Look

Assignable mini-lessons that provide actionable data to help inform instruction while supporting each student with a three-part, gradual-release activity, including:

- Model of the Concept
- Interactive Practice
- Quick Check



Reinforce Understanding Practice Sheet

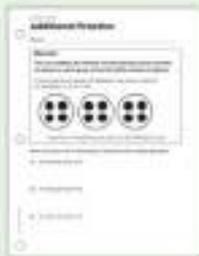
Practice sheet focused on practicing and understanding the concepts within the lesson.

Spiral Review

Digital practice with mixed standards coverage for major clusters within each grade level to prepare students for end-of-year testing.

Interactive Additional Practice

Digital practice, complete with learning aids integrated into problems at point-of-use.



Student Practice Book

Two additional practice pages for practice and/or homework.

WebSketch Exploration

Highly visual and engaging interactive digital activities where students explore with a concept through an open-ended environment.

STEM Adventure

STEM Adventures are rich digital simulations that allow students to apply skills and concepts to solve real-world problems. Simulations deliver multiple outcomes as a result of the student's choices throughout the experience.



Extend Thinking Practice Sheet

Practice sheet focused on application.

Print Resources

Two-Volume Student Edition

Available in print and interactive formats, the Student Editions are consumable and perforated for ease of use. Helpful Math Is...prompts remind students of how to actively apply the mathematical practices.

Student Practice Book

The Student Practice Book provides two pages of additional practice for each lesson.

- Interactive Student Edition
- Math Replay Videos
- eToolkit
- eGlossary
- STEM Career Kid Video Library
- Math In Action Video Library

- Interactive Digital Practice
- Interactive Spiral Review
- Digital Games Library

Student Spanish Materials

Student Edition

Student Practice Book

- Student eBook
- Math Replay Videos
- eGlossary
- Family Letter

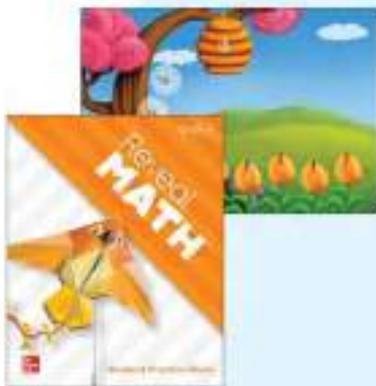
Teacher Spanish Materials

Assessment Resource Book

Application Station Cards

Game Station Resource Book

- Differentiation Resource Book
- Assessment Resource Book
- Application Station Card
- Game Station Resource Book
- Autoscored Online Assessments



Print Resources

Implementation Guide

The Implementation Guide supports implementation with a user guide, professional development resources, and overarching program information, such as lesson components, correlations, and more.

Two-Volume Teacher Edition

Available in print and ebook formats, the Teacher Editions provide comprehensive supports, such as Effective Teaching Practices, embedded within the instruction.

Assessment Resource Book

The Assessment Resource Book contains the masters for the following assessments:

- Course Diagnostic
- Unit Readiness Diagnostics
- Exit Tickets
- Unit Assessments
- Benchmark Assessments
- Math Probes
- Performance Tasks
- Summative Assessment

Differentiation Resource Book

The Differentiation Resource Book provides access to the Reinforce Understanding and Extend Thinking worksheets.

Workstation Kit

The Workstation Kit supports daily differentiation and includes:

- Game Station Resource Book
- Workstation Teacher Guide
- Application Station Cards
- Manipulatives

Manipulative Kits

Manipulative Kits are available and contain the manipulatives used within the lessons.

Digital Center

- Expert Insight Videos
- Program Quick Start
- Classroom Videos
- Workshop Modules
- Point of Use Videos

- Teacher Edition eBook
- Lesson Presentations
- Planning and Classroom Management Tools
- Unit and Lesson Downloadable Files

- Assessment PDFs
- Autoscored Online Assessments
 - Course Diagnostic
 - Unit Readiness Diagnostics
 - Exit Tickets
 - Unit Assessments
 - Performance Tasks
 - Benchmark Assessments
 - Summative Assessment
- Targeted Intervention
 - Guided Support
 - Skills Support Sheets

- Digital Games
- STEM Adventures
- WebSketch Explorations
- Take Another Look Lessons
- Interactive Digital Practice
- Student Practice Book PDFs
- Spiral Review PDFs
- Reteach and Extend PDFs
- Application Station Card PDFs
- Games Station PDFs

eToolkit to include: Counters; Base-Ten Blocks; Array Builder; Fraction Model; Bucket Balance; Geometry Sketch; Money; Fact Triangles; Number Line; and more!



Review the Implementation Guide

The Implementation Guide provides a wide range of information to help familiarize teachers with *Reveal Math*, including:

Program Design

- Product Structure and Components
- Standards
- Focus, Coherence, and Rigor
- Mathematical Practices and Processes

Major Themes

- Fluency
- Practice
- Social and Emotional Learning
- Student Agency
- Language Supports
- Routines

Implementation Support

- Unit and Lesson Walkthrough
- Digital Implementation Support

Content Overview

- Key Objectives
- Standards Correlations
- Scope and Sequence
- Social and Emotional Learning Correlations
- STEM Careers Overview



Find Professional Learning Resources Online

Professional Learning resources are provided for the teacher to reference 24/7. Resources include:

- Workshop modules to unpack key instructional moments in the classroom.
- Classroom videos that demonstrate a productive and positive classroom environment.
- Expert videos that support effective teaching practices and the content within each unit.



Prepare for a Unit

Every unit provides relevant and efficient information to help inform effective unit instruction and content. Within the Teacher Edition, the Unit Overview includes the following overview support for the unit:

- Focus, Coherence, and Rigor
- Routines
- Effective Teaching Practices
- Math Practice and Process
- Social and Emotional Learning
- Language Support

The screenshot shows a 'Unit Overview' page with several sections:

- Focus:** A section with text and a small diagram.
- Coherence:** A section with three columns of text.
- Rigor:** A section with three columns of text.
- Effective Teaching Practices:** A section with text and a small diagram.
- Math Practice and Process:** A section with text and a small diagram.
- Social and Emotional Learning:** A section with text and a small diagram.

Embedded Expert Insight Videos

Experts provide practical information about the math within each unit, tips of effecting teaching, and what to look and listen for during instruction.

The screenshot shows a video player interface with a play button and a video thumbnail. The video title is 'Behind the Math: Multiplication and Division'. The description reads: 'This professional learning video, featuring program author Linda Sparks, identifies the essential elements of teaching multiplication and division and focuses on the use of equal groups and arrays to represent and understand the relationship between the two operations.'

Course Diagnostic

The Course Diagnostic is available in both print and digital.

Data When students complete the Course Diagnostic in the Digital Student Center, their responses are auto-scored.

If students need support based on the Course Diagnostic, use the Unit Level Readiness Diagnostic Intervention Lessons.



Item Analysis

Item	DOK	Skill	Unit	Standard
1	1	Relate multiplication and division	7	4.NBT.B.6
2	2	Add fractions with like denominators	9	4.NF.B.3
3	2	Write whole numbers in standard form	3	4.NBT.A.2
4	2	Subtract fractions to solve word problems	9	4.NF.B.3.d
5	2	Use place value and properties of operations to multiply multi-digit numbers	5	4.NBT.B.5
6	2	Convert standard units of length	12	4.MD.A.1
7	2	Use division to solve multi-step word problems	7	4.OA.A.3
8	2	Add fractions with like denominators	9	4.NF.B.3
9	2	Solve area word problems	2	4.MD.A.3
10	2	Estimate quotients	7	4.NBT.B.6
11	1	Multiply a unit fraction by a whole number	10	4.NF.B.4
12	2	Compare fractions	9	4.NF.A.2
13	2	Round numbers	3	4.NBT.A.3
14	2	Compare decimals	3	4.NF.C.7
15	2	Identify shapes by attributes	13	4.G.A.2
16	2	Convert units of time	12	4.MD.A.2
17	1	Add mixed numbers	9	4.NF.B.3.c
18	2	Multiply by fractions to solve word problems	10	4.NF.B.4.c
19	2	Compare decimals	3	4.NF.C.7
20	2	Calculate area	2	4.MD.A.3
21	2	Multiply by fractions to solve word problems	10	4.NF.B.4.c
22	2	Add mixed numbers	9	4.NF.B.3.c
23	3	Use data on a line plot to solve word problems	12	4.MD.B.4, 4.NF.B.3.c
24	2	Multiply 2-digit numbers to solve word problems	5	4.NBT.B.5
25	2	Subtract fractions	9	4.NF.B.3.a
26	2	Represent comparison word problems with multiplication equations	5	4.OA.A.2
27	2	Interpret the remainder in division word problems	7	4.OA.A.3
28	1	Write a fraction as a decimal	3	4.NF.C.6
29	3	Use data on a line plot to solve word problems	12	4.MD.B.4, 4.NF.B.4
30	2	Identify equivalent fractions	9	4.NF.A.1
31	1	Understand multiplication as scaling	10	4.NBT.A.1
32	2	Use division to solve word problems	7	4.NBT.B.6
33	2	Multiply 2-digit numbers	5	4.NBT.B.5
34	1	Add tenths and hundredths	4	4.NF.C.5
35	3	Use models to write division expressions	7	4.NBT.B.6

Grade 4
Course Diagnostic

Name: _____

1. Which equation has the same unknown in both as $322 + 9 = \square$?

A. $\square + 9 = 331$
 B. $9 + 322 = \square$
 C. $\square + 322 = 9$
 D. $322 + \square = 9$

2. Look at the number line.

Which equation has the same sum?

A. $4 + 4 = 8$
 B. $4 + 2 = 6$
 C. $4 + 1 = 5$
 D. $4 + 3 = 7$

3. Use the clues to determine the number.

I have 20 hundreds, 25 tens, and 7 ones. What number am I?

3,547

4. The area of a rectangular garden is 24 square feet. The length is 6 feet. What is the width of the garden?

A. 3 feet
 B. 10 feet
 C. 22 feet
 D. 24 feet

5. The area of a rectangular garden is 24 square feet. The length is 6 feet. What is the width of the garden?

A. 3 feet
 B. 10 feet
 C. 22 feet
 D. 24 feet

6. Which equation is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 580 + 8$
 C. $33 + 7 + 58 + 4(8) + 7 + 8$
 D. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$

7. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

8. The area of a rectangular garden is 24 square feet. The length is 6 feet. What is the width of the garden?

A. 3 feet
 B. 10 feet
 C. 22 feet
 D. 24 feet

9. The area of a rectangular garden is 24 square feet. The length is 6 feet. What is the width of the garden?

A. 3 feet
 B. 10 feet
 C. 22 feet
 D. 24 feet

10. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

11. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

12. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

13. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

14. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

15. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

16. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

17. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

18. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

19. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

20. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

21. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

22. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

23. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

24. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

25. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

26. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

27. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

28. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

29. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

30. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

31. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

32. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

33. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

34. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

35. Which expression is equal to $33 + 587$?

A. $33 + 7 + 580 + 8$
 B. $33 + 7 + 58 + 4(8) + 7 + 8$
 C. $33 + 33 + 33 + 5 + 4(8) + 3 + 8 + 8 + 8 + 8 + 8$
 D. $33 + 7 + 580 + 8$

Course Diagnostic (continued)

Name _____

16. It took Oscar $\frac{1}{2}$ hour to clean his room.
How many minutes does it take Diego to clean his room?
45 minutes
17. What constant number makes the equation $\frac{1}{2} + \frac{1}{3} = \square - \frac{1}{6}$ true?
A. 2 B. $\frac{1}{2}$ C. $\frac{1}{3}$ D. $\frac{1}{6}$
18. Why has $\frac{1}{2}$ inch of rain not been enough to water each day?
How many days of rain will it take to water each day?
Use the number line to determine your answer.
-
19. How can you compare the amount? Complete with $>$, $=$, or $<$.
125.45 $>$ 125.25

20. Look at the rectangle.



- What is the area of this rectangle?
12 square centimeters
21. Each hour, a river flows $\frac{1}{2}$ percent of water to each mouth.
If each mouth is 50 miles, how many mouths of water does the river do to it?
A. $\frac{1}{2}$ percent B. $\frac{1}{4}$ percent
C. $\frac{1}{2}$ percent D. $\frac{1}{4}$ percent

Answer Key for Test 5

Course Diagnostic (continued)

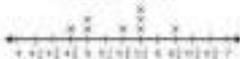
Name _____

22. Write $\frac{37}{100}$ as a decimal number.
0.37
23. It will take eight weeks to complete.
The job shows the weight in pounds of each package.
Weight of Packages (lb)
-
- What is the total weight of the packages that weigh $\frac{1}{4}$ pound?
A. $\frac{1}{4}$ pounds B. $\frac{1}{2}$ pounds
C. $\frac{1}{2}$ pounds D. $\frac{1}{4}$ pounds
24. Which fraction can represent $\frac{1}{2}$? Check all that apply.
A. $\frac{2}{4}$ B. $\frac{1}{2}$
C. $\frac{3}{6}$ D. $\frac{1}{3}$
25. Which number makes the equation true?
125.05 is _____ times greater than 12.500.
A. 10 B. 100 C. 1,000 D. 10,000
26. Publishers say 90 columns to put an 18-column page.
If each page has 18 columns, how many pages does Publishers need?
50 pages

Answer Key for Test 5

27. What unknown number makes the equation $\frac{1}{2} + \square = \frac{3}{4}$ true?
A. $\frac{1}{4}$ B. $\frac{1}{2}$ C. $\frac{1}{4}$ D. $\frac{1}{2}$
28. Total volume for height of three bushes of two garden. The plot shows the height, in feet, of each bush.

Height of Bushes (ft)



How much taller, in feet, is the tallest bush than the shortest bush?

- A. 1 foot B. $\frac{1}{2}$ foot
C. $\frac{1}{4}$ foot D. 3 feet
29. Match play a game to practice typing on the computer for 4 days. He jumps the typing game for 30 minutes each day.
How many minutes does Mateo play in all?
120 minutes
30. What unknown number makes the equation $\frac{1}{2} - \frac{1}{3} = \square$ true?
A. $\frac{1}{6}$ B. $\frac{1}{3}$ C. $\frac{1}{6}$ D. $\frac{1}{3}$
31. Look with 2 calculations. One is a table of times on many basketballs as come.
Which equation represents the number of basketballs that was used?
A. $2 \times 4 = 8$ B. $4 \times 2 = 8$
C. $2 + 4 = 6$ D. $4 + 2 = 6$

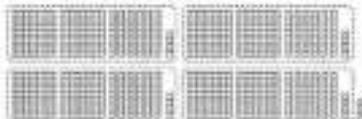
32. There are 48 points to determine some picture frames.
If the user 24 points to 16 pictures each picture frame, how many picture frames can David complete?

3 picture frames

Answer Key for Test 5

33. What is the product of 487 \times 32?
15,680
34. Which expression can be used to find the sum of $\frac{1}{2} + \frac{1}{3}$?
A. $\frac{1}{2} + \frac{1}{3}$
B. $\frac{2}{3} + \frac{1}{3}$
C. $\frac{3}{6} + \frac{2}{6}$
D. $\frac{1}{2} + \frac{1}{3}$

35. Look at the base ten blocks.



Which addition problem is represented by the base ten blocks?

- A. $20 + 4$
B. $20 + 4$
C. $100 + 4$
D. $100 + 4$

Answer Key for Test 5

PACING: 8 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  Map It	Explore how many different colors are needed to color a region so that no adjacent spaces are the same color.		
1-1 Math Is Mine	Students discuss the role of math in their and other people's lives.	Students talk about how to use math while answering <i>Wh-</i> questions.	Students describe their feelings and attitudes toward mathematics.
1-2 Math Is Exploring and Thinking	Students discuss approaches for making sense of a problem and determining strategies for solving it. Students look for connections among quantities.	Students talk about making sense of a problem and represent it in different ways while answering <i>Wh-</i> questions and using <i>another way</i> .	Students recognize when they feel frustration during math class.
1-3 Math Is in My World	Students consider different ways to use mathematics to represent a real-world situation.	Students explain and show real-world phenomena with mathematical models while answering <i>Wh-</i> questions and using <i>visualize</i> and <i>represent</i> as needed.	Students show appreciation for the different perspectives of their classmates.
1-4 Math Is Explaining and Sharing	Students refine their skills in constructing arguments to support their thinking. Students respond to the ideas and arguments of others.	Students discuss arguments to support their thinking while answering <i>Wh-</i> questions and using <i>carefully</i> as needed and able.	Students practice showing respect for classmates as they share ideas and thinking.
1-5 Math Is Finding Patterns	Students consider strategies for uncovering patterns and for using patterns to solve problems. Students consider efficient strategies derived from repeated reasoning.	Students talk about strategies for uncovering patterns and for using patterns to solve problems while answering <i>Wh-</i> and Yes/No questions and using the verb <i>can</i> as needed.	Students practice self-control as they learn to take turns when sharing ideas with a partner or in a group.
1-6 Math Is Ours	Students discuss classroom norms of interaction for a productive learning environment.	Students talk about the behaviors and mindsets that contribute to a productive learning environment while answering <i>Wh-</i> and Yes/No questions and using the verb <i>disagree</i> and the adverb <i>respectfully</i> as needed.	Students make decisions about classroom norms for working productively with classmates.
Unit Review			
Fluency Practice			

FOCUS QUESTION:
What does it mean to do math?

LESSON	KEY VOCABULARY		MATERIALS TO GATHER	RIGOR FOCUS	STANDARD
1-1	<u>Math Terms</u> hobby	<u>Academic Terms</u> interview	<ul style="list-style-type: none"> • bowl • letter-size paper cut into quarters 	Conceptual Understanding	4.OA.C.5
1-2	strategy	analyze	<ul style="list-style-type: none"> • coins: nickels, dimes, and quarters 	Conceptual Understanding	4.NF.B.4 4.NF.B.4.c
1-3	grid model	visualize	<ul style="list-style-type: none"> • none 	Conceptual Understanding	4.NF.B.3.d
1-4	fractional	critique justify defend	<ul style="list-style-type: none"> • none 	Conceptual Understanding	4.NF.A.2
1-5		efficient generalizations	<ul style="list-style-type: none"> • none 	Conceptual Understanding	4.OA.C.5
1-6		norms responsibility	<ul style="list-style-type: none"> • geoboards or <i>Dot Paper Teaching Resource</i> • pattern blocks or <i>Pattern Blocks 2 Teaching Resource</i> 	Conceptual Understanding	4.NF.B.3.d

Unit Overview

Focus

Understanding What Math Is

The focus of this unit is threefold:

- to build students' agency as doers of mathematics. It is important that students understand that math is not just something done in school. Math is part of our daily lives and shows up in almost every activity. It is also important that students see themselves as skilled doers of math, so helping them understand that doing math is not carrying out operations or calculations. Rather, doing math is more accurately making sense of and solving problems and finding patterns and relationships among quantities and numbers. Lesson 1-1 helps students see themselves as doers of math as they examine their attitudes towards math and their images of themselves as doers of math.
- to build students' proficiency with the habits of mind that are integral to doing mathematics. These include the thinking that makes up the problem-solving process and that is involved in finding patterns and relationships among quantities and values. Lessons 1-2 through 1-5 focus on helping students build proficiency with these habits of mind.
- to build understanding of the norms of interaction that allow for a productive math learning environment where students can develop, refine, and enhance the habits of mind that are integral to doing math. Lesson 1-6 offers the opportunity for students to develop together the classroom norms for math for the school year.

Coherence

What Students Have Learned

- Students refined their problem-solving skills as they analyzed givens and developed solution strategies.
- Students modeled real-world situations with a range of representations.
- Students responded appropriately to their classmates' reasoning.
- Students used clear and precise language in their explanations and arguments.
- Students made generalizations after noticing patterns in operations.

What Students Are Learning

- Students build on their problem-solving skills as they consider alternative strategies for solving the problem presented.
- Students model real-world situations with a range of representations.
- Students construct arguments to critique the reasoning of classmates.
- Students use appropriate units in their calculations.
- Students make generalizations after noticing repeated calculations with operations.

What Students Will Learn

- Students extend their problem-solving skills as they consider reasonableness of their solutions.
- Students model real-world situations with equations.
- Students construct arguments to defend their thinking.
- Students use appropriate units in their calculations.
- Students develop efficient approaches for solving equations based on repeated calculations.

Rigor

Conceptual Understanding

- Students refine their understanding of
- the habits of mind that are part of the problem-solving process;
 - classroom norms that are integral to a productive math learning environment;
 - themselves as doers of math.

Procedural Skill and Fluency

- Student build proficiency with
- the habits of mind that are part of the problem-solving process;
 - constructing arguments to support their mathematical thinking;
 - using precise language when constructing arguments.

Application

- Students apply their knowledge of
- the habits of mind that are part of the problem-solving process as they solve problems;
 - themselves as doers of math to solve problems efficiently;
 - the language of mathematics when engaging in mathematical discourse.

Effective Teaching Practices

Ambitious Teaching

In 2014, the National Council for Teachers of Mathematics released *Principles to Actions: Ensuring Mathematical Success for All*, a publication designed to support teachers in implementing “ambitious teaching,” an approach to teaching that views students as able to engage productively in the problem-solving process, and encourages and values students’ thinking and ideas. To implement “ambitious teaching,” the authors of *Principles to Actions* offer eight teaching practices. These research-based practices are grounded in the goals of helping students develop sense-making, thinking, and reasoning skills.

Each unit will highlight one of the eight teaching practices, providing an overview of what the practice means and how it helps to contribute to students’ success in learning mathematics.

The eight practices are:

- Establish mathematics goals to focus learning.
- Implement tasks that promote reasoning and problem solving.
- Use and connect mathematical representations.
- Facilitate meaningful mathematical discourse.
- Pose purposeful questions.
- Build procedural fluency from conceptual understanding.
- Support productive struggle in learning mathematics.
- Elicit and use evidence of student thinking.

Math Practices and Processes

Promoting students’ sense-making, thinking, and reasoning.

- In this unit, Lessons 1-2 through 1-5 focus students’ learning on the mathematical habits of mind that are integral to proficiency in mathematics. Each lesson focuses on two specific habits of mind:
- Lesson 1-2 – *Math Is Exploring and Thinking*: Students are presented with the thinking habits that can help them make sense of a problem posed, analyze givens and unknowns, think through a solution strategy, and consider approaches to persevering when they run into road blocks in the problem-solving process. Students also consider the meaning of quantities and the relationship among the quantities and values in a problem.
- Lesson 1-3 – *Math Is In My World*: Students explore real-world phenomena and look to model these phenomena using the mathematics they know. Students consider the different tools they know that they can use to model the mathematics and make decisions around the appropriate tool for the problem.
- Lesson 1-4 – *Math Is Explaining and Sharing*: Students focus on strengthening their mathematical discourse and argumentation as they explain their reasoning about a strategy or solution. They also build discourse by responding to the reasoning of their classmates. They not only seek clarification around classmates’ reasoning, but also challenge the reasoning with their own explanations and thinking.
- Lesson 1-5 – *Math is Finding Patterns*: Students notice patterns and repeated reasoning with numbers and operations. They analyze the patterns they notice to come up with generalizations and strategies to make computation more efficient.

Social and Emotional Learning

Build Student Agency

This unit introduces students to the Math is... Mindset feature of the program. This feature is designed to build student agency by focusing on students’ social and emotional learning, specifically the five competencies that make up the framework established by the Collaborative for Academic, Social, and Emotional Learning (CASEL). The five competencies are:

Self-awareness: Students learn to recognize their emotions and understand their influence on their behaviors.

Self-management: Students learn to regulate their emotions, and behaviors effectively in different situations.

Social awareness: Students develop understanding of and empathy for others from different backgrounds and cultures.

Relationship skills: Students learn to establish and maintain healthy relationships with students from different backgrounds and cultures.

Responsible decision-making: Students learn to make constructive choices about their behavior and their interactions with others.

Lesson 1 focuses on self-awareness, self-management, and responsible decision-making as students think about their attitudes toward and strengths in mathematics. As part of the lesson, students write their math biography.

Lesson 6 focuses on social awareness, relationship skills, and responsible decision-making as students discuss classroom norms for a productive learning environment. They generate a list of classroom norms and expectations for math class.

Starting in Unit 2, students will see Math Is... Mindset questions at the beginning and end of each lesson. These questions will help students build proficiency with the five competencies.

Unit Overview

Language of Math

Vocabulary

There are some math and academic terms that students should be familiar with but may warrant revisiting.

- **Critique** (Lessons 1-4): Make sure students understand that the focus of the critique is students' reasoning, not the students themselves.
- **Efficient** (Lesson 1-5): Students have seen this term in previous grades, but it is an important term for them to understand. An efficient strategy is one that can be done the same way quickly.

- **Fractional** (Lesson 1-2): Some students may not make the connection between "fraction" and "fractional." Help them see that the two terms are related.
- **Hobby** (Lesson 1-1): This may be a new term for some students. Explain that a hobby is an activity that one does in their free time.
- **Grid** (Lesson 1-3): This may be a new term for some students although they will be introduced to the coordinate plane and coordinate grids later in the school year.

Math Language Development

A Focus on Speaking and Listening

A main emphasis of this unit is helping students become proficient doers of mathematics and that requires that students become proficient at communicating clearly and precisely. Communicating clearly and precisely involves not just strong speaking skills, but strong listening skills as well.

When students engage in active listening, they attend fully to the speaker. They concentrate on what the speaker is saying, processing the ideas being shared. Active listeners can re-state with understanding what the speaker has shared and can then respond clearly to the ideas shared.

When students engage in active speaking, they attend fully to their audience. They concentrate on what they are saying and use the reactions from the audience to determine how well the audience is understanding the ideas that speakers are sharing.

As students go through these lessons, have some students read aloud the Math Is... questions and others actively listen to the questions being asked. Have student listeners re-state the questions read and explain what the question means for them.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to what math is to them. Because many of the words (positive, stuck, argument), phrases (don't give up, keep trying, carry out, work together/on your own), and structures (If..., [then]...) used in this section are likely unfamiliar or unknown to ELs, students are supported in understanding and using these words so that the instruction is more accessible to them.

- Lesson 1-1 – *positive*
- Lesson 1-2 – *stuck, don't give up, keep trying*
- Lesson 1-3 – *carry out*
- Lesson 1-4 – *argument*
- Lesson 1-5 – *If, ..., (then)...*
- Lesson 1-6 – *work together, on your own*

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense. They also help students develop the thinking habits of mind that are important for proficient doers of math.

Math Pictures

Purpose: Build estimating and visual discrimination skills.

Overview: Students examine an interesting photograph and answer a question about it.

Lesson 1-1: Students are presented with an image of people riding in gondolas. They respond to the prompt, “What numbers can describe the picture?”

Lesson 1-2: Students are shown some plastic ducks, most of which are yellow and one is purple and respond to the prompt, “What fractions can you use to describe the picture?”

Lesson 1-3: Students see an assortment of dominos and respond to the prompt, “About how many dots are on all the dominos?”

Lesson 1-4: The image shows two pea pods, one open to show the peas inside and the second closed. Students respond to the prompt, “About how many seeds are in 125 pods?”

Lesson 1-5: The image shows a stack of rolls of pennies. Students to the prompt, “If there are 50 pennies in a roll, are there more or fewer than 400 pennies in the picture?”

Lesson 1-6: The image shows decorated spheres hanging on a board. Students respond to the prompt, “About what fraction of decorations is missing?”

Sense-Making Routines

Notice & Wonder (Lessons 1-1, 1-2, 1-3, 1-5, 1-6)

In Lesson 1-1, students notice and wonder about a student pensively reflecting. For Lesson 1-2, students notice and wonder about two stacks of coins (one of quarters and one of dimes), each about the same height. Students may wonder which stack has the greater value. In Lesson 1-3, students notice the number of squares of each color in two 4×4 grids. They may wonder about the part of the whole that each color represents. The prompt for Lesson 1-5 shows a sunflower. Students may notice the pattern and wonder whether there is a rule that can define the pattern. In Lesson 1-6, students wonder what students are working on and how they work together.

Which Doesn't Belong? (Lesson 1-4)

Students analyze four wholes partitioned into different-sized equal parts with different numbers of sections colored. They may notice while some have two parts colored, the fraction of the whole that is colored differs.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. These routines can also be used as formative assessment opportunities as students develop proficiency in English and mathematical language. They can be used in ways that support real-time-, peer-, and self-assessment. For more information on the Math Language Routines, see the Appendix.

- Lesson 1-1 – In order to cultivate conversation, students participate in MLR8: Discussion Supports.
- Lesson 1-2 – In order to optimize output, students participate in MLR7: Compare and Connect.
- Lesson 1-3 – In order to optimize output, students participate in MLR4: Info Gap.
- Lesson 1-4 – In order to optimize output, students participate in MLR1: Stronger and Clearer Each Time.
- Lesson 1-5 – In order to support sense-making, students participate in MLR2: Collect and Display.
- Lesson 1-6 – In order to maximize linguistic and cognitive meta-awareness, students participate in MLR5: Co-Craft Questions and Problems.

Math Attitude Survey

Unit 1

Math Attitude Survey

Name _____

1. I use my math in the world around me.
I agree I'm not sure I disagree
 ————— —————
2. Math is about exploring your thinking.
I agree I'm not sure I disagree
 ————— —————
3. Math is about solving real-world problems.
I agree I'm not sure I disagree
 ————— —————
4. I am good at math.
I agree I'm not sure I disagree
 ————— —————
5. Math is something I will never learn. I agree or
I agree I'm not sure I disagree
 ————— —————
6. Everyone can be good at math.
I agree I'm not sure I disagree
 ————— —————

7. For me, someone who is good at math is...

8. When I get the wrong answer to a problem, I feel...

9. When I don't know what to do to solve a problem, I...

10. For me, math is...

You may want to have your students complete the Math Attitude Survey to get a sense of their attitudes toward math and their self-perceptions of their math strengths and weaknesses.

Consider having them review their responses periodically throughout the school year to track any changes in their attitudes or self-perceptions.

Download and print the Math Attitude Survey from the Digital Teacher Center.



Unit Opener

Focus Question

Introduce the Focus Question: *What does it mean to do math?* Ask students to think about what they know about doing math.

- What do you notice about Dakota's classroom?
- What math do you see in the classroom?
- What math do you see outside the window?

Remind students that at the end of the unit, they will reflect on what they learned.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

Math in Action Video

Students can watch the Math in Action video.
Grade 5: Meet Dakota



IGNITE!

Name: _____

Map It

Using the fewest colors possible, color each state in the western United States so that no two states that share a boundary are the same color.

How many colors did you use? *Answers may vary.*



Try it a second time. Can you use fewer colors? *Answers may vary.*



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Ignite!

Map It

Students explore map coloring and the four color theorem, which states that no more than four colors are needed to color areas of a map so that no two adjacent areas have the same color.

1. Explain the task to student: They will color each state in the map provided using the fewest number of colors. No two adjacent states can be the same color.
 - How did you think about the problem?
 - What strategy did you use?
 - How did you determine the number of colors needed?
2. Have students try the second task using a different strategy.
 - How did the second strategy compare to the first?

Get Ready for Ignite!

Ignite! Activities, written by Dr. Raj Shah, launch every unit in *Reveal Math K–5*.

These activities are designed to

Cultivate Curiosity Mathematics is as much about asking questions as it is about finding solutions. Get your students to start wondering!

Accept the Challenge Attitude is everything. Encourage your students to take on new challenges and see how far they can go.

Trial and Error Students cannot learn by watching. To make sense of math, they have to try things... and keep trying.

Embrace “Failure” Learning new things is hard. Mistakes will happen. Allow your students the freedom to make mistakes and learn from them.

Work Together There is power in a community of learners working together to discover new things. Math should not be done alone.

Just Play Students can explore, discover, conjecture. Solving problems is fun!

Dr Raj Shah

Dr. Raj Shah has always had an affinity for math. Powered by his love of math, he earned a Ph.D. in Physics in 1999, which led to a career in R&D at Intel. In 2008, he left his job and founded Math Plus Academy, an after-school STEM enrichment program for students ages 5–14. His mission is to introduce students and adults to the wonders of mathematics. Dr. Shah also contributes his time to Math Teacher Circles, the Julia Robinson Math Festival, and is a founding member of The Global Math Project. He believes that everyone can enjoy math, develop strong number sense, and become a perseverant problem solver.

Learning Targets

- I can tell my math biography.
- I can recognize the ways in which we are all doers of math.

Standards • Major • Supporting • Additional

Content

4.OA.C.5 Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Construct viable arguments and critique the reasoning of others.

Vocabulary

Math Terms

hobby

Academic Terms

interview

Materials

The materials may be for any part of the lesson.

- bowl
- letter-size paper cut into quarters

Focus

Content Objective

- Students discuss the role of math in their and other people's lives.

Language Objective

- Students talk about how to use math while answering *Wh-* questions.
- To support cultivating language, ELs participate in MLR8: Discussion Supports.

SEL Objective

- Students describe their feelings and attitudes toward mathematics.

Coherence

Previous

- Students identified their superpowers and those of others.

Now

- Students think about their own and others' math biographies. They reflect on the mindsets that help them be effective doers of math.

Next

- Students continue to make connections between math and the real world. They increase awareness of the mindsets that help them do math.

Rigor

Conceptual Understanding

- Students understand that we each have our own math biography. Students investigate the role of math in our lives.

Procedural Skill & Fluency

- Students develop proficiency with identifying their areas of strength in doing mathematics.

Application

- Students apply their understanding of their math biography to target areas of strength in math.

Number Routine
Math Pictures  5–7 min

Build Fluency

Students build fluency with number sense as they examine a photograph and think about the numbers that can describe the picture.

These prompts encourage students to talk about their reasoning:

- What can you count?
- What can you measure?
- What fractions do you see?
- What can you compare?

Purpose Students discuss what someone could be writing about, including one's own or another person's story.

Notice & Wonder™

- What do you notice?
- What do you wonder?

See Appendix for a full description of the sense-making routines.

Teaching Tip You may want to facilitate a think-pair-share in order to encourage student participation. This may help students feel more at ease sharing their initial thoughts about the image.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about why people write, what they write about, and what a writer would include in a biography or autobiography.

- Why do you think the person is writing?
- What do you think the person is writing? What genre?
- Have you ever written in a journal or diary? Have you ever written a story about your own or someone else's life?
- If you were going to write a biography or autobiography, what types of information would you want to include?
- Why is it important to share stories from our own lives?
- What can we learn from hearing stories from other people's lives?

Transition to Explore & Develop

If students wonder how writing stories relates to math, guide the discussion to explore what thoughts, feelings, and experiences people can have in relation to math. This will be explored further in the Explore & Develop.

Establish Goals to Focus Learning

- Let's think about the thoughts and feelings people may have about math.



Learn
 Math is all around us. Notice it when you're watching a game, and in our neighborhood. We use it when we build projects, play games, or describe our feelings. We often use math every day.

Let's learn about our teacher's math biography.

How have you used math in the past?

Maths ... **Answer**
 When I go out with friends, we play.

How do you estimate now?

Maths ... **Answer**
 When I go to the store, I use math.

How do you think you will use math in your future?

Maths ... **Answer**
 I will use math in my job.

Do you ever yourself as good at math?

Maths ... **Answer**
 I am good at math because I can solve problems.

How do you use math when doing your favorite things?

Maths ... **Answer**
 I use math when I play sports.

Work Together
 What are some other questions you can ask about teacher's math biography?
Answers may vary.

1 Pose the Problem

Discussion Supports

As students talk about math stories, have them focus on how not only their story, but others' stories, can help aid them in their understanding of math. Restate statements they make as a question to seek clarification and provide vocabulary or grammar prompts for students who need more guidance.

In this lesson, students examine their attitudes about math. They listen to their teacher's math biography (or that of another adult) and then write about their math biography, focusing on their attitudes toward math and their perceived strengths in math.

Pose Purposeful Questions

- **Think About It:** What does it mean to have a math biography?
- Why might we want to learn about other people's math biographies?

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit Evidence of Student Thinking

- How does understanding other people's math biographies help us think about our own math biography?
- How does understanding our own math biography help us do our best work in math?

Key Takeaway

- We each have our own math biography. There are no wrong or right math biographies. Our math biographies are always evolving and changing.

Work Together

Students pose additional questions to the teacher about their math biography. When appropriate, students can be given an opportunity to answer the questions themselves in order to start thinking about their own math biographies.

Common Misconception: Students may believe that there is a right and wrong way to feel about math, as well as right and wrong math biographies. Explain that all feelings about math are valid and that all math biographies are valuable. Reframe any attitudes about emotional or academic struggle with math as opportunities for a growth mindset. Remind students that even professional mathematicians and scientists must work through math challenges.

Language of Math

Encourage students to use appropriate mathematics language when discussing their math biographies. Model the appropriate language when sharing your math biography as well.

Activity-Based Exploration

Students ask questions about their teacher's math story as they make connections between one's math biography and one's identity as a doer of math. Being honest in your answers will foster an open and accepting classroom culture and support constructive math communication moving forward.

Materials: bowl, letter-size paper cut into quarters (5 quarter pages per group)

Directions: Distribute a minimum of 5 pieces of paper to each group. After you answer each question on the student page, have each group brainstorm a follow-up question they would like to ask you. Each group decides on one follow-up question and writes this down on a slip of paper and places it in the bowl. Students may take turns being the recorder and writing the question for their group. Time permitting, try to make sure that each group has at least one follow-up question answered. Any unanswered questions may remain in the bowl and be answered at another time.

Activity Debrief: Have students share what they noticed and wondered about your math biography. As they share, ask them to think about the these questions.

Math is... Mindset

- How does your teacher use math during their day? When do you use math during your day?
- How does your teacher stay positive when they do math? How can you stay positive when you do math?
- What does your teacher want to learn about math? What do you want to learn about math?
- What are your teacher's strengths in math? What are your strengths in math?
- How does math help your teacher do their favorite things? How does math help you with your hobbies?

English Learner Scaffolds

Entering/Emerging Support students' understanding of *positive*. Smile confidently. Say *I'm being positive*. Next, slouch your shoulders, slightly frowning. Say *I'm not being positive*. Repeat once with new gestures, one positive and one negative, and then ask students *Am I being positive?*

Developing/Expanding Support students' understanding of *positive*. Smile confidently. Say *I'm being positive*. Next, slouch your shoulders, slightly frowning. Say *I'm not being positive*. Repeat once with new gestures and ask students to tell you about each one, eliciting answers containing *positive/not positive*. Provide sentence prompts for students who need more guidance.

Guided Exploration

Students explore the role math plays in their teacher's and their own lives. An open-format question and answer session with the teacher may lead the conversation in a variety of directions. Help build a classroom culture of trust and acceptance by welcoming all questions and points of view shared by the students. As the teacher, be honest about your own story and accepting of students' feelings and thoughts about math.

Facilitate Meaningful Discourse

- What questions do you have about your teacher's feelings about math?
 - Can you think of ways your teacher uses math that they may not be aware of?
 - In what ways are you a doer of math in your daily life?
- Have students work with a partner and ask each other questions about the other's math biography.

Math is... Mindset

- When do you use math during your day?
- How can you stay positive when you do math?
- What do you want to learn about math?
- What are your strengths in math?
- How does math help you with your hobbies?



Bridging/Reaching Ask students what things make them feel positive, and what they could do more often to keep positive instead of giving up. Then ask them to think of other words they may know that could be used instead of *positive*, such as *optimistic* and *cheerful*. Allow students to use a thesaurus or dictionary to find more similar words as well.

On My Own

Math GO

Write

What is my math biography?

Answers may vary.

Reflect

What about my math biography do I want someone else to know?

Answers may vary.

Practice

Build Fluency from Understanding

To help students write their math biography, have them consider these questions:

- What did you like about math last year? Why did you like that topic?
- What math topics did you find challenging last year? What made them challenging for you?
- What topics are you looking forward to learning this year?
- What is your favorite thing about math?
- What are your strengths in math?

Teaching Tip Remind students that math biographies can include both positive and negative feelings and experiences with math. Thinking about our strengths and what we like about math helps develop our identity as doers of math.

Reflect

Students complete the Reflect question.

- What about my math biography do I want someone else to know?

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can tell my math biography.
- I can recognize the ways in which we are all doers of math.

Exit Ticket Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 11
Exit Ticket

Name: _____

1. What are some ways that your teacher uses math every day?
Write at least two, what you know.

Answers will vary. Check students' answers.

2. What is one way you use math every day?

Answers will vary. Check students' answers.

Reflect On Your Learning

No (Confused) Not at all confident I am confident I got it! (I can teach someone else)



Assessment/Review Book 4

Math Is Exploring and Thinking

Learning Targets

- I can make sense of a problem and represent it in different ways.
- I can explain different ways to think about numbers.

Standards

Major Supporting Additional

Content

- **4.NF.B.4** Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.
- **4.NF.B.4.c** Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Reason abstractly and quantitatively.

Vocabulary

Math Terms

strategy

Academic Terms

analyze

Materials

The materials may be for any part of the lesson.

- coins: nickels, dimes, quarters

Focus

Content Objectives

- Students discuss approaches for making sense of a problem and determining strategies for solving it.
- Students look for connections among quantities.

Language Objectives

- Students talk about making sense of a problem and represent it in different ways while answering *Wh-* questions and using *another way*.
- To support optimizing output, ELs participate in MLR7: Compare and Connect.

SEL Objective

- Students recognize when they feel frustration during math class.

Coherence

Previous

- Students considered their own and others' math biographies. They reflected on the mindsets that help them be effective doers of math.

Now

- Students discuss approaches for making sense of a problem and determining strategies for solving it. They relate ways to represent quantities.

Next

- Students consider strategies for constructing arguments to support their ideas and solutions.

Rigor

Conceptual Understanding

- Students demonstrate understanding of the problem-solving process, with a focus on making sense of a problem and determining a viable solution plan.

Procedural Skill & Fluency

- Students build proficiency with the problem-solving process.

Application

- Students apply their understanding of the problem-solving process as they solve real-world problems.

Number Routine

Math Pictures 5–7 min

Build Fluency

Students are shown some plastic ducks, all except one of which are yellow and respond to the prompt, “What fractions can you use to describe the picture?”

These prompts encourage students to talk about their reasoning:

- How can we show the fractional part of a set?
- What does the denominator represent?



Purpose Students speculate on the number and value of two stacks of coins: one of quarters and one of dimes.

Notice & Wonder

- What do you notice?
- What do you wonder?

See Appendix for a full description of the sense-making routines.

Teaching Tip Students may be inclined to go directly to determining the value of each stack of coins rather than spending time making observations and asking questions. You may want to share some non-math-related observations or questions to help expand the discussion beyond a simple calculation.

1.1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about how to approach a problem situation in order to make sense of the problem and determine a solution plan.

- Which stack has more coins?
- What explains why there are the fewer quarters yet the stacks are about the same height?
- What explains why there are the more dimes yet the stacks are about the same height?

Transition to Explore & Develop

Ask questions that get students thinking about the different attributes of the coins – thickness, size, value – that need to be taken into consideration when determining which stack has the greater value and more coins. If students mention the greater value and thickness of the quarter compared to the dime, incorporate these ideas into the discussion; however, do not bring it up if students do not mention it. This will be explored further in the Explore & Develop.

1.1.2 Establish Goals to Focus Learning

- Let's think about the value of each coin as we determine the value of each stack.



Learn

Some coins in the coins in your bank. They had only quarters, dimes, and nickels.

How many of each coin can you have?

1 When are the coins not used every strategy to make several problems?

1 I can solve:

- 1. I have \$1.00 to get lunch.
- 2. I have two quarters, dimes, and nickels.
- 3. I have three quarters.
- 4. I have one nickel.
- 5. I have one dime.

Math 1A **Exploring**
Write all 10 ways about the problem!

1 I can solve:

- 1. I have many dimes and nickels would they need to be 100 cents? 20 dimes or 20 nickels?
- 2. I have many quarters would they be 40 cents? 20 dimes and 20 nickels in the bank?

Math 1A **Planning**
What amounts can I get?

1 When are the coins not used to solve problems, but sometimes you find by using 1 coin, like exploring and then give up.

1 I can solve several different questions of quarters, dimes, and nickels.

- 1. I have 1 coin, how many 20 quarters, 20 dimes, and 20 nickels?
- 2. I have 2 coins, how many 20 quarters, 20 dimes, and 20 nickels?

Math 1A **Perseverance**
What can I do if I struggle?

1 I can solve 1. I have 1 coin, how many 20 quarters, 20 dimes, and 20 nickels?

1 When are the coins not used to solve problems, but sometimes you find by using 1 coin, like exploring and then give up.

1 I can solve several different questions of quarters, dimes, and nickels.

- 1. I have 1 coin, how many 20 quarters, 20 dimes, and 20 nickels?
- 2. I have 2 coins, how many 20 quarters, 20 dimes, and 20 nickels?

Math 1A **Perseverance**
What can I do if I struggle?

1 I can solve 1. I have 1 coin, how many 20 quarters, 20 dimes, and 20 nickels?

Work Together

Reggie bought the bag of apples shown. She paid with notes, dimes, and quarters. How coins could Reggie use?

Sample answer: She could have used 13 quarters, 12 dimes, 11 nickels.

1 Pose the Problem

This is the first of four lessons that introduce students to the habits of mind that are foundational to doing math. In this lesson, the focus is on making sense of problem situations, formulating a solution plan, and representing quantities in different ways.

1.1 Pose Purposeful Questions

- What questions could you ask about the problem?
- What information do we have that can help us solve the problem?

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Compare and Connect

Pair students and ask each to write a combination of coins for a given dollar value, such as \$4.00. Have them work alone to form a combination, and then compare their combination with their partner. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

3.1 Elicit Evidence of Student Thinking

- If most of the coins are quarters, what does that tell you about the total number of coins?
- Could most of the coins be nickels? Explain your reasoning.

Key Takeaway

• There are different ways to solve problems, but a first step is always to make sense of the problem by asking questions about the problem. It is also important to be flexible in our thinking and implement alternate strategies as needed.

Work Together

Students solve a similar problem involving determining coins that sum to \$5.

Common Error: Students may struggle to get started with the open-endedness of the problem. Suggest students determine the number of one of the coin types and from that determine how many of the other coin types there would need to be.

3.2 Language of Math

Encourage students to talk of the fractional and decimal value of one dollar that each coin represents.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students explore the different parts of the problem-solving process, helping them develop flexibility and strategic thinking about problems and quantities.

Directions: Students work in pairs or small groups to solve the Pose the Problem.

Display these questions for students to ask themselves as they work on the problem presented:

- What do I know about the problem?
- What questions can I ask about the problem before looking to solve it?
- What might be another way to think about the problem if my first strategy does not help me solve the problem?
- How do the values and quantities in this problem relate?

Support Productive Struggle

- How are you approaching the problem? What assumptions are you making?

Activity Debrief: Before students share their solutions, have them talk through the first two questions that were displayed.

Students should note that there are some nickels, some dimes, and some quarters in the bank.

Among the questions students might ask are, “Are the numbers of each coin equal?”

Ask students whether their first strategy for solving the problem worked, or if any student pair had to try a different strategy.

- How did you think differently about the numbers of each coin?
- How did your thinking about the values and quantities of the different coins help you solve the problem?

As students share their solutions, display some of their solutions. Then have students talk through their strategies for solving the problem, focusing especially on the decisions around how to represent the problem.

English Learner Scaffolds

Entering/Emerging Support students understanding of *stuck*, *don't give up*, and *keep trying* through gestures. For example, pretend to be stuck on a task. Say *I'm stuck*. Then say *I don't give up*. *I keep trying*. Demonstrate not giving up and “completing” the task. Then ask students to first demonstrate *stuck* and then *don't give up/keep trying*.

Developing/Expanding Support students understanding of *stuck*, *don't give up*, and *keep trying* through gestures. For example, pretend to be stuck on a task. Say *I'm stuck*. Then say *I don't give up*. *I keep trying*. Demonstrate not giving up and “completing” the task. Then ask students to demonstrate the task as well. Provide sentence frames for students who need more guidance.

Guided Exploration

Students explore the different parts of the problem-solving process, helping them develop flexibility and strategic thinking about problems and quantities.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the first two “When we do math,...” statements.

- What does it mean to “make sense of a problem”?
- What do we do when we make sense of a problem?

Math is... Exploring

- What else do we know about the problem?

Math is... Planning

- Why is it important to ask questions before we solve a problem?

Math is... Perseverance

- Why should we always try to find another way to think about the problem?

Facilitate Meaningful Discourse

Engage students in a brief discussion of the third “When we do math,...” statement.

- What are some questions we can ask to determine the coins that are in the bank?

Math is... Quantities

- What are some other ways to think about the value of each coin?

Students can work in pairs or small groups to determine the possible number of each coin in the bank. As students share, ask them to explain their thinking.



Bridging/Reaching Ask students to think about how they handle times where they feel stuck. *Do you they give up, or do they keep trying?* Allow students to chime in with their thoughts. For example, *That's a great way of handling.... or When I get stuck, I...because....*

On My Own

Math

Large fourth-grade money value problems can be fun! The coins include quarters, dimes, nickels, and pennies. How many of each coin could she have?

Sample answer: She could have 33 quarters, 33 dimes, and 33 pennies.



Reflect

Tell about a time when you had a problem and you didn't give up. It might be a math problem, but it might be a problem you had at home, playing a game, playing a sport, playing an instrument, drawing a picture, or doing a puzzle.

Answers may vary.

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Practice

Build Fluency from Understanding

To help students build proficiency with the habits of mind for problem solving, have them consider these questions:

- How is this problem similar to the one we did together?
How is it different?
- What questions can you ask about this problem? How are the questions similar to the ones you asked for the other problems?

Reflect

Students complete the Reflect question.

- Tell about a time when you had a problem and you didn't give up. It might be a math problem. But it might be a problem you had at home, playing a game, playing a sport, playing an instrument, drawing a picture, or doing a puzzle.

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can make sense of a problem and represent it in different ways.
- I can explain different ways to think about numbers.

Exit Ticket  **Formative Assessment**

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 1-2
Exit Ticket

Name _____

- What operations do you always add parentheses you will always a problem?
Answers will vary. Check students' answers.
- Why is it important to look at base numbers when simplifying a problem?
Answers will vary. Check students' answers.

Reflect On Your Learning

How confident I am about my learning

1 2 3 4

1. Assessment Review Book

Learning Targets

- I can represent a real-world situation using mathematics.
- I can describe tools I can use to solve a problem.

Standards Major Supporting Additional

Content

4.NF.B.3.d Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

Math Practices and Processes

MPP Model with mathematics.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms

grid
model

Academic Terms

visualize

Materials

none

Focus

Content Objective

- Students consider different ways to use mathematics to represent a real-world situation.

Language Objective

- Students explain and show real-world phenomena with mathematical models while answering *Wh-* questions and using *visualize* and *represent* as needed.
- To support optimizing output, ELs participate in MLR4: Info Gap.

SEL Objective

- Students show appreciation for the different perspectives of their classmates.

Coherence

Previous

- Students discussed and refined their problem solving skills and process. They related ways to represent quantities.

Now

- Students consider models to represent real-world situations and problems. They choose tools that are appropriate for solving a given problem.

Next

- Students refine their skill in constructing arguments and in critiquing the reasoning of their classmates.

Rigor

Conceptual Understanding

- Students demonstrate understanding of how real-world situations and problems can be modeled with mathematics.

Procedural Skill & Fluency

- Students build proficiency with modeling with mathematics.

Application

- Students apply their understanding of modeling with mathematics to model real-world problems with mathematics.

Number Routine
Math Pictures  5–7 min

Build Fluency Students are shown an image of pumpkin seeds on a tray and respond to the prompt “How could you estimate the number of seeds?”

Encourage students to talk about their reasoning:

- What are some strategies you can use to estimate the number of seeds?

Purpose Students explore two wholes composed of different colors.

Notice & Wonder

- What do you notice?
- What do you wonder?

See Appendix for a full description of the sense-making routines.

Teaching Tip Some students may benefit from having physical versions of the two wholes available to explore.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about how real-world situations can be modeled using mathematics.

- Which color is used most in the first square? In the second square?
- How can you know which color is used most in each square?

Transition to Explore & Develop

Ask questions that get students thinking about comparing parts of a whole. If students comment that parts of a whole can have different shapes, incorporate that idea into the discussion; however, do not bring it up if students do not mention it. This will be explored further in the Explore & Develop.

Establish Goals to Focus Learning

- Let's think about the different ways to represent what part of the whole each color is.



Activity-Based Exploration

Students explore concepts related to modeling with mathematics. They expand understanding of the value of a mathematical model in understanding a problem or real-world phenomenon.

Materials: different-sized grids (4×4 ; 6×6 ; 10×10)

Directions: Students work in pairs. Each student colors in one grid using 3 different colors. Students swap their colored grids with their partner. Each partner comes up with different ways to represent the number of squares for each color. After each student has completed their representations, they can discuss their models and their thinking.

Display these questions for students to ask themselves as they work on the problem presented:

- How can I visualize the problem?
- How can I represent the problem?
- What tools can I use to represent and solve the problem?
- Which tool might work best for me to solve the problem?

Support Productive Struggle

- How can you determine which fractional part of a whole part each color is?

Activity Debrief: Before students share their solutions, have them talk through some of the questions that were displayed. Encourage students to share how they visualize and represent the problem. As appropriate, ask them to explain why they might visualize the problem different from how they represent it. As students talk about the tools they used, make sure they explain their thinking for choosing the tools they chose. As students share their solutions, have them explain their reasoning.

English Learner Scaffolds

Entering/Emerging Support students' understanding of *carry out*. Use manipulatives to carry out an operation. Say *I'm carrying out an operation*. Write a problem on the board and begin to solve it. Say *I'm carrying out an operation*. Turn to the Learn page and point to examples and non-examples of carrying out an operation. Ask each time *Does this show carrying out an operation?*

Developing/Expanding Support students' understanding of *carry out*. Use manipulatives to carry out an operation. Say *I'm carrying out an operation*. Write a problem on the board and begin to solve it. Say *I'm carrying out an operation*. Then ask students to demonstrate carrying out an operation. Be sure they say they're carrying out an operation while they do so.

Guided Exploration

Students explore concepts related to modeling with mathematics. They expand their understanding of the value of a mathematical model in understanding a problem or real-world phenomenon.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the first "When we do math..." statement.

- What does it mean to make a model of a problem?
- How can different models show a problem in different ways?

Math is... in My World

- What might be another way to visualize the problem?
- What might be another way to represent the problem?

Students think about how real-world problems can be both visualized and represented with mathematics. Emphasize to students the role that math plays in helping people understand aspects of real-world phenomena.

Ask students how the grid would change if two of the purple squares were changed to yellow. Students can work in pairs or small groups to update the different models.

Facilitate Meaningful Discourse

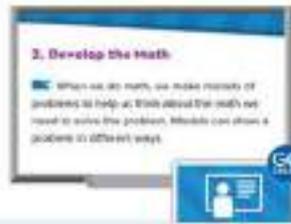
Engage students in a brief discussion for the second "When we do math..." statement.

- What tools did we use last year when working with fractions?
- What were some uses of those tools?

Math is... Choosing Tools

- What other tools might we use for this problem?

Students consider which tools are best suited for solving this problem. Some may propose fraction bars.



Bridging/Reaching Ask students to explain how to carry out a math operation of their choice. Allow students to interject, providing correction as needed. For example, *I don't think you carried out the operation. For example, you didn't.... or Are you sure...?*

On My Own

Work on your own.

Choose one item under the problem on the grid below. Color some of the squares blue, some yellow, some red, and some green. Find the fraction of the square for each color. And don't tell what you did. Show your partner your pattern in color.

Answers may vary.



Reflect

What did you do to represent a problem in math?

Answers may vary.

What tools do I prefer to use when solving problems involving fractions?

Answers may vary.

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Practice

Build Fluency from Understanding

To help students build proficiency with the habits of mind for modeling with mathematics and selecting appropriate tools, have them consider these questions:

- How is this problem similar to the one we did together?
How is it different?
- How can you represent this problem?
- What other tools could you use to solve this problem?

Reflect

Students complete the Reflect question.

- What are some ways to represent a problem in math?
- What tools do I prefer to use when solving problems involving fractions?

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to Reflect on the Learning Targets of the lesson.

- I can represent a real-world situation using mathematics.
- I can explain tools I can use to solve a problem.

Exit Ticket Formative Assessment

The *Exit Ticket* assess students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 1-3
Exit Ticket

Name: _____

- How can mathematical models help us understand the world?
Answers will vary. Check students' answers.
- What does it mean to approximate to solve problems that involve multiplication or division?
Answers will vary. Check students' answers.

Reflect On Your Learning

1 2 3 4

Not Confident Somewhat Confident Confident I got it! Approximate when



Mathematical Practices Book 18

Math Is Explaining and Sharing

Learning Targets

- I can construct an argument to explain my thinking.
- I can explain my thinking with clear and appropriate terms.

Standards

Major Supporting Additional

Content

4.NF.A.2 Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

Math Practices and Processes

MPP Construct arguments and critique the reasoning of others.

MPP Attend to precision.

Vocabulary

Math Terms

fractional

Academic Terms

critique

defend

justify

Materials

none

Focus

Content Objectives

- Students refine their skills in constructing arguments to support their thinking.
- Students respond to the ideas and arguments of others.

Language Objectives

- Students discuss arguments to support their thinking while answering *Wh-* questions and using *carefully* as needed and able.
- To support optimizing output, ELs participate in MLRT: Stronger and Clearer Each Time.

SEL Objective

- Students practice showing respect for classmates as they share ideas and thinking.

Coherence

Previous

- Students considered models to represent real-world situations and problems. They choose appropriate tools for solving a given problem.

Now

- Students refine their skill in constructing arguments and in critiquing the reasoning of their classmates.

Next

- Students analyze and generate patterns.

Rigor

Conceptual Understanding

- Students demonstrate understanding of the importance of supporting their solutions and ideas with viable arguments and responding constructively to the arguments of others.

Procedural Skill & Fluency

- Students build proficiency with building viable arguments.

Application

- Students apply their understanding of argumentations to evaluate the reasonableness of the arguments of others.

Number Routine

Math Pictures 5–7 min

Build Fluency Students are shown an image of two pea pods, one open to show the peas inside and the second closed. Students respond to the prompt “About how many seeds are in 125 pods?”

Encourage students to talk about their reasoning:

- What are some strategies you can use to estimate the number of seeds?



Purpose Students explore four wholes partitioned into different parts.

Which Doesn't Belong?

- Which doesn't belong?

See Appendix for a full description of the sense-making routines.

Teaching Tip You may want to model your thinking around one solution for *Which Doesn't Belong?* since this is the first time students have seen this routine this year. Remind students that for this routine there are always multiple solutions, so encourage students to find as many solutions as they can.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about how real-world situations can be modeled using mathematics.

- If one more section is shaded in each whole, how does that change which doesn't belong?
- If two more sections are shaded in each whole, how does that change which doesn't belong?
- What are some ways to describe the shaded part of each square?

Transition to Explore & Develop

Ask questions that get students thinking about what part of the whole is shaded in each square. If students mention benchmark fractions, incorporate that idea into the discussion; however, do not bring it up if students do not mention it. This will be explored further in the Explore & Develop.

Establish Goals to Focus Learning

- Let's think about the different ways we can use to compare parts of a whole.



Learn
 Start with these fractions in mind. How are they alike and how are they different? One of the fractions is a unit fraction.

What could these fractions be?

1 When we do math, we often need to explain our thinking. Sometimes you write numbers and symbols to make an argument.

Think Aloud: Explaining
 How can I justify my thinking?

Even just words is enough to clarify my thinking.

- The first fraction could be $\frac{1}{2}$ if it is less than 1 or $\frac{3}{2}$ if it is greater than 1.
- The second fraction could be $\frac{1}{3}$ if it is less than 1.
- The third fraction could be $\frac{1}{4}$ if it is greater than 1.

2 When we do math, we often use the arguments of others and then think about what makes sense and what doesn't.

3 Others might use different numbers and I sometimes disagree.

Think Aloud: Hearing
 What surprised both of us about thinking about the problem?

4 **Share It!** Tell to a partner and explain.

1 When we do math, we try to be precise in our arguments.

2 I used number lines to compare the fractions to see how much they differ.

3 I understand why what a unit fraction is.

4 We use correct vocabulary and make sure our arguments are accurate. We used our thinking and words to make an argument.

5 When we argued, we used numbers and mathematical symbols.

Work Together

The denominator of the $\frac{1}{2}$ and $\frac{1}{3}$ could be the three fractions. Do you agree with the classmate? What arguments can you construct to justify your position?

Sample answer: I do not agree because no fraction is less than $\frac{1}{2}$.

1 Pose the Problem

This is the third of four lessons that introduce students to the habits of mind that are foundational to doing math. In this lesson, students develop proficiency with constructing arguments to explain and defend their thinking and with responding to arguments of their classmates.

1.1 Pose Purposeful Questions

- What do we know about the problem?
- How useful is the information presented? Explain your thinking.

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Stronger and Clearer Each Time

Pair students and have them justify their thinking on a fraction problem like the one on the Learn page. Ask each to work individually and write what the two fractions could be and why. Then have students compare their writing and revise if needed. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

3.1 Elicit Evidence of Student Thinking

- How often were your arguments similar to your classmates'?
- What does that tell you?
- What new ideas or thinking did you gain from hearing your classmates' arguments?

Key Takeaway

- Constructing mathematical arguments and responding to the thinking and arguments of others are both important parts of doing mathematics.

Work Together

As students share out their responses, ask their classmates to evaluate the reasonableness of the argument presented.

Common Error: Students may think that there is just one argument in response to the solution presented. As students share their arguments, challenge others in the class to present a different argument.

3.2 Language of Math

Be consistent in your use of the term *argument* so that it becomes part of your students' active math discourse.

Activity-Based Exploration

Students refine their proficiency with constructing arguments to support their reasoning around the concept of comparing fractions. Students also analyze the arguments of their classmates to assess their validity.

Directions: Students work in pairs or small groups on the task in the Pose the Problem.

*Aisha has three fractions in mind.
Two are less than $\frac{1}{2}$ and one is greater than $\frac{1}{2}$.
One of the fractions is a unit fraction.
What could these fractions be?*

Display these questions for students to ask themselves as they work on the problem presented:

- How can I explain my thinking?
- Do I need an exact answer or an estimate?
- How can I make sure my thinking is clear and precise?

Support Productive Struggle

- What questions can you ask yourself to determine what the three fractions could be?

Activity Debrief: Before students share their solutions, have them talk through some of the questions that were displayed. Encourage students to share how they explained their thinking, whether they used words, drawings, or equations. Students can also share how they made sure their thinking is clear and precise.

Have one group share their solution with justification followed by the other groups responding to the presented solution in a respectful way. As students share their arguments, check that they are using appropriate mathematical terms. When students respond to the argument, remind them to address specifically the argument. Offer sentence starters, such as “I agree/disagree with your argument because...”

English Learner Scaffolds

Entering/Emerging Support students in understanding the word *argument*. Point to the first box on the Learn page. Point to each argument listed and say *This is one argument. This is another argument.* Then point to other parts of the Learn page, some that show arguments and some that don't. Ask *Is this an argument?*

Developing/Expanding Support students in understanding the word *argument*. Point to the first box on the Learn page. Point to each argument listed and say *This is one argument. This is another argument.* Then ask students to find other examples of arguments on the Learn page (second box).

Guided Exploration

Students explore constructing of arguments to support their reasoning around the concept of comparing fractions. Students also analyze the arguments of their classmates to assess their validity.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the first two “When we do math...” statements.

- What does it mean defend our thinking?
- What are some ways to defend our thinking?

Math is... Explaining

- Which way of explaining your thinking do you find most useful?

Students reflect on the importance of explaining their thinking around mathematical strategies and processes.

Students can work in pairs or small groups to find a different solution to the problem.

Math is... Sharing

- What are some strategies we can use to determine whether an argument makes sense to use?

Students consider how to evaluate an argument.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the next two “When we do math...” statements.

- Why is it important to be clear and specific when we explain our thinking?

Math is... Precision

- What are some strategies for making our arguments clear and precise?

Students consider how to communicate precisely when constructing arguments.



Do My Own

Write two more fractions in each box. One is a unit fraction that is less than $\frac{1}{2}$. Another is a unit fraction that is less than $\frac{1}{4}$. The total is greater than $\frac{1}{2}$ and is equivalent to $\frac{1}{2}$. What could these fractions be?

Sample answer: $\frac{1}{3}$, $\frac{1}{6}$, and $\frac{1}{6}$



Reflect

How did you create an argument and justify your thinking?
Answers vary.

Why do you think it is important to be precise in math?
Answers vary.

Practice

Build Fluency from Understanding

To help students build proficiency with the habits of mind for constructing arguments and critiquing the reasoning of others, have them consider these questions:

- What arguments can you construct to support your thinking?
- What terms can you use in your arguments?

Reflect

Students complete the Reflect question.

- How did you create an argument and justify your thinking?
- Why do you think it is important to be precise in math?

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can construct an argument to explain my thinking.
- I can explain my thinking with clear and appropriate terms.

Exit Ticket Formative Assessment

The *Exit Ticket* assess students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 1.4
Exit Ticket

Name _____

- Why is it important to share confidence when offering the reasoning of one's work?
Answers will vary. Check students' answers.
- How does using mathematical tools help make your arguments more precise?
Answers will vary. Check students' answers.

Reflect On Your Learning

1 2 3 4

Not confident Some confidence Confident Very confident



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Math Is Finding Patterns

Learning Targets

- I can use patterns to develop efficient strategies to solve problems.
- I can explain why patterns are useful to solve problems.

Standards

Major Supporting Additional

Content

4.OA.C.5 Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself.

Math Practices and Processes

MPP Look for and make use of structure.

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

Academic Terms

efficient
generalizations

Materials

none

Focus

Content Objectives

- Students consider strategies for uncovering patterns and for using patterns to solve problems.
- Students consider efficient strategies derived from repeated reasoning.

Language Objectives

- Students talk about strategies for uncovering patterns and for using patterns to solve problems while answering *Wh-* and *Yes/No* questions and using the verb *can* as needed.
- To support sense-making, ELs participate in MLR2: Collect and Display.

SEL Objective

- Students practice self-control as they learn to take turns when sharing ideas with a partner or in a group.

Coherence

Previous

- Students refined their skill in constructing arguments and in critiquing the reasoning of their classmates.

Now

- Students analyze and generate patterns.

Next

- Students determine classroom norms for a productive math learning environment.

Rigor

Conceptual Understanding

- Students demonstrate understanding of pattern analysis.

Procedural Skill & Fluency

- Students build proficiency with analyzing and generating patterns.

Application

- Students apply their understanding of patterns to solve problems.

Number Routine

Math Pictures 5–7 min

Build Fluency

Students are shown an image of a stack of rolls of pennies. Direct students respond to the prompt, “If there are 50 pennies in a roll, are there more or fewer than 400 pennies in the picture?”

Encourage students to talk about their reasoning:

- What are some strategies you can use to estimate the number of pennies?



Purpose Students explore the different patterns that can be seen in a sunflower.

Notice & Wonder

- What do you notice?
- What do you wonder?

See Appendix for a full description of the sense-making routines.

Teaching Tip Students may not be used to thinking about patterns in plants or animals, so you may want to model observations and questions about the pattern that can be seen in the sunflower.

Pose Purposeful Questions

The questions that follow can be used in any order. They are meant to help advance students' thinking about analyzing and generating patterns and are based on possible comments and questions students may make during the share out.

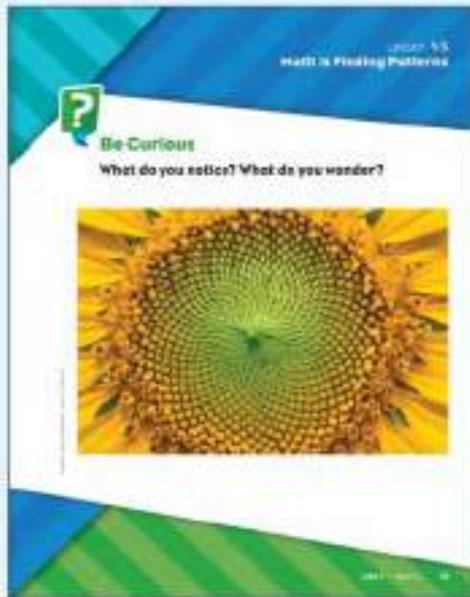
- What are other examples of patterns in nature?
- What are some considerations when thinking about patterns?

Transition to Explore & Develop

Ask questions that get students thinking about patterns in our everyday lives. If students mention number patterns, incorporate those concepts into the discussion, but do not introduce number patterns otherwise. These will be explored further in the Explore & Develop.

Establish Goals to Focus Learning

- Let's think about the patterns that we see in mathematics.



Learn
How are the equations related?

$3 \times 3 = 9$ $4 \times 3 = 12$
 $5 \times 3 = 15$ $6 \times 3 = 18$
 $7 \times 3 = 21$ $8 \times 3 = 24$

Math Is... Patterns
How are these related to patterns?

I have that I can a pattern when I see something, write one and read again.

- Some products are the same.
- There is a pattern with the factors.

$3 \times 3 = 9$ $4 \times 3 = 12$

$3 \times 2 = 6$ $4 \times 2 = 8$

$3 \times 4 = 12$ $4 \times 4 = 16$

Math Is... Patterns
How are these related to patterns?

When we do math, we use patterns to solve problems efficiently. Understanding helps us solve problems that are easier.

I can use the patterns above to solve these equations.

$3 \times 24 = 72$ $34 \times 3 = 102$ $34 \times 3 = 102$
 The product of 3 & 34 is 102. Use the pattern to find the product of 34 & 3.

$16 \times 12 = 192$ $16 \times 12 = 192$
 If I take a step in a fact, the product of the same as 8 x 24.

Math Is... Patterns
How are these related to patterns?

Search & Share Working together

Math Is... Patterns
How are these related to patterns?

When you do math, we look for rules or generalizations. Patterns can also help you solve problems that are easier.

Here are some rules to the equations.

$3 \times 24 = 72$ $4 \times 3 = 12$
 $4 \times 12 = 48$ $4 \times 12 = 48$
 $3 \times 12 = 36$ $4 \times 24 = 96$
 $16 \times 12 = 192$ $4 \times 48 = 192$

What are the rules? Is doubling the product is doubled?

Let's use this pattern to find other products.

- If I multiply 4 by 48 is 192.
- When I know that 4 x 56 is 224 and 4 x 58 is 232.
- When 2 x 192 = 384.

Math Is... Patterns
How are these related to patterns?

Work Together

$3 \times 8 = 24$ $3 \times 16 = 48$ $3 \times 32 = 96$ $3 \times 64 = 192$
 $4 \times 8 = 32$ $4 \times 16 = 64$ $4 \times 32 = 128$ $4 \times 64 = 256$
 $8 \times 8 = 64$ $8 \times 16 = 128$ $8 \times 32 = 256$ $8 \times 64 = 512$

How are these equations related? What other equations can you write that follow the same pattern?

Simple answer: When one factor is doubled, the product is doubled. Other equations include $12 \times 4 = 48$, $12 \times 8 = 96$, $5 \times 16 = 80$, so $5 \times 32 = 160$, $8 \times 16 = 128$, so $8 \times 32 = 256$.

1 Pose the Problem

Collect and Display

As students discuss the question, record relevant words they may use such as *patterns*, *relationships*, *products*, and *factors*. Display the words for student reference. Use the student-generated expressions to help students make connections between student language and math vocabulary.

This is the fourth of four lessons that introduce students to the habits of mind that are foundational to doing math. In this lesson, students build proficiency with analyzing patterns and making generalizations so that computation is more efficient.

Pose Purposeful Questions

- What do we know about the problem?

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit Evidence of Student Thinking

- How did you use patterns to make generalizations?
- How did you use rules or generalizations to help you solve the equations efficiently?

Key Takeaway

- Patterns and relationships are foundational to mathematics. Helping students recognize the importance of looking for patterns and making use of these patterns in problem solving will help them become more proficient doers of math.

Work Together

Students' share out should focus mostly on the patterns in the equations.

Common Error: Students may think that doubling both factors results in a product that is just double the original product. Have students work through the product when both factors are doubled by doubling first factor and solving, then doubling the second factor.

Language of Math

Check students' use of terms *patterns* and *relationships* as they describe the patterns.

Activity-Based Exploration

Students explore patterns in multiplication equations. Students look to make generalizations that can lead to efficient strategies.

Directions: Students work in pairs or small groups. Each group develops a series of up to 10 multiplication equations that follow a pattern. (The equations should not have solutions.)

Groups then trade their equations with those of another group. Each group describes the pattern that the equations show and a rule for solving equations efficiently using the pattern.

Display these questions for students to ask themselves as they work on the problem presented:

- What patterns can I see in the equations?
- How can the pattern help me solve the problem?
- Can this pattern help me work more efficiently?

Support Productive Struggle

- How can you sort the equations?
- Does that help you see a pattern?

Activity Debrief: Before students share their solutions, have them talk through some of the questions that were displayed.

Encourage students to share the pattern(s) they noticed in the equations. Students can also share their thinking on how the patterns they noticed helped them to solve the problem.

As groups share their solutions and their reasoning based on any patterns they noticed, encourage others to respond to the reasoning presented.

English Learner Scaffolds

Entering/Emerging Support students in understanding *If... then....* Go to your desk. Point to a drawer handle and say *If I pull this, it will open*. Demonstrate. Repeat the task with another object. Then go to the door and point to the doorknob. Ask *If I turn this, will the door open?* Then open a book and ask *If I close this, can I read it?*

Developing/Expanding Support students in understanding *If... then....* Go to your desk. Point to a drawer handle and say *If I pull this, it will open*. Demonstrate. Repeat the task with another object. Then go to the door and point to the doorknob. Ask *What will happen if I turn this?* Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to form a sentence using *If... then....* and to demonstrate. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, that's not correct because....* or *No, if you..., then....*

Guided Exploration

Students explore patterns in multiplication equations. Students look to make generalizations that can lead to efficient strategies.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the first two “When we do math,...” statements.

- How can we recognize a pattern?
- What kinds of patterns do we see in math?

Math is... Patterns

- How do we know when we see a pattern?
- How can we use the pattern to help us solve problems?

Students reflect on defining different kinds of patterns and thinking about their uses in problem solving.

Students can work in pairs or small groups to determine additional relationships between the equations.

Facilitate Meaningful Discourse

Engage students in a brief discussion for the next two “When we do math,...” statements.

- Why should we always look for patterns when solving a problem or an equation?

Math is... Generalizations

- Are there generalizations we can make about the patterns that can help us work more efficiently?

Students consider the applicability of generalizations to problem solving.



On My Own

Write the following equations without a calculator.

$4 \times 3 = 7$	$7 \times 10 = 7$	$9 \times 6 = 7$	$8 \times 8 = 7$
$6 \times 6 = 7$	$7 \times 30 = 7$	$3 \times 9 = 7$	$2 \times 9 = 7$
$5 \times 35 = 7$	$7 \times 60 = 7$	$9 \times 34 = 7$	$3 \times 32 = 7$

Sample answer: When one factor is doubled, the product is doubled.

What other equations can you write that follow the same pattern?

Sample answers: $10 \times 12 = 24$, $10 \times 32 = 320$, $44 \times 10 = 440$, $15 \times 9 = 144$

Reflect

What other patterns and relationships do you know about in math? Tell how these patterns have helped you.

Answer may vary.

How can patterns help you solve problems or equations?

Answer may vary.

Practice

Build Fluency from Understanding

To help students build proficiency with the habits of mind for analyzing patterns and making generalizations, have them consider these questions:

- What patterns do you notice?
- How can the patterns help you solve equations more efficiently?

Reflect

Students complete the Reflect questions.

- What other patterns and relationships do you know about in math? Tell how those patterns have helped you.
- How can patterns help you solve problems or equations?

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use patterns to develop efficient strategies to solve problems.
- I can explain why patterns are useful to solve problems.

Exit Ticket  **Formative Assessment**

The *Exit Ticket* assess students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 1-5
Exit Ticket

Name _____

- What six ways patterns that you notice when multiplying (include and whole number)?
Answers will vary. Check students' answers.
- How can the patterns you notice that you multiply more efficiently?
Answers will vary. Check students' answers.

Reflect On Your Learning

No confidence Getting ready I understand I can teach someone else



Assessment Source: [www.illustrativemathematics.org](#)

Learning Targets

- I can recognize the behaviors and attitudes that support a productive classroom learning environment.
- I can identify the mindsets that help me problem solve.

Standards

Major Supporting Additional

Content

4.NF.B.3.d Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators.

Math Practices and Processes

- MPP** Make sense of problems and persevere in solving them.
- MPP** Construct viable arguments and critique the reasoning of others.
- MPP** Use appropriate tools strategically.

Vocabulary

- | | |
|-------------------|-----------------------|
| Math Terms | Academic Terms |
| | norms |
| | responsibility |

Materials

The materials may be for any part of the lesson.

- geoboards or *Dot Paper* Teaching Resource
- pattern blocks or *Pattern Blocks 2* Teaching Resource

Focus

Content Objective

- Students discuss classroom norms of interaction for a productive learning environment.

Language Objectives

- Students talk about the behaviors and mindsets that contribute to a productive learning environment while answering *Wh-* and *Yes/No* questions and using the verb *disagree* and the adverb *respectfully* as needed.
- To optimize output, ELs participate in MLR7: Compare and Contrast.

SEL Objective

- Students make decisions about classroom norms for working productively with classmates.

Coherence

Previous

- Students identified the classroom norms that lead to productive math work.

Now

- Students discuss classroom norms of interaction for a productive math learning environment. They reflect on how to problem solve effectively.

Next

- Students continue to reflect on the behaviors and mindsets that help them work collaboratively and independently on challenging math tasks.

Rigor

Conceptual Understanding

- Students demonstrate an understanding of the expectations and agreements that promote a productive and positive learning environment

Procedural Skill & Fluency

- Students develop proficiency in recognizing and reflecting upon the behaviors that support their work as doers of math.

Application

- Students apply their understanding of a productive learning environment to contribute to a positive classroom culture.

Number Routine

Math Pictures 5–7 min

Build Fluency Students examine a photograph of decorations on hooks and estimate what fraction of the decorations are missing.

These prompts encourage students to talk about their reasoning:

- How does the word “about” in the question affect how you will find the answer?
- Is there one correct answer to this question?



Purpose Students think about behaviors of productive group work.

Notice & Wonder

- What do you notice?
- What do you wonder?

See Appendix for a full description of the sense-making routine.

Teaching Tip You may want to facilitate a think-pair-share in order to encourage student participation. This may help students feel more at ease sharing their initial thoughts about the image.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about the mindsets and behaviors that facilitate group work, both in general and when learning math and are based on possible comments and questions students may make during the share out.

- What might the students be working on?
- If this image became a video (in other words, went from a still shot into a video recording), what do you think you would see and hear?
- What is hard about sharing a device with another student? What is fun about it?
- What do you like about group work? What do you like about individual work?

Transition to Explore & Develop

Ask questions to get students thinking about the factors that help make the classroom a productive learning environment.

Establish Goals to Focus Learning

- Let's think about what helps make our classroom a positive and productive place to learn.



Learn

How do we do math?

1. When we do math, we often work together.

- We value ourselves.
- We share our thinking.
- We are respectful of others' ideas.
- We engage one another so that we learn together better.
- We don't work when playing others.

Math 1.0 Mindset
What can I learn from another student?

2. When we do math, sometimes we work alone first.

- We only try once.
- We only try to solve independent math.

Math 1.0 Mindset
What can I learn from the answer?

3. When we do math, we solve problems.

- We make sense of problems.
- We order and think the problem and the situation among the students.
- We don't quit. If we get stuck, we look for different ways.
- We get stuck. We work the problem until we find a way.
- We look for patterns.

Math 1.0 Mindset
What can I learn from the problem?

24 | **Learn** | Unit 1.0

Work Together

- What rules should we have when we share our thinking with classmates?
Answers may vary.
- What ways do you think help classmates best contribute to math class?
Answers may vary.
- How do we give feedback respectfully?
Answers may vary.
- How can I know when I need help?
Answers may vary.

25 | **Work Together** | Unit 1.0

1 Pose the Problem

In this lesson, students establish the classroom norms that foster the development of the mathematical habits of mind and thinking habits that have been focus of previous lessons.

- 1.1.1 Pose Purposeful Questions**
- Think About It:** How do we do math?
 - What behaviors and mindsets help us do math?

2 Develop the Math

Choose the option that best meets your instructional goals.

- 1.1.2 Compare and Contrast**
- Pair students and prompt them to identify and explain ways they can do math, e.g. work together, work on their own, and solve problems. Have them compare the strategies, reflect on how they are the same and different, then discuss their preferences for one or the other approach.

3 Bring It Together

- 1.1.3 Elicit Evidence of Student Thinking**
- What class agreements can help us do our best math work?
 - What attitudes help us as doers of math?

Key Takeaways

- For group work to be productive, we must listen attentively, share our thinking, and be respectful of others.
- To productively work on our own, we should stay focused and ask for help when we are stuck.
- A natural part of doing math is working through challenges. Certain mindsets and behaviors can help us as we work through challenges.

Work Together

Students think further about rules and practices that support classroom math work. You may want to have students work in pairs on the activity before sharing their work.

Common Misconception: Students may believe that successful groups do not ever disagree. Explain that disagreements can lead to new ideas and creative group problem-solving.

1.1.4 Language of Math

Model for students appropriate mathematical language around problem solving, making clear the difference between a problem and an exercise or an assessment item.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students work in groups on an open-ended math problem and reflect upon the process of working collaboratively.

Materials:

Option 1: pattern blocks, virtual pattern blocks, or *Pattern Blocks 2* Teaching Resource

Option 2: geoboards and rubber bands (1 board and 16 bands per group), virtual geoboards, or *Dot Paper* Teaching Resource

Directions: Groups work together on one of the following problems:

Option 1: Pattern Block Challenge The hexagon is worth 1 whole. Use pattern blocks to create a design that is equal to 10 wholes.

Option 2: Geoboard Challenge Using 12 to 16 rubber bands, create a design that appears the same as you turn it, no matter which side of the geoboard is up.

As students work in groups, encourage them to observe how their groups communicate, cooperate, cultivate inclusivity, and deal with conflict.

Support Productive Struggle

- How are you communicating your ideas when you disagree?
- How can you work through conflict when collaborating with others?
- Is the finished work going to look the same as it would have if you had worked on it by yourself?

Activity Debrief: Review the classroom behaviors and skills that support productive learning. As students share, ask them to think about these questions.

Math is... Mindset

- What can you do to be an active listener?
- What can you do to stay focused on your work?
- What can you do when you feel frustrated?

PDFs of the Teaching Resources are available in the Digital Teacher Center.



Guided Exploration

Students think about what behaviors and attitudes support productive group work and individual work. They also consider strategies that help them work through challenging math problems. Model active listening and allow students to share any thoughts or feelings they have about the topics being discussed. Explore with students the role of conflict in group work and the skills students can use to work through disagreements as they arise.

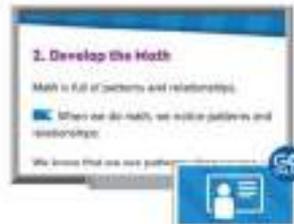
Facilitate Meaningful Discourse

- What are the benefits of group work? What are the challenges?
- How can we ensure that all members of a group are included?
- What does respect look like when working with others on math?
- How can we disagree while remaining respectful?
- What habits help us work independently?
- What can we do when we get stuck on a challenging math problem?

 Have students discuss with a partner what they do when they get frustrated doing math.

Math is... Mindset

- What can you do to be an active listener?
- What can you do to stay focused on your work?
- What can you do when you feel frustrated?



English Learner Scaffolds

Entering/Emerging Support students' understanding of *work together* and *on your own*. Work on a task by yourself. Say *I'm working on my own*. Have a student help you. Say *We're working together*. Group students, some individually and others in pairs or groups, and assign them a task. Say *Point to a student who is working on their own*. Then say *Point to students who are working together*.

Developing/Expanding Support students' understanding of *work together* and *on your own*. Work on a task by yourself. Say *I'm working on my own*. Have a student help you. Say *We're working together*. Then ask students to repeat the task, using *on my own* and *working together*. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to talk about the pros and cons of both *working together* and *on your own* and to explain their reasoning. Provide sentence prompts when necessary and suggest to students that they think of similar-meaning words and phrases that may help them with their explanations, such as *individually/by myself* or *working in pairs/groups*.

On My Own

Name: _____

What are two promises our class can make so that we always work well together?

Answers may vary.



Reflect

What are my responsibilities to make sure we all learn math productively?

Answers may vary.

Practice

Build Fluency from Understanding

To help students think about promises the class can make in order to work well together, have them consider these questions:

- Imagine you are observing a group working well together. What would you see and hear?
- What helps you focus when working on your own?
- What steps can you take when you are working on a challenging math problem?

Reflect

Students complete the Reflect question.

- What are my responsibilities to make sure we can all learn math productively?

Ask students to share their reflections with their classmates.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can recognize the behaviors and attitudes that support a productive classroom learning environment.
- I can identify the mindsets that help me problem solve.

Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assess students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.



Lesson 1-6
Exit Ticket

Name _____

- How do we compare the ideas of reflect responsibility?
Answers will vary. Check students' answers.
- What is the most important idea we learned from this lesson?
Answers will vary. Check students' answers.

Reflect On Your Learning

1. I understand
2. I understand
3. I understand
4. I understand

1 2 3 4

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Unit Review

Unit Review Name _____

Vocabulary Review

1. What does it mean to defend your thinking?
Answers may vary.
2. Why is it possible to solve a problem backwards?
Answers may vary.
3. How can we decide when it is better not to solve a problem?
Answers may vary.
4. What are some examples of patterns in the world you did not see?
Answers may vary.

Unit 1 Review 27

Review

Write a card for the classroom review for doing math!
Write up to 5 items. *Answers may vary.*

- 1.
- 2.
- 3.
- 4.
- 5.

Reflect

Choose one of the items you wrote and tell why it is important.
Answers may vary.

Unit 1 Review

Students can complete the **Unit Review** to review concepts presented in the unit. Students may complete the Review in their Interactive eBook in the Digital Student Center.

Fluency Practice

Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students practice using partial sums to add.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Unit 5
Fluency Practice

Name: _____

Fluency Strategy
Use your partial sums to solve the problem.

Partial Sums

$$\begin{array}{r} 281 \\ + 222 \\ \hline 503 \end{array}$$

$$\begin{array}{r} 503 \\ + 222 \\ \hline 725 \end{array}$$

$$\begin{array}{r} 725 \\ + 222 \\ \hline 947 \end{array}$$

5. Use double sums to find the sum.

$$\begin{array}{r} 522 \\ + 222 \\ \hline 744 \\ + 222 \\ \hline 966 \end{array}$$

Fluency Flash
Add the two sets of blocks. Write the addition equation.

221 + 317 = 548

Unit 5, Lesson 5, 29

Fluency Check

What is the sum?

3. $722 + 128 =$ 850	8. $702 + 239 =$ 941
4. $308 + 191 =$ 499	9. $230 + 402 =$ 632
5. $302 + 223 =$ 525	10. $276 + 587 =$ 863
6. $423 + 188 =$ 611	11. $918 + 589 =$ 1507
7. $508 + 182 =$ 690	12. $412 + 220 =$ 632

Fluency Talk

Write one addition equation (3-digits) and one subtraction equation (3-digits) using partial sums. Explain how you found the sum.

Explanations may vary.

Write one addition equation (2-digits) and one subtraction equation (2-digits) using partial sums to solve the problem. Explain how you found the sum.

Explanations may vary.

PACING: 10 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  Painted Cubes	Students use connecting cubes to build a cube. They relate what they build to volume.		
2-1 Understand Volume	Students understand volume is a measurable attribute of 3-dimensional figures. Students understand that a rectangular prism can be packed using unit cubes with no gaps or overlaps to establish volume.	<ul style="list-style-type: none"> Students talk about ways to measure volume using the verb <i>find</i>. 	Students use prior knowledge and new understanding of mathematical concepts to complete a task, building stronger self-efficacy.
2-2 Use Unit Cubes to Determine Volume	Students determine the volume of a rectangular prism by counting unit cubes. Students determine the volume of a rectangular prism by multiplying the number of unit cubes in one layer by the number of layers.	<ul style="list-style-type: none"> Students discuss how to determine the volume of any 3-dimensional solid by counting unit cubes while answering <i>Wh-</i> questions. 	Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing thoughtful and constructive feedback.
2-3 Use Formulas to Determine Volume	Students determine the volume of rectangular prisms using formulas.	<ul style="list-style-type: none"> Students explain how to determine the volume of rectangular prisms using formulas while answering <i>Wh-</i> and Yes/No questions and using the term <i>dimensions</i>. 	Students practice strategies for persisting at a mathematical task, such as setting a small goal or setting timers for remaining focused.
Math Probe Volume of Rectangular Prisms	Gather data on students' understanding of determining volume of rectangular prisms.		
2-4 Determine Volume of Composite Figures	Students determine the volume of composite solid figures.	<ul style="list-style-type: none"> Students discuss how to determine the volume of composite solid figures while answering <i>Wh-</i> questions. 	Students engage in active listening and work collaboratively with a partner to complete mathematical tasks.
2-5 Solve Problems Involving Volume	Students apply the volume formulas to solve real-world problems involving rectangular prisms.	<ul style="list-style-type: none"> Students talk about applying the volume formula to solve real-world problems using the adjective <i>given</i>. 	Students determine the strategies and analyses necessary to make informed decisions when engaging in mathematical practices.
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION:
How can I find the volume of rectangular prisms?

LESSON	KEY VOCABULARY	MATERIALS TO GATHER	RIGOR FOCUS	STANDARD
2-1	<p>Math Terms</p> <ul style="list-style-type: none"> rectangular prism unit cube volume <p>Academic Terms</p> <ul style="list-style-type: none"> analyze establish 	<ul style="list-style-type: none"> <i>Nets Teaching Resource</i> centimeter cubes marbles, beans, or other measurement units 	<ul style="list-style-type: none"> Conceptual Understanding 	<ul style="list-style-type: none"> 5.MD.C.3 5.MD.C.3.a
2-2	<ul style="list-style-type: none"> cubic unit unit cube volume <p>debate</p> <p>suggest</p>	<ul style="list-style-type: none"> centimeter cubes <i>Nets Teaching Resource</i> 	<ul style="list-style-type: none"> Conceptual Understanding Procedural Skill & Fluency 	<ul style="list-style-type: none"> 5.MD.C.3.a 5.MD.C.3.b 4.MD.C.4
2-3	<p>base (of a solid)</p> <p>formula</p> <p>assert</p> <p>evaluate</p>	<ul style="list-style-type: none"> cubes 	<ul style="list-style-type: none"> Conceptual Understanding Procedural Skill & Fluency Application 	<ul style="list-style-type: none"> 5.MD.C.5.a 5.MD.C.5.b
2-4	<p>composite solid</p> <p>figure</p> <p>formula</p> <p>complex</p> <p>speculate</p>	<ul style="list-style-type: none"> <i>Nets Teaching Resource</i> ruler unit cubes 	<ul style="list-style-type: none"> Conceptual Understanding Procedural Skill & Fluency Application 	<ul style="list-style-type: none"> 5.MD.C.5.c
2-5	<p>equation</p> <p>formula</p> <p>unknown</p> <p>variable</p> <p>relevant</p> <p>valid</p>	<ul style="list-style-type: none"> <i>Problem-Solving Tool Teaching Resource</i> 	<ul style="list-style-type: none"> Procedural Skill & Fluency Application 	<ul style="list-style-type: none"> 5.MD.C.5.b

Unit Overview

Focus

Volume

In this unit, students explore measurable attributes of different figures and discover that all 3-dimensional figures have a measurable attribute of the space inside, which is called volume. They discover that volume can be measured by packing the figure with unit cubes and that there must be no gaps or overlaps of the unit cubes.

Students extend their understanding of multiplication as equal groups to discover that the volume of a rectangular prism can be calculated by multiplying the number of unit cubes in one layer by the number of layers. Students generalize methods for calculating volume of rectangular prisms to derive the formulas $V = l \times w \times h$ and $V = B \times h$.

Students discover that volume is additive. They can calculate the volume of composite solid figures by decomposing the figure into rectangular prisms, then add the volumes.

Students apply the volume formulas to solve real-world problems, including problems involving unknown dimensions.

Coherence

What Students Have Learned

- **Area** Students described area as an attribute of plane figures and understood concepts of area measurement. (Grade 3)

What Students Are Learning

- **Volume** Students describe volume as an attribute of solid figures and understand concepts of volume measurement.
- **Determining Volume** Students determine volumes by counting unit cubes and using formulas.
- **Composite Solid Figures** Students determine volumes of composite solid figures.
- **Real-World Problems** Students solve real-world volume problems.

What Students Will Learn

- **Volume** Students find the volume of a right rectangular prism with fractional edge lengths. (Grade 6)

Rigor

Conceptual Understanding

Students develop understanding of

- volume as an attribute;
- concepts of volume measurement.

Procedural Skill and Fluency

Students build proficiency with

- counting cubes to determine volume;
- using formulas to determine volume;
- determining the volume of composite solid figures.

Application

Students apply their knowledge of

- using volume formulas to solve real-world volume problems;
- decomposing figures to solve real-world volume problems.

Effective Teaching Practices

Elicit and Use Evidence of Student Thinking

Look for evidence of student thinking and evaluate their growth toward conceptual understanding. Before, during, and after learning a new skill or concept, students should be assessed to see if they are understanding the new information or if they have any misconceptions of past information. Collecting evidence of students' thinking can be as simple as asking clarifying questions or it can be as complex as having students complete an in-depth project.

Assessment is continuous because students' understanding drives instruction. Sometimes topics that have been previously covered need to be approached in a different way because students may be struggling with a prior topic that is stopping future learning from occurring.

As you encounter different concepts in these lessons, spend time using evidence of student thinking to advance instruction.

- Determine what evidence you will be looking for and how you will respond based on students' learning trajectories. Use this evidence in planning next steps in your instruction.
- Ask students why they chose a particular strategy to represent their work. Take note of their reasoning and equations in order to facilitate the share portion of the lesson.
- As students engage in mathematical discourse, determine how to respond to what they say in order to deepen their conceptual understanding.

Mathematical Practices and Processes

Model With Mathematics

Using and connecting multiple mathematical representations is an important first step in helping students build proficiency with using models in math.

When students model with mathematics, they use different representations, especially visual and concrete representations, to help them solve problems. As they model the mathematics, they build an understanding of which representations better help them reach a solution. Building proficiency with modeling the mathematics using different representations provides a strong foundation to help students become problem-solvers. Building the foundation for modeling with mathematics prepares students for their middle and high school work.

To help students build proficiency with modeling, students need opportunities to interact with different representations. Some suggestions for building proficiency include:

- Students should recognize that if a rectangular prism were packed with unit cubes, the area of the base represents the number of cubes in each layer, and the height represents the number of layers.
- Students use unit cubes to build 3-dimensional figures, allowing them to apply the mathematics necessary to solve problems.
- As students seek to determine the volume of rectangular prisms or a missing dimension given the volume, they need to consider what information they have. Encourage students to state the formula they are using and the variables whose values they know before solving for an unknown variable.

Social and Emotional Learning

What Skills Will We Develop?

- **Self-Awareness: Self-Efficacy** (Lesson 2-1) Students with high self-efficacy are more likely to persevere to complete a challenging task.
- **Social Awareness: Appreciate Diversity** (Lesson 2-2) Diversity appreciation can help students collaborate well with peers.
- **Self-Management: Control Impulses** (Lesson 2-3) Students who can control their impulses are more likely to persist through challenging tasks.
- **Relationship Skills: Build Relationships** (Lesson 2-4) Building positive relationships can help establish a strong classroom community.
- **Responsible Decision-Making: Solve Problems** (Lesson 2-5) Efficient problem solvers can make informed decisions that lead to solutions.

Language of Math

Vocabulary

Students will be using these key terms in this unit:

- **Volume*** (Lesson 2-1): This is a new term. It is a measure of the amount of space occupied by a 3-dimensional figure.
- **Unit cube*** (Lesson 2-1): This is also new term. Students were introduced to unit squares when determining area in Grade 3.
- **Cubic unit*** (Lesson 2-2): This is also a new term. Students were introduced to different kinds of units when determining area in Grade 3. They may be more familiar with square units.

- **Formula*** (Lesson 2-3): This is also a new term. A formula is an equation that represents the relationship between two or more quantities. Students may recall the area formula used in Grade 4.
- **Rectangular prism*** (Lesson 2-3): This is also a new term. A rectangular prism has six rectangular faces.
- **Composite solid figure*** (Lesson 2-4): This is also a new term. Students found the area of composite 2-dimensional figures in Grade 3.

*This is a new term.

Math Language Development

A Focus on Listening

Listening to mathematical concepts can be extremely helpful because listening to other strategies and explanations can be eye-opening and informative. Students may have never even considered a certain approach to a problem or may discover that they did not understand the problem or concept correctly.

However, listening to other strategies and explanations can also be difficult if students do not agree with the explanations, if the explanations are more complex than they need to be, or if students cannot grasp the concepts. In these cases, students may need alternate explanations of concepts and problems or discussions about whether the strategies are correct.

In this unit, students can listen to explanations about mathematical topics in order to gain a better understanding about

- how to find volume using the terms unit cubes and cubic units correctly;
- how to find the volume of a rectangular prism using key terms;
- the decision-making process involved with decomposing figures;
- how to find unknown edge lengths;
- what strategies worked and what strategies did not work as students attempted to solve volume problems.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain volume. Because many of the words and phrases used in this section are likely unfamiliar or unknown, students are supported in understanding and using these words.

Lesson 2-1 – *fill, pack*
Lesson 2-2 – *gap, overlaps*
Lesson 2-3 – *dimensions*
Lesson 2-4 – *that compose it*
Lesson 2-5 – *given*

Unit Routines

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

Would You Rather?

Purpose: Build flexibility with number sense and mental math operations; enhance decision-making.

Overview: Students choose between two options, both of which require mental computation. Students explain their choice and their rationale for their choice.

Can You Make the Number?

Purpose: Build flexibility with numbers.

Overview: Students use all the given numbers to build expressions with a value matching the target number. Students can use a range of operations in their expressions. The teacher records students' expressions, then facilitates a discussion about students' expressions.

Where Does It Go?

Purpose: Build estimating skills using benchmarks.

Overview: Students place a target number on number lines with different endpoints and justify their placement. In some instances, as a challenge, the target number may not actually belong on one of the number lines.

Sense-Making Routines

Notice and Wonder™: How are they the same? How are they different? (Lessons 2-1, 2-4, 2-5) In Lesson 2-1, students discuss and share their thoughts about similarities and differences among 2-dimensional and 3-dimensional objects.

Notice and Wonder™: What do you notice? What do you wonder? (Lessons 2-2, 2-3) In Lesson 2-2, students discuss and share their thoughts about filling a space with objects so that there are no gaps or overlaps.

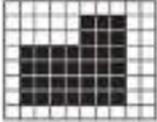
Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. These routines can also be used as formative assessment opportunities as students develop proficiency in English and mathematical language. They can be used in ways that support real-time-, peer-, and self-assessment. For more information on the Mathematical Language Routines, see the Appendix.

- **Lesson 2-1** – In order to support sense-making and maximize linguistic, students participate in MLR2: Collect and Display so that students' oral words and phrases can be captured into a stable, collective reference.
- **Lesson 2-2** – In order to optimize output, students participate in MLR3: Critique, Correct, and Clarify so that they have an opportunity to analyze, reflect on, and develop a piece of mathematical writing that is not their own.
- **Lesson 2-3** – In order to support cognitive meta-awareness and optimize output, students participate in MLR1: Stronger and Clearer Each Time so that students have a structured and interactive opportunity to revise and refine both their ideas and their verbal and written output while solving such problems.
- **Lesson 2-4** – In order to optimize output, students participate in MLR5: Co-Craft Questions and Problems so that they have a structured and interactive opportunity to create, solve, and share their own problems for determining the volume of composite solid figures.
- **Lesson 2-5** – In order to cultivate conversation and optimize output, students participate in MLR8: Discussion Supports so that they can have a rich and inclusive discussion about the tools and strategies they can use to apply volume to solve real-world problems.

Unit 2
How Ready Am I?

Name: _____

- Which of the following shapes always has two pairs of parallel sides and four right angles?
 - A. trapezoid
 - B. rectangle
 - C. square
 - D. parallelogram
- What is the area of the rectangle?
 
 - A. 75 square units
 - B. 70 square units
 - C. 12 square units
 - D. 20 square units
- Find the value of the expression $2 + 3 \times 4$.
 - A. 7
 - B. 10
 - C. 20
 - D. 34
- Make a shape of a figure on grid paper.
 

What is the area of the figure?

 - A. 25 square units
 - B. 20 square units
 - C. 33 square units
 - D. 38 square units

Answer Record Book 14

- A rectangular rug is 12 feet long and 9 feet wide. What is the area of the rug?
 - A. 21 square feet
 - B. 42 square feet
 - C. 108 square feet
 - D. 198 square feet
- Ms. Garcia is packing boxes for a storage bin. The total sum of all boxes has a total area of 150 square feet. How many boxes of the same size can she pack?
 
 - A. 15 square feet
 - B. 25 square boxes
 - C. 30 square boxes
 - D. 35 square boxes
- Mr. Garcia wants to use garden to cover exactly 48 square feet. What of the following dimensions could he use for the garden?
 - A. 6 feet by 8 feet
 - B. 7 feet by 8 feet
 - C. 8 feet by 6 feet
 - D. 9 feet by 6 feet
- Find the sum of the expression.

$$[(3 + 5) \times 2]$$
 - A. 16
 - B. 17
 - C. 18
 - D. 19

Answer Record Book

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

14 Use Guided Support Intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill	Item Skill	Guided Support Intervention Lesson	Standard
1	3	Identify 2-D figures	Use Lines to Classify Shapes	4.G.A.2
2	1	Find area of rectangles by counting tiles	Area Using Tiling and Counting	3.MD.C.6
3	1	Evaluate expressions using Associative Property of Multiplication	Multiply Three Numbers	3.OA.B.5
4	2	Decompose composite figures to find area	Decompose Shapes to Find Area (Grids)	3.MD.C.7.d
5	2	Use a formula to find area	Area of Rectangles and Squares	4.MD.A.3
6	2	Find area in composite figures	Decompose Shapes to Find Area	3.MD.C.7.d
7	2	Understand area	Area of Rectangles and Squares	4.MD.A.3
8	1	Evaluate expressions	Rearrange Factors	3.OA.B.5
9	2	Write equations to find unknown dimension	Area of Rectangles and Squares	4.MD.A.3
10	2	Identify finding area situations	Calculate Perimeter and Area	4.MD.A.3

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.



Unit Opener

Focus Question

Introduce the Focus Question, *How can I find the volume of rectangular prisms?*

Ask students to think about what they know about volume of rectangular prisms.

- Do you know what it means to find the volume of rectangular prisms?
- What do you already know about finding volume of rectangular prisms?
- What do you think you will be doing in the unit?

Remind students that at the end of the unit, they will reflect back on what they learned in this unit.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

STEM in Action

Videos

Students can watch the two STEM videos.

Ocean Engineer Hiro talks about the work of an ocean engineer.

Hiro Finds the Volume of a Waterproof Case Hiro explains how to find the volume of his camera.

STEM Project

Students can complete the STEM project during their workstation time.



Ocean Engineer



Hiro Finds the Volume of a Waterproof Case



Ignite!

Name: _____

Painted Cubes

Use connecting cubes to build each figure.



Figure 1



Figure 2

Figure 2 is made up of small cubes. Suppose Figure 2 is dipped into a bucket of red paint. How many small cubes would have:

all 6 faces painted red?	0
exactly 5 faces painted red?	0
exactly 4 faces painted red?	0
exactly 3 faces painted red?	24
exactly 2 faces painted red?	48
exactly 1 face painted red?	60
no faces painted red?	1

Find the sum of the numbers of cubes you listed above. 27

Did you account for all of the small cubes in Figure 2? Yes

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Ignite!

Painted Cubes

Students use connecting cubes to build a larger cube. They relate what they build to faces and volume.

Material: 30 connecting cubes for each group

- Direct students to Figure 1.
 - What are the dimensions of the large cube?
- Have students work in pairs to build a $2 \times 2 \times 2$ cube using connecting cubes.
 - How many connecting cubes are needed to make a $2 \times 2 \times 2$ cube?
 - How could you determine the number of connecting cubes needed without counting them one-by-one?
- Have students imagine dipping the entire $2 \times 2 \times 2$ cube into a bucket of red paint. The entire outer surface of the cube would now be red.
 - For each cube, how many of its faces would be red? How many would not be red?
- Direct students to Figure 2.
 - How could you determine the total number of small cubes in Figure 2 without counting them one-by-one?
 - Based on your findings for Figures 1 and 2, how could you determine the total number of small cubes needed to make $4 \times 4 \times 4$ cube?
- Have students use connecting cubes to build a $3 \times 3 \times 3$ cube.
 - Are there any connecting cubes in the cube you built that cannot be seen at all? Explain.
- Have students answer the questions on the student page for Figure 2 for dipping a $3 \times 3 \times 3$ cube into a bucket of red paint.
 - How many connecting cubes would have ... all 6 faces painted red? Where are they? exactly 5 faces painted red? Where are they? exactly 4 faces painted red? Where are they? exactly 3 faces painted red? Where are they?

Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson	
Game Station		Students build proficiency with finding the volume of rectangular prisms.		
		• Volume Sort	2-1	
		• Volume Sort	2-2	
		• Volume Showdown	2-3	
		• Additive Volume Task Cards	2-4	
• Volume Situation Concentration	2-5			
Digital Game		Dino Dig Students practice multiplying to find area. 2-1		
		Have students complete at least one of the Use It! activities for this unit.		
Application Station		STEM Project Card Developing and Using Models Students create a scale model of a kitchen cabinet.	2-5	
			Connection Card Harvesting Water Students plan and build a model of a rainwater harvesting reservoir.	2-4
			Real World Card You Are a Computer Programmer Students design 2-3 a computer program to find the volume of a rectangular prism.	

Additional Resources

Use the resources below to provide additional support for this unit.



Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the key terms on the front side of the card.



Foldables

Use the unit foldables with Lessons 2-3 and 2-4.



Spiral Review

Students can complete the Spiral Review at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
2-1	4.OA.A
2-2	4.NBT.A
2-3	4.NBT.B
2-4	4.NF.A
2-5	4.NF.B

Understand Volume

Learning Targets

- I can describe volume as an attribute of solid figures.
- I can describe how rectangular prisms can be packed using unit cubes with no gaps or overlaps.

Standards

Major Supporting Additional

Content

- **5.MD.C** Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition.
- **5.MD.C.3** Recognize volume as an attribute of solid figures and understand concepts of volume measurement.
- **5.MD.C.3.a** A cube with side length 1 unit, called a “unit cube,” is said to have “one cubic unit” of volume, and can be used to measure volume.

Mathematical Practices and Processes

MPP Attend to precision.

MPP Look for and make use of structure.

Vocabulary

Math Terms

rectangular prism

unit cube

volume

Academic Terms

analyze

establish

Materials

The materials may be for any part of the lesson.

- centimeter cubes
- marbles, beans, or other measurement units
- *Nets* Teaching Resource

Focus

Content Objective

- Students understand volume is a measurable attribute of 3-dimensional figures.
- Students understand that a rectangular prism can be packed using unit cubes with no gaps or overlaps to establish volume.

Language Objectives

- Students talk about ways to measure volume using the verb *find*.
- In order to support sense-making and maximizing linguistic, ELS will participate in MLR2: Collect and Display.

SEL Objective

- Students use prior knowledge and new understanding of mathematical concepts to complete a task, building stronger self-efficacy.

Coherence

Previous

- Students described area as an attribute of plane figures and explained concepts of area measurement (Grade 3).

Now

- Students describe volume as an attribute of solid figures and understand concepts of volume measurement.

Next

- Students measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units (Unit 2).
- Students find the volume of a right rectangular prism with fractional edge lengths (Grade 6).

Rigor

Conceptual Understanding

- Students develop understanding of volume as the amount of space taken up by a solid object.

Procedural Skill & Fluency

- Students develop proficiency with determining volume.
- Procedural skill and fluency is not a targeted element of rigor for this standard.*

Application

- Students apply their understanding of volume in different situations.
- Application is not a targeted element of rigor for this standard.*

Number Routine

Would You Rather?

Build Fluency Students build skills with multiplication and finding area as they compare measurements.

These prompts encourage students to talk about their reasoning:

- What strategies did you use in finding your answer?
- What do you know about the sizes of the yards?

Purpose Students notice similarities and differences among 2-dimensional and 3-dimensional objects.

Notice & Wonder™

- How are they the same?
- How are they different?

Teaching Tip You may wish to have students use physical objects in the classroom, such as a tissue box, pencil box, and construction paper, to compare and contrast attributes of 2-dimensional and 3-dimensional objects.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' recognition of volume as a measurable attribute of solid figures and are based on possible comments students may make during the share out.

- How can you establish if a figure has length, width, and height?
- How can you measure a 2-dimensional figure?
- How can you measure a 3-dimensional figure?

Math is... Mindset

- What do you already know that can help you with today's work?

Self-Awareness: Self-Efficacy

As students work through the Notice & Wonder™ routine, provide specific, constructive feedback that can help guide each student toward task-completion. This sense of completion can enhance feelings of self-efficacy in mathematics as well as provide models for peers. As students work with understanding volume throughout the lesson, encourage them to connect and use their prior knowledge of area. Encouraging use of prior knowledge can help students feel more competent and promote stronger self-efficacy.

Transition to Explore & Develop

Establish Goals to Focus Learning

Help focus students' attention on the attributes of the shelves and the pictures, specifically, their measurable attributes,

- Let's analyze the measurable attributes of 2-dimensional and 3-dimensional figures.



Learn
How are these figures the same?
How are they different?



The figure has two dimensions.



Each dimension is a measurable edge length.

The figure has three dimensions.



Each dimension is a measurable edge length.

The space occupied by a 3-dimensional figure is called **volume**.

You can pack 3-dimensional figures using **unit cubes** with no gaps or overlaps to establish volume.



A unit cube has edge lengths of 1 unit.

Work Together
How do you think the marbles in the rectangular prism below compare?
What do you think about these cubes?
Sample answer: The marbles do not completely fill the rectangular prism because there are gaps. The unit cubes fill the rectangular prism with no gaps.




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1 Pose the Problem

1.1 Collect and Display

As students discuss the questions, make a list of key words you hear, such as *alike*, *different*, *width*, *length*, *dimensional*, *volume*, and *area*. Display the list and use it to help students connect words they already know and math vocabulary.

1.2 Pose Purposeful Questions

- What do you think are the mathematically important attributes of the figures?
- How can you use a tool to organize your answers?
- What words can you use to help you organize your answers?
- How can you use mathematical categories to solve this problem?

2 Develop the Math

Choose the option that best meets your instructional goal.



3 Bring It Together

3.1 Elicit Evidence of Student Thinking

- How is volume similar to area? How is it different?
- Could you pack a rectangular prism with a length of $3\frac{1}{2}$ units using unit cubes with no gaps or overlaps? Explain why or why not.
- Can you think of figures other than rectangular prisms that could be packed using unit cubes without gaps or overlaps? Explain why they could be packed that way.

Key Takeaways

- Volume is an attribute of 3-dimensional figures.
- Volume is the space occupied by a 3-dimensional figure.
- Rectangular prisms can be packed using unit cubes with no gaps or overlaps to establish volume.

Work Together

Students explore which figures can pack a rectangular prism without gaps. Students can work on the problem in pairs before sharing their work.

Common Misconception: Make sure students understand that the marbles do not fill the rectangular prism completely. When packing a 3-dimensional figure to determine volume, there must be no gaps.

3.2 Language of Math

Make sure students see the *cube* connections in volume. Packing with unit cubes is used to determine volume in *cubic* units.

Activity-Based Exploration

Students explore the concept of volume by filling a paper rectangular prism with different units, such as unit cubes, marbles, and beans.

Materials: *Nets Teaching Resource*, unit cubes, marbles, beans, or other measurement units

Directions: Provide each pair or small group a copy of *Nets Teaching Resource* and various measurement units. Demonstrate how to form rectangular prisms using the nets. Have students determine how many of each unit can fit inside the rectangular prism.

Support Productive Struggle

- How would you explain what you are trying to determine?
- Explain why there are different numbers for each unit used to fill the rectangular prism.
- What is different about the way the beans/marbles fill the rectangular prism when compared to the way the unit cubes fill the rectangular prism?

Math is... Precision

- Does an empty box have volume? Does a filled box have volume? Explain why or why not.

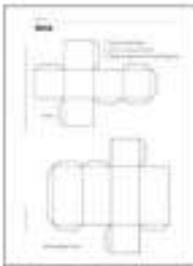
Students try to use clear definitions in discussion with others and in their own reasoning.

Activity Debrief: After students have completed the activity, facilitate a discussion to ensure students understand the terms *volume*, *unit cubes*, and *rectangular prism*.

Have students revisit the Pose the Problem question and discuss answers.

- How are these figures alike? How are they different?

A PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students develop an understanding that 3-dimensional figures also have a measurable attribute called *volume*, and that volume can be measured by packing *rectangular prisms* with *unit cubes*.

Pose Purposeful Questions

- **Think About It:** Why is the width a length?
- **Think About It:** Why is the height a length?

Have students build rectangular prisms and other figures using unit cubes with no gaps or overlaps to gain a deeper understanding of the idea of packing with unit cubes with no gaps or overlaps.

- What solid could be filled without gaps or overlaps using cylinders? Explain why.

Math is... Precision

- Does an empty box have volume? Does a filled box have volume? Explain why or why not.

Students use clear definitions in discussion with others and in their own reasoning.



English Learner Scaffolds

Entering/Emerging Support students in understanding the terms *fill* and *pack*. Fill a small box with similar objects, such as counting chips. Say, *I'm filling the box*. Shake the box so it's clear that the objects don't encompass the entire volume of the box. Next, using cubes or any like object, completely pack the box, saying, *I'm packing the box*. Shake the box so it's clear that the objects completely pack the entire box (there should be no movement). Repeat with new objects, both filling and completely packing the box. Ask *Did I pack this box?*

Developing/Expanding Support students in understanding the terms *fill* and *pack*. Fill a small box with similar objects, such as counting chips. Say *I'm filling the box*. Shake the box so it's clear that the objects don't encompass the entire volume of the box. Next, using cubes or any like object, completely pack the box, saying, *I'm packing the box*. Shake the box so it's clear that the objects completely pack the entire box (there should be no movement). Ask students to repeat the task with similar objects to demonstrate *fill* and *pack*, stating which they are doing each time. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to explain what it means to both *fill* and *pack* something. As students provide their explanations, listen for key words such as *gaps*, *overlaps*, and *volume*, and prompt students to explain how they know if an object is packed or not.

On My Own

Name _____

1. Which 3-dimensional figures have volume? Justify your reasoning.



Sample answer:
Only 3-dimensional figures have volume.

For the situation, would you measure the length, area, or volume? Explain.

1. The amount of soil needed to fill a flower pot.
Sample answer: You are filling a 3-dimensional figure.
length. **Sample answer:** Distance is length.

2. The amount of concrete needed to fill a hole.
Sample answer: You are covering a 3-dimensional figure.
volume. **Sample answer:** The concrete is filling a 3-dimensional figure.

3. The space inside a moving truck.
Sample answer: You are packing a 3-dimensional figure.
length. **Sample answer:** Perimeter is length.

4. The distance around a building.
Sample answer: Perimeter is length.

5. The amount of concrete needed to fill a hole.
Sample answer: The concrete is filling a 3-dimensional figure.
volume. **Sample answer:** The concrete is filling a 3-dimensional figure.

6. The space inside a moving truck.
Sample answer: You are packing a 3-dimensional figure.
length. **Sample answer:** Perimeter is length.

7. The distance around a building.
Sample answer: Perimeter is length.

8. The amount of concrete needed to fill a hole.
Sample answer: The concrete is filling a 3-dimensional figure.
volume. **Sample answer:** The concrete is filling a 3-dimensional figure.

9. The space inside a moving truck.
Sample answer: You are packing a 3-dimensional figure.
length. **Sample answer:** Perimeter is length.

10. The distance around a building.
Sample answer: Perimeter is length.

Level 1 • Item 28

2. **180°** **Connected:** An artist requires needs to lay the walls of an aquarium. She is told by her father to fill the walls of the tank with concrete. Why do you think he is frustrated with concrete? Does he require something else instead? Justify why.



Sample answer: Walls are 2-dimensional and have area. The tank is 3-dimensional and has volume.

3. Both rectangular prisms in this wall will cover the same area. Why are they not the same? Justify your reasoning.



Sample answer: The one on the right is filled completely by the unit cubes. There are no gaps or overlaps.

4. **Extend Your Thinking:** Can you pack a cylinder with unit cubes without gaps or overlaps? Justify your thinking.

Sample answer: No. The unit cubes will leave gaps between them and the curved surface of the cylinder.

Reflect

How can you verify volume of rectangular prisms and a cylinder?
Answers may vary.

Math is... Mindset

How did you do on this assignment? Do you have any questions?

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Practice

Build Fluency from Understanding

Common Error: Exercise 5 Students may assume that a concrete patio consists just of its surface. Point out that a concrete patio has depth in addition to length and width.

Practice Item Analysis

Item	DOK	Rigor
1	2	Conceptual Understanding
2–7	2	Conceptual Understanding
8	3	Conceptual Understanding
9	4	Conceptual Understanding
10	4	Conceptual Understanding

Reflect

Students complete the Reflect Question.

- How can I explain volume of rectangular prisms to a friend?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What do you already know that can help you with today's work?

Students reflect on how they practiced self-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can describe volume as an attribute of solid figures.
- I can describe how rectangular prisms can be packed using unit cubes with no gaps or overlaps.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Understand volume	5.MD.C.3.a
2	1	Understand volume	5.MD.C.3.a
3	2	Understand volume	5.MD.C.3.a

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

- 3 of 3 Additional Practice or any of the ✔ or ✔ activities
- 2 of 3 *Take Another Look* or any of the ✔ activities
- 1 or fewer of 3 Small Group Intervention or any of the ✔ activities

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 2-1
Exit Ticket

Name: _____

- The volume of a figure can be found if the figure has two (only one) dimension?
 - A. 1
 - B. 2
 - C. 3
 - D. 4
- Which of these figures has volume? (Choose all that apply.)
 - A.
 - B.
 - C.
 - D.
- Which of these situations is which volume is measured? (Choose all that apply.)
 - A. the amount of water in a swimming pool
 - B. the amount of wall space covered by a poster
 - C. the distance walked from home to the library
 - D. the amount of area in a car

Reflect On Your Learning

1 2 3 4

Not confident Fully confident

How confident are you about your learning?

○ ○ ○ ○

Assessment Resource Book 18

R Reinforce Understanding

SMALL GROUP

Little Boxes

Work with pairs of students. Give each pair 30 unit cubes and small empty containers with various shapes. Have each pair try to fill the container with unit cubes in order to find the volume. Remind students that to be considered filled, the container must have no gaps or overlaps. Then discuss with the students which shapes could be filled with cubes and which could not.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Volume Sort
Students explore volume.

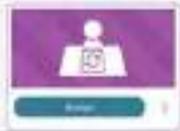


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Understand Volume



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 1

Lesson 3-1 - Reinforce Understanding
Understand Volume

Name: _____

Review
Use unit cubes to measure the space inside a three-dimensional figure.

The space inside a three-dimensional figure is called **volume**. You can fill a figure with unit cubes by measuring the volume.

1. Circle the figures that would be measured using unit cubes.

Put an X next to the shapes that would be measured using unit cubes.

1. Kary is measuring the distance she drove to school.

2. Kary is measuring what size 8 is her sneakers.

3. Mal is measuring how much water a pond can hold.

4. Mal is measuring the space a window will take in the wall.

5. Sam is measuring how high the floor is up stairs.

6. Sam is measuring how much soil Steve's storage unit can hold.

7. Describe how to find the volume of a solid using **unit cubes**.

Sample answer: Measure the volume by packing the object with unit cubes until no gaps or overlaps remain between the

INDEPENDENT WORK

Student Practice Book, pp. 1–2

Lesson 3-1
Additional Practice

Name: _____

Review
Volume is the space inside a three-dimensional figure. You can fill the inside of the figure with unit cubes to determine its volume.

1 unit cube

1 unit cube

The volume of this rectangular prism is 8 unit cubes.

1. Which of these figures do you think will be measured by _____?

Sample answer: The rectangular prism and the sphere are the only two figures that are three-dimensional.

2. Tell what type of unit you would use to measure each of the following. Circle the length units, square units, or cube units.

a. A piece of string **length units**

b. The amount of space inside a rectangular box **cubic units**

c. The amount of floor space a carpet covers **square units**

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Own It! Digital Station**Build Fluency Games**

Assign the digital game to develop fluency with multiplying to find area.

**Use It! Application Station****You Are a Computer Programmer**

Students design a computer program to find the volume of a rectangular prism. *The content of this card has concepts covered later in Lesson 2-3.* You may want to assign this card to students ready to explore content covered later in this unit.

**Spiral Review**

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.

**Websketch Exploration**

Assign a websketch exploration to apply skills and extend thinking.

**Student Practice Book, pp. 1–2**

For each situation, tell whether you would measure using length units, square units, or cubic units. Explain your reasoning.

- Tommy is measuring the amount of wall space in his room so that he knows how much paint to buy.
square units; Sample answer: Area is measured in square units.
- Yolana wants to know how much water is inside her fish tank.
cubic units; Sample answer: Volume is measured in cubic units.
- Paul wants to know how far his school is from home.
length units; Sample answer: Distance is measured in length units.

Use your understanding of area and volume to answer each question.

- Henry wants to know how much air is inside his balloon. He thinks that air should occupy the area of the balloon. Henry suggests that she should find the volume of the balloon. What is correct? Explain.
Henry; Sample answer: The space inside the balloon is a measure of volume.

Math in Motion Activity

Use the Student Practice Book to help you understand the concepts of area and volume. Use the Student Practice Book to help you understand the concepts of area and volume.

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Differentiation Resource Book, p. 2

Lesson 2-4 • Extend Thinking

Understand Volume

Name _____

A pencil company advertises its new ball that is shaped like a bowl.

- Do these balls have equal volume?
No; Sample explanation: Since it isn't a ball, it has volume.
- Can you use a ball to find the volume of these bowls?
No; Sample answer: There will be gaps after filling it.
- Do you see a pencil bag with the new pencil. Can you use the new pencil to find the volume of the pencil bag?
No; Sample answer: They cannot be used to measure volume. There will be gaps after the bag is filled.
- The company wants to be able to use their pencil to find the volume of the pencil bag. What shape of pencil should they recommend?
Sample answer: A unit cube that will fill the bag with no gaps or overlaps will tell the volume.

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Use Unit Cubes to Determine Volume

Learning Targets

- I can determine volume by counting unit cubes that fill a solid with no gaps or overlaps.
- I can determine volume by multiplying the number of unit cubes in one layer by the number of layers that fill a solid with no gaps or overlaps.

Standards Major Supporting Additional

Content

- 5.MD.C.3.a** A cube with side length 1 unit, called a “unit cube,” is said to have “one cubic unit” of volume, and can be used to measure volume.
- 5.MD.C.3.b** A solid figure which can be packed without gaps or overlaps using n unit cubes is said to have a volume of n cubic units.
- 5.MD.C.4** Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units.

Math Practices and Processes

MPP Look for and make use of structure.

Focus

Content Objective

- Students determine the volume of a rectangular prism by counting unit cubes.
- Students determine the volume of a rectangular prism by multiplying the number of unit cubes in one layer by the number of layers.

Language Objectives

- Students discuss how to determine the volume of any 3-dimensional solid by counting unit cubes while answering *Wh-* questions.
- In order to support optimizing output, ELs will participate in MLR3: Critique, Correct, and Clarify.

SEL Objective

- Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing thoughtful and constructive feedback.

Coherence

Previous

- Students described volume as an attribute of solid figures and understood concepts of volume measurement (Unit 2).

Now

- Students measure volume by packing prisms with unit cubes then counting, using cubic cm, cubic in, cubic ft, and improvised units.

Next

- Students use two formulas to determine the volume of a right rectangular prism with whole-number side lengths (Unit 2).

Rigor

Conceptual Understanding

- Students understand that the volume of a right rectangular prism can be determined by counting the number of unit cubes that fill it completely with no gaps or overlaps.

Procedural Skill & Fluency

- Students build proficiency in determining volume using multiplication.

Application

- Students start to recognize the relationship between the dimensions of a rectangular prism and how many unit cubes it takes to pack it

Application is not a targeted element of rigor for this standard.

Vocabulary

Math Terms

cubic unit
unit cube
volume

Academic Terms

debate
suggest

Materials

The materials may be for any part of the lesson.

- centimeter cubes
- Nets* Teaching Resource

Number Routine
Would You Rather?

5–7 min

Build Fluency Students build skills with multiplication and area as they compare measurements.

These prompts encourage students to talk about their reasoning:

- What information about the rugs did you use to find your answer?
- How could you use estimation to compare the areas of the rugs?

Purpose Students explore objects that fill a solid container. They consider what objects may fill the given space with no gaps or overlaps.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip It may help students visualize the scenario by distributing containers shaped like rectangular prisms or plastic cups, and have them fill the cups with objects like counting cubes.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' thinking about packing a solid to determine volume and are based on possible comments and questions students may make during the share out.

- What ways could you suggest to count the boxes in the truck?
- Do the boxes pack the truck with no gaps or overlaps? Explain why or why not.

Math is... **Mindset**

- How can different ideas and viewpoints help you learn better?

Social Awareness: Appreciate Diversity

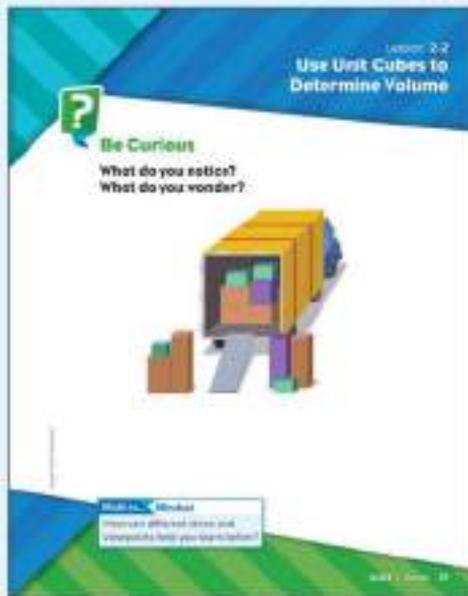
As students consider the Notice & Wonder routine, invite them to collaborate with peers and discuss different tools/strategies/representations/methods that they might use to determine the volume of the box. As students share their unique thought processes and ideas, emphasize the value of the differences as well as the similarities so students can understand the importance of diversity within a math context. Encourage students to listen to and build off the ideas of their peers.

Transition to Explore & Develop

Establish Goals to Focus Learning

Ask questions that focus students' attention on the packing and counting objects to find volume and efficient ways to do that counting.

- Let's think about how to count unit cubes to find volume and efficient ways to do that counting.



Lesson 2-2
Use Unit Cubes to Determine Volume

Be Curious
What do you notice?
What do you wonder?

Math is... Mindset
Different colored boxes and containers help you learn better.



Be Curious
What do you notice?
What do you wonder?

GO ON

Layers
How can you determine the volume of this box?

You can pack the box with unit cubes to determine the volume. 8 unit cubes is twice as many as one **unit cube**.



When you count the number of unit cubes in the box, you have to count every unit cube.

There are 8 layers of unit cubes in the box. It is 4 unit cubes high, 2 unit cubes wide, and 2 unit cubes deep.

Math 2.1.1 **Strategies**
Why don't you use **area** or **multiplication** to determine the number of unit cubes?

Counting to determine the volume of a 3-dimensional figure is not practical without cubes and counting cubes.

Do Work Together
How can you determine the volume of this box?
Sample answer: There are 4 × 3, or 12, unit cubes in each layer. There are 5 layers, and 12 × 5 = 60.



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1 Pose the Problem

1.1 Pose Purposeful Questions

- How does the picture help you understand this problem?
- Using what you know about volume, can you make a conjecture about how to find the volume of the box?
- How will the units and labels you will use correspond to the quantities in this problem?

2 Develop the Math

2.1 Choose the option that best meets your instructional goal.

2.1.1 Critique, Correct, and Clarify

Make a false claim for students to critique. Draw a cube with 3×2 unit cubes and 4 layers. Solve, but add instead of multiply the layers. Say *The volume of the box is 10. Yes or No?* Have the class discuss how to correct your mistake. Revisit this activity throughout the lesson.

3 Bring it Together

3.1 Elicit Evidence of Student Thinking

- How is a cubic unit like a square inch? How is it different?
- When can you count unit cubes to determine the volume of a solid figure?
- What strategies can you use to find quickly the number of unit cubes that pack a rectangular prism?

Key Takeaways

- A unit cube has a volume of 1 cubic unit.
- Volume of rectangular prisms can be determined by counting the number of unit cubes that fill the rectangular prism with no gaps or overlaps.
- Volume of rectangular prisms can be found by multiplying the number of unit cubes in one layer by the number of layers that fill the prism.

Work Together

Students determine the total number of unit cubes that fill a rectangular prism when given the number of cubes in the length, width, and height.

Common Misconception: Students may count just the number of cubes shown. Remind them that they are determining the volume of the box, so they need to imagine that the box is filled with the cubes.

Language of Math

Some students may have noticed that packing unit cubes in layers like this would leave gaps if any of the dimensions of the box contained a fraction. For our purposes, *rectangular prism* means *rectangular prism with whole number dimensions*.

Activity-Based Exploration

Students explore volume of rectangular prisms by multiplying the number of unit cubes in each layer by the number of layers.

Materials: centimeter cubes, *Nets Teaching Resource*

Directions: Demonstrate creating a rectangular prism from nets. Have students pack the rectangular prism using centimeter cubes to determine its volume.

Implement Tasks that Promote Reasoning and Problem Solving

- How might you pack a box with unit cubes? Where would you start?

After students have completed the activity, ask

- What do you notice about how the cubes are arranged in the box?
- How can you describe the relationship between the number of layers, the number of cubes in each layer, and the volume of the box?

Math is... Structure

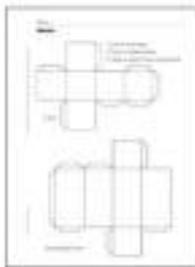
- What concepts have you learned before that were useful when determining the volume?

Students relate the concepts of multiplication as equal groups (or arrays) to the calculations used to determine volume.

Activity Debrief: Have students share their strategies for counting the number of centimeter cubes needed to fill the rectangular prism. Encourage students to use precise language, such as a multiplication.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine the volume of this box?



A PDF of the Teaching Resource is available in the Digital Teacher Center.

English Learner Scaffolds

Entering/Emerging Support students in understanding the terms *gaps*. Add some objects to a box, being sure not to fill it. Point to the spaces inside the box. Say *There are gaps*. Repeat the task again, asking, *Are there gaps?*

Developing/Expanding Support students in understanding the terms *gaps*. Add some objects to a box, being sure not to fill it. Point to the spaces inside the box. Say *There are gaps*. Ask students to repeat the task with similar objects provided to them. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to discuss how gaps affect the volume of an object. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, I disagree because gaps...*

Guided Exploration

Students explore ways to determine the volume of rectangular prisms.

Facilitate Meaningful Discourse

- **Think About It:** What do you notice about the way the unit cubes are packed?
- If the unit cubes did not fill the box completely, could you determine the volume? Explain why or why not.

Have students propose strategies they have for counting the number of unit cubes that pack the box. Encourage them to debate the advantages of their strategies.

- Can you to make a layer a different way? How could you use it to find the volume of the box?

Math is... Structure

- Why can you use addition or multiplication to determine the number of unit cubes?

Students are understanding the properties in mathematics that connect repeated addition and multiplication.



On My Own

Name _____

Determine the volume of the figure.

1.  Number of layers: 2
Number in each layer: 4
Volume: 8 cubic units

2.  Number of layers: 2
Number in each layer: 6
Volume: 12 cubic units

3.  Number of layers: 2
Number in each layer: 6
Volume: 12 cubic units

4.  Number of layers: 2
Number in each layer: 9
Volume: 18 cubic units

5. How can you determine the volume of the box?

Sample answer: There are 4 x 6 unit cubes in a layer and 2 layers: $4 \times 6 \times 2 = 48$.

What is the volume of the figure?

6.  12 cubic units

7.  18 cubic units

Math 1. Volume 28

8. What equation could you write to determine the volume of this figure?

Sample answer: $4 + 4 + 4 = 12$; $12 \times 4 = 48$

9. The volume of this box is 36 cubic units. How many layers of unit cubes are in the box? Explain your thinking.

Sample answer: There are 6 unit cubes in each layer; there are 6 unit cubes for 6 layers; $36 \div 6 = 6$.

10. **Enter a classmate's** Carlos and Kaitlin are finding the volume of this figure. Carlos says there are 5 layers and 8 unit cubes in each layer. Kaitlin says there are 4 layers and 10 unit cubes in each layer. Who is correct? Explain.

Both are correct. Sample explanation: Carlos and Kaitlin are looking at the prism different ways: Carlos is describing layers from left to right; Kaitlin is describing layers from front to back.

Reflect

Why does understanding multiplication as an array connect to determining the volume of a 3-dimensional figure?

Answers may vary.

Math 1.1.10

Use unit cubes to find the volume of a 3-dimensional figure and explain how you found the volume.

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Practice

Build Fluency from Understanding

Common Misconception: Exercise 10 A layer does not have to be horizontal or the *bottom*. A layer can be vertical. Students should choose the orientation of the layer based on what is easiest for them to use. If it is easier to find the number of cubes in a vertical layer, then they should use that.

Practice Item Analysis

Item	DOK	Rigor
1–4	1	Procedural Skill & Fluency
5–7	2	Procedural Skill & Fluency
8–10	3	Conceptual Understanding

Reflect

Students complete the Reflect Question.

- How does understanding multiplication as an array connect to determining the volume of a 3-dimensional figure?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How can different ideas and viewpoints help you learn better?
- Students reflect on how they practiced social-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can determine volume by counting unit cubes that fill a solid with no gaps or overlaps.
- I can determine volume by multiplying the number of unit cubes in one layer by the number of layers that fill a solid with no gaps or overlaps.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



R Reinforce Understanding

SMALL GROUP

Finding Volume

Work with students in groups of three. Give each student 30 unit cubes. Have each student create a rectangular solid using some or all of the cubes then find the volume of the figure. Have students switch figures with another student and find the volume of the figure. Then have students switch again so that each student finds the volume of all three figures. If necessary, remind students that they can count the number of cubes used to find the volume.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Volume Using Unit Cubes
- Volume Using Multiplication



INDEPENDENT WORK

Differentiation Resource Book, p. 3

Lesson 3.2 - Reinforce Understanding
Use Unit Cubes to Determine Volume

Name: _____

Review
 Pack the rectangular prism with unit cubes to determine the volume.

Count the cubes that fill the bottom layer. There are 12 cubes. Multiply by the number of layers. There are 4 layers. $12 \times 4 = 48$. The volume is 48 cubic units.

Match the figure to its volume:

a. 48 cubic units b. 36 cubic units c. 24 cubic units

3. Determine the number of layers in a prism that is 12 cubes in each layer and the volume is 36 cubic units. Explain.

Sample answer: Divide the volume by the number of cubes in each layer. $36 \div 12 = 3$. There are 3 layers.

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Volume Sort
 Students explore volume.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 3–4

Lesson 3.2
Additional Practice

Name: _____

Review
 You can find the volume of a rectangular prism by packing it with cubes.
 The rectangular prism contains 24 unit cubes.
 The volume of the prism is 24 cubic units.

Find the volume of each cube.

1. 8 cubic units 2. 27 cubic units

Find the volume of each rectangular prism.

3. 24 cubic units 4. 36 cubic units

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplying to find area.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 3–4

Determine the volume of each prism.

1. 32 cubic units 2. 40 cubic units

3. Mimi is packing DVD's into a shipping box. Explain how many DVD's will fit in this shipping box.

32 DVD's. Sample answer: I counted that 4 DVD's fit on one layer, and then I multiplied that by 8 since there are 8 layers.

4. A rectangular prism with a volume of 48 cubic feet is shown. What is the volume of the prism?

48 cubic units. Sample answer: I counted a total of 48 unit cubes.

5. Jose wants a fish tank with a volume of at least 36 cubic feet for his pet fish. The tank shown is an example. Is this tank large enough? Explain.

Yes. The volume of the tank is 36 cubic feet, which is larger than 30 cubic feet.

Math 2 Home Activity

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E

Extend Thinking

Use It! Application Station

Harvesting Water Students plan and build a model of a rainwater harvesting reservoir. *The content of this card has concepts covered later in Lesson 2-4. You may want to assign this card to students ready to explore content covered later in this unit.*



WORKSTATIONS

Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 4

Lesson 2-2 - Extend Thinking

Use Unit Cubes to Determine Volume

Name: _____

This lesson book is used to design lesson with specific volumes.

1. Use A box, a volume of 36 unit cubes. Identify each variable (number of layers and the number of cubes in each layer).

Number of layers	1	2	3	4	6	9	12	18	36
Number of cubes in each layer	36	18	12	9	6	4	3	2	1

2. Use B box, a volume of 36 unit cubes. Identify each variable (number of layers and the number of cubes in each layer).

Number of layers	1	2	3	4	6	9	12	18	36
Number of cubes in each layer	36	18	12	9	6	4	3	2	1

3. What strategy do you use to find all of the different boxes?

Sample answer: I found all of the ways to multiply to get the volume.

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INDEPENDENT WORK

Use Formulas to Determine Volume

Learning Targets

- I can find the volume of rectangular prisms using formulas.
- I can explain how to find the volume of rectangular prisms using formulas.

Standards

Major Supporting Additional

Content

- **5.MD.C.5.a** Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication.
- **5.MD.C.5.b** Apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real-world and mathematical problems.

Mathematical Practices and Processes

MPP Model with mathematics.

Vocabulary

Math Terms Academic Terms

base (of a solid) assert

formula

evaluate

Materials

The materials may be for any part of the lesson.

- cubes

Focus

Content Objective

- Students determine the volume of rectangular prisms using formulas.

Language Objectives

- Students explain how to determine the volume of rectangular prisms using formulas while answering *Wh-* and *Yes/No* questions and using the term *dimensions*.
- In order to support cognitive meta-awareness and optimize output, ELs will participate in MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students practice strategies for persisting at a mathematical task, such as setting a small goal or setting timers for remaining focused.

Coherence

Previous

- Students measured volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units (Unit 2).

Now

- Students use formulas to determine the volume of a right rectangular prism with whole-number side lengths.

Next

- Students determine the volume of composite solid figures (Unit 2).

Rigor

Conceptual Understanding

- Students use their understanding of volume to develop the formula used to calculate the volume of rectangular prisms.

Procedural Skill & Fluency

- Students build proficiency in calculating the volume of rectangular prisms.

Application

- Students apply the formulas for volume of a rectangular prism to solve real-world problems.

Number Routine

Can You Make the Number?



Build Fluency

Students build number sense as they use combinations of numbers and mathematical operations to make the target number.

Remind students there is more than one solution to the problem. If they find one way, challenge them to continue to find other ways.

These prompts encourage students to talk about their reasoning:

- How many different equations did you write to make the target number?
- How many different mathematical symbols did you use?

Purpose Students notice that layers are one way of arranging objects, such as pizza boxes.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may wish to have students Turn and Talk before sharing out their ideas with the whole class.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' ability to generalize the strategies they used in the previous lesson and are based on possible comments students may make during the share out.

- Are the boxes rectangular prisms? How could you find the volume of one of the boxes?
- What information would you need to determine the total volume of the stack of boxes?

Math is... **Mindset**

- What can you do to stay focused on your work?

Self-Management: Control Impulses

Provide opportunities for students to practice self-regulation. Have students discuss strategies to help maintain focus for the Notice & Wonder routine. As you transition from the Notice & Wonder routine, brainstorm strategies that can help students express emotionally and behaviorally appropriate responses in times of frustration or disappointment. As students work with using formulas to determine volume, invite them to practice deep-breathing techniques or take movement breaks when necessary.

Transition to Explore & Develop

Establish Goals to Focus Learning

Ask questions that focus students' attention on the techniques they have used for counting, and how they might be used to create a formula for finding the volume of a rectangular prism.

- Let's think about how we can determine and use a formula and use it to find the volume of a rectangular prism.



Learn
What are some ways to determine the volume of this rectangular prism?



One Way: Multiply to find the number of cubes in one layer. Then multiply by the number of layers.



Volume = Base \times height
 $V = 15 \times 2$
 $V = 30$ cubic units

Another Way: Multiply the three attributes.



Volume = length \times width \times height
 $V = 3 \times 5 \times 2$
 $V = 30$ cubic units

Math is... Modeling
What are the formulas related?

Work together
What do you notice about the volume of the rectangular prisms? Explain why this occurs.



They all have the same volume. Simple explanation: They all have the same dimensions: $10 \times 5 \times 2 = 100$

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1 Pose the Problem

Pose Purposeful Questions

- What problems like this have you done this before?
- What patterns did you see in the way you solved those problems?
- What words will you use to explain your thinking?
- How will the units and labels you will use correspond to the quantities in this problem?

2 Develop the Math

Choose the option that best meets your instructional goal.

Stronger and Clearer Each Time

Pair students and have them determine the volume of a figure. Have them individually write sentences explaining the steps they took to get the volume. Then have them share their writing with their partner and revise if necessary. Revisit throughout the lesson for reinforcement.

3 Bring it Together

Elicit Evidence of Student Thinking

- Explain how the $V = B \times h$ formula represents the volume of a rectangular prism.
- Explain how the $V = l \times w \times h$ formula determines the volume of a rectangular prism.

Math is... Modeling

- How are the two formulas related?

Students are looking at the structure in mathematics that relates the length times the width and the number of cubes in the base layer.

Key Takeaway

- Two formulas can be used to determine the volume of rectangular prisms: $V = l \times w \times h$ and $V = B \times h$.

Work Together

Students think about how using different bases for the same prism yields the same volume, and how that represents the Associate Property. Have students work on the problem in pairs before asking them to share their work.

Common Misconception: Students may feel they need to calculate the volume of each rectangular prism to compare their volumes. Suggest to them that the volumes can be compared without determining the volumes of any of the prisms.

Language of Math

Base is a difficult term to define. Fortunately, for rectangular prisms, any face can serve as a base. This is not the case for prisms in general.

Activity-Based Exploration

Students derive the volume formulas by exploring patterns in the dimensions of rectangular prisms with the same volume.

Materials: 24 cubes per pair or small group

Directions: Have students explore different rectangular prisms that have a volume of 24 cubic units.

- What is the shortest rectangular prism you can create with a volume of 24 cubic units? Tallest?
- It is possible to create a height of each number between 1 and 24? If not, which heights are possible?



Support Productive Struggle

- How can you record your work?
- How did you determine that it is not possible to have a height of 5 units?

After students have determined all possible heights of rectangular prisms with a volume of 24 cubic units, ask them to determine all possible dimensions of the rectangular prisms.

- How did you begin to think about this problem?
- How could you prove that you have found all possible dimensions of the rectangular prisms?
- What strategy did you use to solve this problem?
- How does your strategy compare to a classmate's strategy?
- How does your thinking connect to previous mathematical concepts?

Activity Debrief: Facilitate a discussion to ensure all students understand that an efficient method of determining all possible rectangular prisms with a volume of 24 cubic units is to think about factors of 24. From this understanding, students can derive the volume formulas.

Have students revisit the Pose the Problem question and discuss answers.

- What are some ways to determine the volume of this figure?

Guided Exploration

Students generalize the method for determining the volume of a rectangular prism discovered in the previous lesson to derive two formulas for calculating volume of rectangular prisms.



Use and Connect Mathematical Representations

- How are slices of bread like layers? How are they different?
- **Think About It:** When have you multiplied length by width before? What measurable attribute were you finding when you multiplied length by width?



Ensure students understand that *Base* in the formula represents the area of the base of the rectangular prism (as well as the number of cubes in a layer), by having students connect the number of cubes in a layer to the area of the base of that layer.



English Learner Scaffolds

Entering/Emerging Support students in understanding the term *dimensions*. Draw a line. Point and say *This has one dimension*. Next, draw a square. Point and say *This has two dimensions*. Finally, draw a cube, emphasizing its depth. Point and say *This has three dimensions*. Repeat the task with new drawings (such as a point, a triangle, and a cylinder) asking *How many dimensions does this have?*

Developing/Expanding Support students in understanding the term *dimensions*. Draw a line. Point and say *This has one dimension*. Next, draw a square. Point and say *This has two dimensions*. Finally, draw a cube, emphasizing its depth. Point and say *This has three dimensions*. After confirming comprehension of the term, ask students to draw and demonstrate *dimensions* as well. Provide examples and sentence frames for students who need more guidance.

Bridging/Reaching Ask students to explain why it's important to know the dimensions of an object before trying to find its volume. As students provide their explanations, listen for key words and phrases such as *height*, *length*, *width*, and *volume formula*, and provide validation or correction as needed.

Go My Own

Name _____

Label the dimensions and then determine the volume of the figure.

1.  $V = 24$ cubic in.

2.  $V = 84$ cubic in.

What is the volume of the figure? For which volume formula you used exactly. Check students' explanations.

3.  $V = 24$ cubic in.

4.  $V = 24$ cubic in.

5.  $V = 18$ cubic in.

6.  $V = 60$ cubic in.

7. Explain how the Associative Property can be used to mentally find the volume of the figure.

Sample answer: It is easier to mentally multiply 3×4 , then by 10.

Math 1.0 - Volume 28

8. A person's driveway is a rectangular prism, 4 ft long, 2 feet wide, and 3 feet tall. What is the volume of the driveway?
36 cubic ft

9. An Olympic swimming pool is 50 meters long. What is the volume of the swimming pool? **2,500 cubic in.**

10. **Reasonable Thinking** Can you explain or disagree with this statement? Justify your reasoning. "When the edge lengths of 3 rectangular prisms are multiplied, the answer is also correct."
Disagree; Sample answer: When the edge lengths are doubled the volume is 8 times as much because $2 \times 2 \times 2 = 8$.

11. **Order Analysis** Peter says that he can find the volume of a rectangular prism by multiplying the length and width together to find the volume of the figure. Do you agree? Explain.
Yes. Sample answer: You also need to know the height of the figure to find the volume.

Reflect

Can you use a formula to find the volume of a rectangular prism? Explain why or why not.
Answers may vary.

Math 1.0 - Volume
How do you find the volume of a prism?

Practice

Build Fluency from Understanding

Common Error: Exercises 4–5 Students may be confused that the area of the base is given and not the number of cubes in the base layer. Remind them that both are equal to the length times the width.

Practice Item Analysis

Item	DOK	Rigor
1–2	2	Procedural Skill & Fluency
3–6	3	Procedural Skill & Fluency
7	4	Conceptual Understanding
8–9	3	Application
10–11	4	Conceptual Understanding

Reflect

Students complete the Reflect Question.

- Does the base you use to find the volume of a rectangular prism have to be its bottom? Explain why or why not.

Ask students to share their reflections with their classmates.

Math is... Mindset

- What steps did you take to maintain focus?

Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can find the volume of rectangular prisms using formulas.
- I can explain how to find the volume of rectangular prisms using formulas.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Use volume formula	5.MD.C.5.b
2	2	Use volume formula	5.MD.C.5.b
3	2	Use volume formula	5.MD.C.5.b

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 3 or 4 Then have students do

- 3 of 3 Additional Practice or any of the or activities
- 2 of 3 *Take Another Look* or any of the activities
- 1 or fewer of 3 Small Group Intervention or any of the activities

Key for Differentiation

- Reinforce Understanding
- Build Proficiency
- Extend Thinking



Lesson 2-3
Exit Ticket

Name: _____

- Use a formula to find the volume of the rectangular prism.



$V = 4 \times 3 \times 2 = 24$
 $V = 24$ cubic units

Draw a picture.
- If the rectangular prism is filled with unit cubes, how many cubes will fit the prism?



$V = 4 \times 3 \times 2 = 24$
 $V = 24$ unit cubes

Draw a picture.
- Miss Parker's container has a base that is 10 feet long and 6 feet wide. The area of the base is 60 square feet. She fills the container 3 times high with unit cubes. What is the volume of this container?



$V = 10 \times 6 \times 3 = 180$
 $V = 180$ cubic feet

Reflect On Your Learning

1 to 4
 1 2 3 4
 Not confident Fully confident

Adapted from IM 5-MA7-GE-1.8

R Reinforce Understanding

SMALL GROUP

Calculate Volume

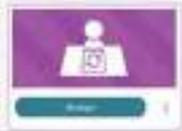
Provide students with a piece of paper showing several rectangular prisms with the length, width, and height labeled in one column and a list of calculated volume in the other. Have students calculate the volumes of the prisms and match them with the values in the volume column. Each prism should be matched with a value. If students struggle, remind them that the Distributive and Associative properties may make it easier to multiply.

GO ONLINE

Take Another Look Lessons

Assign the interactive lesson to reinforce targeted skills.

- The $l \times w \times h$ Volume Formula
- The $B \times h$ Volume Formula



INDEPENDENT WORK

Differentiation Resource Book, p. 5

Lesson 3.3 • Reinforce Understanding
Use Formulas to Determine Volume

Name: _____

Review
 There are 2 formulas you can use to find the volume of the prism.

Example: The volume of a rectangular prism is 24 cubic units.

One Formula	Another Formula
Volume = Base \times Height $V = B \times h$ $V = 3 \times 4$ $V = 12$ cubic units	Volume = length \times width \times height $V = l \times w \times h$ $V = 4 \times 2 \times 3$ $V = 24$ cubic units

Match each figure to its volume.

1. a. 70 cubic units
 2. b. 30 cubic units
 3. c. 108 cubic units
 4. d. 24 cubic units

Illustration: © Pearson Education, Inc.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Volume Showdown

Students practice using a formula to find the volume of rectangular prisms.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 5–6

Lesson 3.3
Additional Practice

Name: _____

Review
 You can calculate the volume of a rectangular prism by multiplying its length, width, and height.

*Example: A rectangular prism has a length of 4 centimeters, a width of 2 centimeters, and a height of 3 centimeters. What is its volume in cm^3 ?
 $V = l \times w \times h = 4 \times 2 \times 3 = 24$ cubic cm.*

Use the given volume formula to calculate the volume of each rectangular prism. $V = l \times w \times h$.

1. $V = 30$ cubic in. $l = 5$ in., $h = 2$ in.
 $V = 30$ cubic in.

2. $V = 7$ cubic in. $l = 3$ in., $h = 4$ in.
 $V = 7$ cubic in.

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Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplying to find area.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 5–6

Label the dimensions of each rectangular prism. Then use the volume formula to calculate the volume of each prism. *Students should label the length, width, and height of each prism.*

1. $V = 54$ cubic units $V = 24$ cubic units

2. Use the two volume formulas, $V = lwh$ and $V = A \cdot h$, with the information you have to find the volume of this rectangular prism.

$l = 5$, $w = 4$, $h = 2$
 $V = 5 \cdot 4 \cdot 2$

3. Calculate the volume of a water glass exactly with the formula $V = lwh$ or $V = A \cdot h$.

$l = 9$, $w = 4$, $h = 3$
 $V = 108$ cubic in.

4. A webkit is a computer program that checks for updates. The size of a webkit file is about 15 square inches, and the height is 3 inches. The volume of the space is $V = 45$ in³ or 45 cubic inches, which is within the range of the file conditions.

Yes, the volume can be calculated using the volume formula $V = lwh$ or $V = A \cdot h$. The area of the base is 15 square inches and the height is 3 inches. The volume of the space is $V = 45$ in³ or 45 cubic inches, which is within the range of the file conditions.

Math in Home Activity

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Student Practice Book

E

Extend Thinking

Use It! Application Station

You Are a Computer Programmer

Students design a computer program to find the volume of a rectangular prism.



WORKSTATIONS

Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 6

Lesson 2.3 • Extend Thinking

Use Formulas to Determine Volume

Given:

Each item is placed in the smallest possible box. Use the dimensions of the box to label the measurements of the objects. Then determine the volume of the box.

1. Dimensions: 2 in \times 2 in \times 4 in
Width: 2 units Height: 4 units

2. Dimensions: 10 in \times 10 in \times 10 in
Width: 10 units Height: 10 units

3. Dimensions: 12 in \times 22 in \times 22 in
Width: 12 units Height: 22 units

4. Dimensions: 100 in \times 1 in \times 1 in
Width: 1 units Height: 1 units

5. What common dimensions do the smallest possible boxes for each object have?

Sample answer: The longest part of the object has the same length as the box. The widest part of the object has the same width as the box. The deepest part of the object has the same depth as the box.

(Illustration: © Pearson Education, Inc.)

INDEPENDENT WORK

Level 2
Volume of Rectangular Prisms

Notes

Which expression(s) can be used to determine the volume of the rectangular prism shown? Select all that apply. Do not actually find the volume of the prism.



Explain your choice(s).
Explanations may vary.

a. 18×2
 b. $3 \times 3 \times 2$
 c. $2(9 \times 2) + 2(3 \times 3) + 2(3 \times 3)$
 d. $18 \times 3 \times 2$
 e. $3 \times 3 \times 6$

Which expression(s) can be used to determine the volume of the rectangular prism shown? Select all that apply. Do not actually find the volume of the prism.



Explain your choice(s).
Explanations may vary.

a. $20 \times 5 \times 3$
 b. 60×3
 c. $20 \times 5 \times 30$
 d. $20 \times 5 \times 15$
 e. $20 \times 31 + 5 \times 15$

Reflect On Your Learning

For what I learned, I still need to learn, I understand it, I can teach someone else.

Analyze The Probe Formative Assessment

Targeted Concept The volume of a rectangular prism may be found by multiplying the three dimensions. It may also be found by multiplying the area of the base by the height.

Targeted Misconceptions Some students lack understanding of volume and the relationship between area and volume. They may use addition to determine volume, confuse volume with surface area, or recognize the formula, $V = l \times w \times h$, as the only way to calculate the volume of a rectangular prism.

Authentic Student Work

Below are examples of correct student work and explanations.

Sample A

Explain your choice(s).



Explain your choice(s).
I chose A and E because with A the problem was just a step ahead from E. It was still using the addition of lwh.

Circle all correct expression(s).

a. 18×2
 b. $3 \times 3 \times 2$
 c. $(3 \times 3) + (3 \times 2) + (3 \times 2)$
 d. $30 \times (3 \times 2)$
 e. $3 \times 3 \times 6$

Sample B

Explain your choice(s).



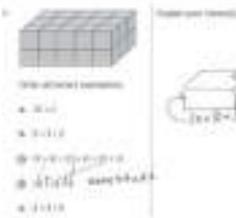
Explain your choice(s).
they are basically the same equation
 $l \times w \times h$
 $20 \times 5 \times 3$
 20×15
 30×20

Circle all correct expression(s).

a. 20×5
 b. 60×3
 c. $(15 \times 5) \times 20$
 d. $20 \times 5 \times 3$
 e. $(20 \times 5) \times (3 \times 3)$

Collect and Assess Student Work

Collect and review student response to determine possible misconceptions. See examples in If-Then chart.

IF incorrect...	THEN the student likely...	Sample Misconceptions
1. b, c 2. a	adds the length of the three dimensions (height, length and width) rather than multiplying, or adds the area of the faces.	
2. e	finds the sum of the areas of the labeled faces.	
1. d 2. c	misapplies the formula, $V = l \times w \times h$, by multiplying the areas of three faces (rather than multiplying the lengths of the three dimensions); OR finds the sum of two dimensions and multiplies that sum by the third dimension.	
1. Chooses e, but not also a 2. Chooses d, but not also b	only recognizes the expression that matches the familiar $V = l \times w \times h$ formula for the volume of a rectangular prism.	

Many of the above difficulties result in a combination of correct and incorrect responses.

For correct responses, be sure to check for sound reasoning.

Take Action

Choose from the following resources or suggestions:

- Revisit the activities on understanding and finding volume in Lessons 2-1, 2-2, and 2-3.
- Use concrete materials to construct rectangular prisms to build understanding of the meaning of volume and to develop a variety of approaches to find volume. These approaches should include counting units and determining the area of a layer, extrapolating to multiple layers that comprise the prism.
- Explore the relationship between area and volume and how knowledge of the area of a base of a prism can be used to find the volume.
- Build understanding that the volume of a rectangular prism can be represented with more than one expression—and that those expressions are equivalent.

Revisit the Probe after additional instruction. Have students review their initial answers to the probe. Use these questions for discussion:

- Are there any answers you would like to change? Which ones?
- Explain why you might want to change them.
- Are there any questions that you still have about any of the items on this probe?

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Determine the Volume of Composite Figures

Learning Targets

- I can find the volume of composite figures.
- I can explain how to find the volume of composite figures.

Standards

Major Supporting Additional

Content

5.MD.C.5.c Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems.

Mathematical Practices and Processes

MPP Reason abstractly and quantitatively.

MPP Model with mathematics.

Vocabulary

Math Terms

composite solid figure
formula

Academic Terms

complex speculate

Materials

The materials may be for any part of the lesson.

- *Nets* Teaching Resource
- ruler
- unit cubes

Focus

Content Objective

- Students determine the volume of composite solid figures.

Language Objectives

- Students discuss how to determine the volume of composite solid figures while answering *Wh-* questions.
- In order to support optimizing output, ELs will participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students engage in active listening and work collaboratively with a partner to complete mathematical tasks.

Coherence

Previous

- Students found and used two formulas to determine the volume of a right rectangular prism with whole-number side lengths (Unit 2).

Now

- Students recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms.

Next

- Students apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems (Unit 2).

Rigor

Conceptual Understanding

- Students build on their understanding of volume by decomposing composite figures to calculate volume. They recognize that volume is additive and to calculate the volume of the composite figure, the volumes of each part must be added.

Procedural Skill & Fluency

- Students build proficiency with calculating volumes of rectangular prisms by using the volume formulas.

Application

- Students build proficiency with calculating volumes of rectangular prisms by using the volume formulas.

Number Routine

Can You Make the Number?



Build Fluency

Students build their number sense as they use combinations of numbers and mathematical operations to make the target number.

Remind students there is more than one solution to the problem. If they find one way, challenge them to continue to find other ways.

These prompts encourage students to talk about their reasoning:

- What two numbers do you want to start with?
- What operation(s) could you perform to create an answer close to 21?
- What other number(s) from the list and which operation(s) could you use to get the number closer to 21?

Purpose Students discuss and share their thoughts about composite figures composed of rectangular prisms.

Notice & Wonder

- How are they the same?
- How are they different?

Teaching Tip You may want to have students work in pairs as they look for similarities and differences. This can help build a collaborative classroom culture. It also allows for greater participation among students as they share their thinking with their partners.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' awareness of composite figures composed of rectangular prisms and are based on possible comments and questions students may make during the share out.

- How do you think the figure on the right was made?
- What do you think is the volume of the figure on the right?

Math is... Mindset

- What can you do today to help build a relationship with a classmate?

Relationship Skill: Build Relationships

Invite students to partner with a new or less familiar peer to complete the activity. Encourage students to actively and respectfully listen to one another as they explore and collaborate to identify similarities and differences.

Transition to Explore & Develop

Establish Goals to Focus Learning

Ask questions that focus students' attention on the additive nature of volume and how it could be used to determine the volume of a composite figure.

- Let's think about how we can use parts of a figure to determine the volume of the figure.



Learn
How can you determine the volume of this figure?



Look for ways to determine rectangular prisms.



Problem 1: Decompose
Why do you find the volume for this figure? Explain why you decomposed a rectangular figure.

Determine the volume of each rectangular prism.



$V = 2 \times 2 \times 2 = 8$
 $V = 8$ cubic ft



$V = 1 \times 1 \times 1 = 1$
 $V = 1$ cubic ft

Apply the volume:
 $24 + 12 = 36$ 24 cubic ft 12 cubic ft

The volume of the figure is 36 cubic feet.

You can determine the volume of this **composite solid figure** by adding the volumes of its rectangular prisms that compose it.

Work Together

How does it differ from your partner's decomposition? Why? What is the volume of the figure?

3 cubic meters



1 Pose the Problem

🗨️ Pose Purposeful Questions

- How are the quantities in this problem related?
- How does the picture help you make sense of those quantities?
- What words will you use to explain your thinking?
- How will the units and labels you will use correspond to the quantities in this problem?

2 Develop the Math

Choose the option that best meets your instructional goal.

👥 Co-Craft Questions and Problems

Pair students and have them co-create a problem similar to the one on the Learn page. Have them work together to solve their problem and then trade their problem with another pair. After each pair solves the other pair's problems, have them form a group of four to check solutions and correct any mistakes that may have been made. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

🗨️ Elicit Evidence of Student Thinking

- How is the process of determining the volume of a composite solid figure similar to the process of finding the area of a composite 2-dimensional figure? How is it different? How is it more complex?

Key Takeaway

- The process for determining the volume of a composite solid figure is similar to the process of finding the area of a composite 2-dimensional figure.

Work Together

Students think about decomposing a composite figure into rectangular prisms to find the volume of the composite figure. Have students work on the problem in pairs before asking them to share their work.

Common Error: Students may struggle because all sides are not labeled. Point out that all the edges and faces in this figure are parallel or perpendicular. Because of that, for example, they can extrapolate the unknown edge lengths.

🗨️ Language of Math

Composite solid figures are not limited to figures composed of rectangular prisms. In Grade 1, students spent time composing solid figures of cubes, right rectangular prisms, right circular cones, right circular cylinders, etc.

Activity-Based Exploration

Students explore the concept of finding the volume of composite solid figures.

Materials: Nets Teaching Resource, ruler

Directions: Have students construct a composite solid figure that matches the figure in the Pose the Problem. Students can measure the prisms to find the dimensions of the figure.

Support Productive Struggle

- What do you notice about this figure?
- How could you decompose this figure?
- What rectangular prisms do you see?
- How is finding the volume of a composite figure similar to finding the area of a composite figure?

Math is... Connections

- Why should the volume be the same whichever way you decompose a composite figure?

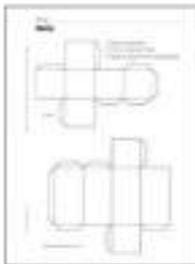
Students are thinking abstractly about the volume of a figure being independent of the way it is decomposed

Activity Debrief: Have students share how they decomposed the composite solid figure and found the volume of each rectangular prism. Encourage students to explain why it was necessary to add the volumes of each rectangular prism to determine the volume of the composite solid figure.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine the volume of this figure?

A PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students extend their understanding of decomposing 2-dimensional composite figures to find area to decomposing composite solid figures to find volume.

Use and Connect Mathematical Representations

- How does this figure look familiar?
- How can the labels in the drawing of the figure help you solve the problem?
- Think About It: Why are some of the dimensions filled in and some are not?

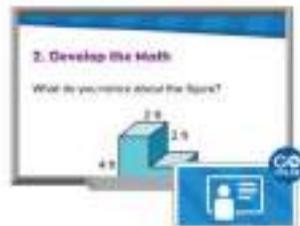
Have students determine the missing lengths. Ensure that students understand the length of the composite figure is 4 feet.

Have students determine the volume using a different decomposition. Show that decomposing the composite figure horizontally results in the same volume. Students may also notice that the composite solid figure can be decomposed into three rectangular prisms.

Math is... Connections

- Why should the volume be the same whichever way you decompose a composite figure?

Students are thinking abstractly about the volume of a figure being independent of the way it is decomposed.



English Learner Scaffolds

Entering/Emerging Support comprehension of the phrase *that compose it*. With students, look together at the sentence below the table on the Learn page. Make sure students understand that *it* refers to the composite solid figure. Have students move a finger from “it” back to “composite solid figure.” Then explain that *that compose it* gives us more information about the prisms. It means that there are rectangular prisms in the composite solid figure. Be sure to accompany your explanation with comprehension supports such as pointing to visuals on the page.

Developing/Expanding Support comprehension of the phrase *that compose it*. With students, look together at the sentence below the table on the Learn page. Ask students what *it* refers to (the composite solid figure). Then ask what *that compose it* gives us more information about (the prisms). Explain to students that this means that there are rectangular prisms in the composite solid figure. Work with students to break down the meaning into more manageable chunks of information: *This is a composite solid figure. In it are two rectangular prisms.*

Bridging/Reaching Work with students to break down the meaning and purpose of the phrase *that compose it*. With students, look together at the sentence below the table on the Learn page. Have students discuss what they think this means. *The composite solid figure has two rectangular prisms in it. You can add the volumes... to... Ensure that students understand that *that compose it* tells us more about the prisms and that *it* refers to the composite solid figure.*

On My Own

1. Label the unknown dimensions of the decomposed figure and then find the volume of the composite solid figure.

$V = 2,300$ cubic in.

2. What is the volume of the figure?

$V = 14$ cubic units $V = 32$ cubic units

3. Draw lines to show how you decomposed the figure. What is the volume of the figure? *Example: 600 square ft.*

$V = 32$ cubic cm $V = 280$ cubic cm

Draw lines to show how you decomposed the figure. What is the volume of the figure? *Example: 600 square ft.*

$V = 60$ cubic ft.

$V = 425$ cubic in.

4. **18in Composite:** An artist engineer is designing an advertisement cube. The cube will have four prisms like the one shown. What is the volume (cubic inch)?

360 cubic in.

5. A sign company needs the letter "H" using rectangular prisms. Each prism is 12 inches by 2 inches by 2 inches. What is the volume of the letter "H" figure?

170 cubic in. *Check students' explanations.*

6. **Student Near-Transfer:** Two rectangular prisms have a combined volume of 18 cubic feet. The volume of one prism is twice the volume of the other prism. What is the volume of each prism? Round your answer.

6 cubic ft and 12 cubic ft. *Check students' work.*

Reflect

How is finding the volume of composite figures similar to finding the area of composite figures?

Answers may vary.

Math is... Mindset

What did you do today to build a better relationship with a classmate?

Practice

Build Fluency from Understanding

Common Error: Exercises 4–5 Students may not include units. Remind them that including correct units in an answer is as important as doing correct calculations.

Practice Item Analysis

Item	DOK	Rigor
1	2	Conceptual Understanding
2–7	3	Procedural Skill & Fluency
8	3	Application
9–10	4	Conceptual Understanding

Reflect

Students complete the Reflect Question.

- How is finding the volume of composite figures similar to finding the area of composite figures?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What did you do to help build a relationship with a classmate?

Students reflect on how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can find the volume of composite figures.
- I can explain how to find the volume of composite figures.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Find volume of composite figures	5.MD.C.5.c
2	2	Find volume of composite figures	5.MD.C.5.c
3	2	Find volume of composite figures	5.MD.C.5.c

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

- 3 of 3 Additional Practice or any of the **U** or **E** activities
- 2 of 3 *Take Another Look* or any of the **U** activities
- 1 or fewer of 3 Small Group Intervention or any of the **R** activities

Key for Differentiation

- U** Reinforce Understanding
- E** Build Proficiency
- R** Extend Thinking



Lesson 2-4
Exit Ticket

Name _____

- Find the volume of the composite figure.

The volume of the figure is **320** cubic units.
- How many cubes does it take to build a set of stairs like this? What is the volume of the solid shown?

The volume of the solid is **1,250** cubic units.
- Which expression shows how to find the volume of the composite figure?

A. $(5 \times 10 \times 5) + (3 \times 10 \times 5)$
 B. $(5 \times 10 \times 5) + (3 \times 10 \times 10)$
 C. $(5 \times 5 \times 5) + (3 \times 5 \times 5)$
 D. $(5 \times 10 \times 5) + (3 \times 10 \times 10)$

Reflect On Your Learning:

How confident do you feel about your learning?

1 (Not at all confident) 2 (Somewhat confident) 3 (Confident) 4 (Very confident)

1 2 3 4

Additional Resources

R Reinforce Understanding

SMALL GROUP

Find the Dimensions

Work with students in pairs. Give each student 24 unit cubes. Have each student use some or all of the cubes to create a composite figure, sketch the figure, and label the dimensions. Then have students switch sketches with their partners and use the labeled sketches to find the volume of each figure. Encourage students to determine how the figures could be divided into two rectangular prisms and what the dimensions of each prism would be. Students can check each other's work by identifying the number of unit cubes used.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Additive Volume Task Cards
Student practice finding the volume of composite figures.

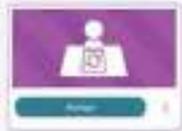


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Recognize Volume as Additive



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 7

Lesson 3-4 • Reinforce Understanding
Determine the Volume of Composite Figures

Name: _____

Review
Decompose a composite figure to find the volume.

Find the volume of the top: $V = 3 \times 3 \times 2$
 $V = 18$ cubic units

Find the volume of the bottom: $V = 3 \times 2 \times 3$
 $V = 18$ cubic units

Add the volume of each part: $V = 18 + 18$
 $V = 36$ cubic units

Find the volume of each figure. Draw lines to show how you decomposed the figure.

A **1,000 cubic ft**

B **7 cubic yd**

INDEPENDENT WORK

Student Practice Book, pp. 7–8

Lesson 3-4
Additional Practice

Name: _____

Review
You can find the volume of a composite solid figure by decomposing the figure, finding the volume of each solid part, and then adding to find the total volume.

The composite solid figure can be decomposed into rectangular prisms with volumes of 28 cubic units and 48 cubic units. The total volume of the composite solid figure is $28 + 48 = 76$ cubic units.

Find the volume of each composite solid figure.

A $V = 42$ cubic units **B** $V = 44$ cubic units

Find the volume of each figure. Draw lines to show how you decomposed the figure.

A $V = 28$ cubic units **B** $V = 87$ cubic units

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplying to find area.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 7–8

5. Find the volume of composite solids by decomposing them. Explain your work.

Top Prism:
 $V = 10 \cdot 10 \cdot 5 = 5 \cdot 100 = 500$ cubic in.

Bottom Prism:
 $V = 10 \cdot 10 \cdot 10 = 10 \cdot 100 = 1,000$ cubic in.

Total Volume:
 $V = 500 + 1,000 = 1,500$ cubic in.

Sample answer: I decomposed the shape into two prisms with a volume of 40 in. \times 30 in. \times 5 in. = 6,000 cubic in. and another prism with a volume of 40 in. \times 30 in. \times 5 in. = 6,000 cubic in. The total volume is 6,000 cubic in. + 6,000 cubic in. = 12,000 cubic in.

6. The shape of an irregularly shaped object is shown. Calculate its volume. Explain your work.

Total Volume:
 $V = 2,250$ cubic in.

Sample answer: I decomposed the composite solid into two prisms with a volume of 30 in. \times 15 in. \times 5 in. = 2,250 cubic in. and another prism with a volume of 30 in. \times 15 in. \times 20 in. = 9,000 cubic in. The total volume is 2,250 cubic in. + 9,000 cubic in. = 11,250 cubic in.

Health or Home Activity

Student Practice Book

E

Extend Thinking

Use It! Application Station

Harvesting Water Students plan and build a model of a rainwater harvesting reservoir.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Differentiation Resource Book, p. 8

Lesson 2-4 • Extend Thinking

Determine the Volume of Composite Figures

Name _____

Sam and Kelly were given the dimensions of composite figures. Sam built the benches using 2 boxes of concrete. The diagrams show how each person built the bench.

1. Calculate the total amount of concrete used for each bench.

Sam: _____

Kelly: _____

Volume: 2,000 cubic in. Name: 2,250 cubic in.

2. Compare the two benches. How are they alike? How are they different?

Sample answer: They are the same size, and they are each made from 2 pieces. They decompose the benches differently.

3. Compare the amount of concrete used for each bench. They use the same amount of concrete.

4. What else you could build? How does the decomposition of the benches affect the amount of concrete used? Explain why.

Sample answer: How the benches is decomposed does not affect the amount of concrete. The benches are identical in size, and, therefore, have the same volume.

Differentiation Resource Book

WORKSTATIONS

GO ONLINE

INDEPENDENT WORK

Solve Problems Involving Volume

Learning Targets

- I can solve problems involving volume.
- I can describe how to solve problems involving volume.

Standards • Major • Supporting • Additional

Content

5.MD.C.5.b Apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems.

Mathematical Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Reason abstractly and quantitatively.

Vocabulary

Math Terms

equation
formula
unknown
variable

Academic Terms

relevant
valid

Materials

The materials may be for any part of the lesson.

- *Problem-Solving Tool Teaching Resource*

Focus

Content Objective

- Students apply the volume formulas to solve real-world problems involving rectangular prisms.

Language Objectives

- Students talk about applying the volume formula to solve real-world problems using the adjective *given*.
- In order to support cultivating conversation, ELs will participate in MLR8: Discussion Supports.

SEL Objective

- Students determine the strategies and analyses necessary to make informed decisions when engaging in mathematical practices.

Coherence

Previous

- Students applied the area and perimeter formulas for rectangles in real world and mathematical problems (Grade 4).
- Students recognized volume as additive. Found volumes of solid figures composed of two non-overlapping right rectangular prisms (Unit 2).

Now

- Students apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems.

Next

- Students recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left (Unit 3).
- Students find the volume of a right rectangular prism with fractional edge lengths (Grade 6).

Rigor

Conceptual Understanding

- Students continue to build on their understanding of volume. They relate volume to multiplication and addition and solve real-world problems involving volume.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students build proficiency with calculating volume of prisms, and determining missing dimensions given the volume, by using the volume formulas.

Application

- Students apply their understanding of volume to solve real-world problems involving volume of rectangular prisms.

Number Routine
Where Does It Go?

Build Fluency

Students build estimation skills and spatial reasoning as they determine a number's position on a number line relative to two other numbers.

These prompts encourage students to talk about their reasoning:

- With what number would you label the center of each number line?
- Where does 532 fall with respect to the center of each number line?
- How can you be sure that 532 can be plotted on each line?

Purpose Students share and discuss volume of real-world objects, and that objects may have the same volume but different dimensions.

Notice & Wonder

- How are they the same?
- How are they different?

Teaching Tip You may wish to have students Think-Pair-Share before inviting volunteers to share what they notice about the different containers.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' awareness of volume of real-world objects, and that objects may have the same volume but different dimensions and are based on possible comments and questions students may make during the share out.

- How can two rectangular prisms with the different dimensions have the same volume?
- If you know the product of three factors and you know two of the factors, how can you determine the factor you do not know?

Math is... Mindset

- How can creative thinking help you solve a problem?

Responsible Decision-Making: Solve Problems

Help students develop responsible decision-making skills by providing them opportunities to practice problem solving. As students begin the Notice & Wonder routine, encourage them to first identify the problem, then think critically about what they will do to solve the problem. As students work through the Notice & Wonder routine, have them think about alternative ways to find objects that have the same volume but different dimensions. Encourage students to use a different strategy to check their answer or identify multiple possible answers/solutions. As you come together to collaboratively discuss the Notice & Wonder routine, you can invite students to share their problem-solving processes.

Transition to Explore & Develop

Establish Goals to Focus Learning

Ask questions that focus students' attention on using the volume formulas to solve real-world problems.

- Let's think about using the volume formulas we know to help us solve real-world problems.



Leena
 A box holds a volume of 24 cubic feet.
 How can you determine the height of the box?



Problem
 How can you determine the height of the box?

Remember volume formula for rectangular prisms.

<p>The volume of the box is 24 cubic feet. The base is 2 square feet.</p> $V = B \times h$ $24 = 2 \times h$	<p>To solve for h, divide both sides of the equation by 2.</p> $\frac{24}{2} = \frac{2 \times h}{2}$ $12 = h$ <p>The box is 12 feet high.</p>
--	--

When solving problems involving volume, you can use the given information to help you determine which volume formula to use.

Work Together

A jewelry box has a volume of 30 cubic inches. What is the height of the jewelry box? Show your work.

3 Use Facts: Examples answers:
 $30 = 3 \times 3 \times 3 \frac{1}{3}$
 $30 = 15 \times 2$
 $30 = 15 \times 1.5 \times 2$



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1 Pose the Problem

LEP Pose Purposeful Questions

- What quantities in this problem are relevant? Why?
- How could a drawing help you make sense of those quantities?
- How could a formula or tool help you solve this problem?

2 Develop the Math

Choose the option that best meets your instructional goal.

DISC Discussion Supports

As students engage in discussing the answers to the questions, restate statements they make as a question to seek clarification. Encourage students to challenge each other's ideas when warranted, as well as to elaborate on their ideas and give examples.

3 Bring It Together

LEP Elicit Evidence of Student Thinking

- How can you check that an unknown dimension you found is valid?
- If you know the height and volume of a rectangular prism, explain how you could find the area of its base.
- Describe how the length, width, height, and volume of a rectangular prism are related.

Key Takeaway

- The volume formulas for rectangular prisms can be used to solve real-world problems.

Work Together

Students think about using volume formulas to determine the missing dimension in a real-world problem. Have students work on the problem in pairs before asking them to share their work.

Common Error: Students may use the wrong unit in their answer, e.g., 2 cubic inches. Remind them that they are trying to determine the height, which is the length of one of the edges of the box, and that length is measured in units, like inches.

Language of Math

Students may be familiar with *context* from their literacy classes. That term is used in mathematics also. Students use the *context* of a real-world problem to write an equation that relates the quantities in the problem and to check if their answer makes sense.

Activity-Based Exploration

Students apply the volume formula to solve real-world problems.

Materials: *Problem-Solving Tool* Teaching Resource

Directions: Distribute copies of the *Problem-Solving Tool* Teaching Resource to each student or pairs. Have students solve the Pose the Problem.

Math is... Quantities

- How can you describe the relationship between the given quantities?

Students are making sense of quantities and their relationships.

Implement Tasks that Promote Reasoning and Problem Solving

- What formula did you use to solve the problem?
- What is another formula you could have used?
- Why might you use one formula and not another?

Activity Debrief: After students solve the problem, have students discuss answers and check students' understanding.

A PDF of the Teaching Resource is available in the Digital Teacher Center.

Guided Exploration

Students apply the volume formula to solve real-world problems.

Math is... Quantities

- How can you describe the relationship between the given quantities?

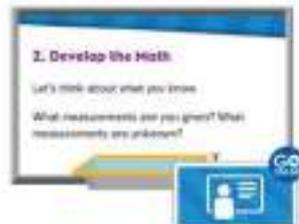
Students are making sense of quantities and their relationships.

Facilitate Meaningful Discourse

- **Think About It:** Why doesn't the formula $V = l \times w \times h$ help solve this problem?
- Does the related division equation $24 \div h = 8$ help you solve the problem? Why or why not?

Have students work in pairs or small groups to discuss strategies to solve unknown factor problems. Invite volunteers to share their strategies. Encourage students to compare the strategy they used to their classmates' strategies.

- Explain why the answer is 3 feet and not 3 cubic feet.



English Learner Scaffolds

Entering/Emerging Support students in understanding the meaning of the word *given* as it pertains to the lesson. Point to *24 cubic feet* in the problem on the Learn page. Say *The volume of the fish tank is given*. Next, point to the fish tank and ask *What other quantity is given?* (*8 square ft*).

Developing/Expanding Support students in understanding the meaning of the word *given* as it pertains to the lesson. Point to *24 cubic feet* in the problem on the Learn page. Say *The volume of the fish tank is given*. Then, without pointing at or gesturing towards the fish tank, ask students to tell you what other quantity is given.

Bridging/Reaching Encourage students to explain how given quantities can help them to find the volume, height, or base of an object. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, I disagree because... or No, given quantities...*

On My Own

Name: _____

1. **Water tanks** to help the football with the groundwater. Which tank will hold the most? Explain.

Saltzman A:  **Saltzman B:**  **Saltzman C; Sample answer:** Saltzman A's volume is approximately 1,080 cubic in., and Saltzman B's volume is approximately 2,970 cubic in.

2. A large container has a volume of 100 cubic inches, a length of 2 inches, and a width of 2 inches. How long is the large container? Show your work.

10 in; Sample work: $l = 2 \times 2 \times 100 \div 2 = 100 \div 2 = 50 \times 2 = 100$

3. The volume of this metal box is 36 cubic feet. What is the width? Show your work.

3 ft; Sample work: $6 \times 3 \times 2 = 36$; $3 = 36 \div 6 \div 2 = 36 \div 12 = 3$

4. The base of a rectangular prism is a square with side length 4 units. The volume of the rectangular prism is 300 cubic centimeters. What is the prism's height? Explain.

4 cm; Sample answer: The area of the base is 20 square cm; $20 \times 4 = 80$, so the height is 4 cm.

Math 1 • Lesson 10

3. **Three boxes.** Determine each box's volume and the surface area of the surface it is 30 cubic feet. Can you agree with Clement's solution? Explain your thinking.

Sample response: I disagree with his solution. The volume of the surface is 32 cubic ft. Clement added the dimensions, rather than multiplying.

4. Use a building's rectangular cross-section to find its floor area. How long and 14 feet high. How many 2 cubic feet of soil does each hole hold? How many holes will cover the field to fix the parking? Explain.

5 cubic ft more; Sample explanation: $V = 2 \times 4 \times 14$; $V = 112$ cubic feet; $112 \div 2 = 56$

5. The aquarium has a volume of 320 cubic meters. What is the width of the tank? Show your work.

10 m; Sample work: $8 \times 4 \times 10 = 320$; $320 \div 4 = 320 \div 8 = 10$

6. **Shared floor thinking:** Rachel is buying a rectangular sandbox with a volume of 50 cubic feet and a height of 2 feet. What are the possible lengths and widths of the sandbox?

Sample answer: 1 ft by 20 ft, 2 ft by 10 ft, 4 ft by 5 ft

Reflect

How did you think this problem was set up to solve these problems?
Answers may vary.

Math 1 • Lesson 10
Practice problem-solving. Read after school to prepare.

Practice

Build Fluency from Understanding

Common Error: Exercise 6 Students may try to find an unknown dimension for this problem. Point out to them that not all real-world problems involving volume are those types of problems. This is a two-step problem. Suggest that students do it in chunks by finding the volume first.

Practice Item Analysis

Item	DOK	Rigor
1	2	Conceptual Understanding
2–3	2	Procedural Skill & Fluency
4–6	4	Procedural Skill & Fluency
7	3	Application
8	4	Conceptual Understanding

Reflect

Students complete the Reflect Question.

- How did you think like a mathematician to solve these problems?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did creative thinking help you solve a problem?

Students reflect on how they practiced responsible decision-making.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can solve problems involving volume.
- I can describe how to solve problems involving volume.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



R Reinforce Understanding

SMALL GROUP

Ready to Fly

Ask student pairs to design suitcases in the shape of rectangular prisms with dimensions no greater than 9 inches \times 14 inches \times 22 inches (the maximum size of a carry-on bag on many airlines). Have students draw and label the dimensions and calculate the volume. Then have them share 2 of the 3 dimensions and the volume with their partner, who finds the missing measurement. As needed, help students write and solve an equation to describe the volume.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Solve Volume Problems



INDEPENDENT WORK

Differentiated Resource Book, p. 9

Lesson 3-5 Reinforce Understanding Solve Problems Involving Volume

Review

The box Joe jumps out of has a volume of 840 cubic inches. How can you determine the height of the box?

The size of the rectangular prism is $14 \text{ in} \times 10 \text{ in} \times 6 \text{ in}$.
 $V = l \times w \times h$
 $840 = 14 \times 10 \times h$
 Joe jumps out of a box that is 6 in high.

1. The base of the popcorn box is 20 square inches. The popcorn box holds 200 cubic inches of popcorn. What is the height of the popcorn box? **5 inches**

2. The volume of a cube is 400 cubic inches. What is the side length?
10 in. $10 \times 10 \times 10 = 1,000$, so the width has to be 10 in.

3. How had 2000 cubic centimeters of greeting cards to make a box. The side length is 20 centimeters and the area of the base is 400 square centimeters. Will the cardstock fit the box containing 2000 cubic centimeters? **No, the volume of the box is 2,000 cubic centimeters, which is less than the cardstock.**

Differentiated Resource Book

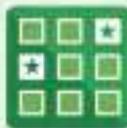
B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Volume Situation Concentration

Students solve word problems involving volume.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 9–10

Lesson 3-5 Additional Practice

Review

You can solve problems involving volume by using the formulae $V = l \times w \times h$ and $V = s^3$.

The unknown length of the rectangular prism can be found by substituting the volume for the volume, width, and height into the volume formula.

$$V = l \times w \times h$$

$$90 = 7 \times 4 \times h$$

$$90 = 28h$$

$$h = 3.21$$

The unknown length is 3.21 centimeters.

1. The volume of the prism is 400 cubic feet. The length is 20 feet and the width is 10 feet. What is the height of the prism?

2. The volume of the rectangular prism is 400 cubic inches. The length is 10 inches and the width is 4 inches. What is the height of the prism?
10 in. Sample answer: The area of the base is $2 \times 2 = 4$. Since $V = l \times w \times h$, $40 = 4 \times 4 \times h$, and so $h = 2.5$.

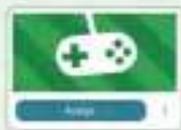
3. The volume of the rectangular prism is 400 cubic inches. The length is 10 inches and the width is 4 inches. What is the height of the prism?
10 in. Sample answer: Since $V = l \times w \times h$, $400 = 10 \times 4 \times h = 40h$. Then $400 = 40h$ so we can solve for h . $400 \div 40 = h$.

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplying to find area.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 9–10

3. A toy box has a volume of 34 cubic feet. It has a length of 3 feet and a height of 2 feet. What is the width of the toy box? **3 ft. Sample answer: I used the volume formula to solve.**

$$\begin{aligned} V &= l \cdot w \cdot h \\ 34 &= 3 \cdot w \cdot 2 \\ 34 &= 6w \\ 34 \div 6 &= w \\ 5.67 &= w \end{aligned}$$

4. Andre has a container in the shape of a rectangular prism that can store 6,000 cubic centimeters of water. The height of the container is 20 centimeters. What is the volume of the container in the container? Show your work.

6,000 cubic cm. $V = 20 \times 20 \times 15 = 6,000$ cubic cm

5. A fish tank has a volume of 42 cubic feet. The dimensions given in the figure are 4 ft by 3 ft by 3 ft. What is the missing dimension? **3 ft. Sample answer: I decomposed the figure into two prisms with dimensions 4 ft by 3 ft by 3 ft (volume of 36 cu. ft.) and another prism with the dimensions 2 ft by 3 ft by 3 ft. Since the total volume is 42 cu. ft., the volume of the second prism is $42 - 36 = 6$ cu. ft. Then I found the missing dimension = 3 ft using volume.**

Math in Motion Activity

M

Extend Thinking

Use It! Application Station

Developing and Using Models Students create a scale model of a kitchen cabinet.



WORKSTATIONS

Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



GO ONLINE

Differentiated Resource Book, p. 10

Lesson 2-5 • Extend Thinking

Solve Problems Involving Volume

Name _____

The volume of a prism is 48 cubic inches. The area of the base of the prism is 12 square inches.

- What are the length and width of the prism? **Yes. Sample answer: The area of the base times the height equals the volume, and $12 \times 4 = 48$.**
- Quinn says that the only possible length and width are 3 inches and 4 inches. Explain or correct Quinn. **No. Sample answer: This is only one of the possible dimensions for the length and width of the base. There are other numbers that multiply to 12, so the length and width could be other measures.**
- List all the possible side lengths for the prism. **1 in. by 12 in., 2 in. by 6 in., and 3 in. by 4 in.**
- What are all the possible dimensions for a prism that has an area of the base 12 square inches and a volume of 48 cubic inches? **1 in. by 12 in., by 4 in., 2 in. by 6 in., by 4 in., 3 in. by 4 in., by 4 in.**
- How many possible rectangular prisms with a base with an area of 12 square inches and a volume of 48 cubic inches are there? **2. Sample explanation: The height must be 4 inches, and there are two ways to get 12, 1 × 12 and 3 × 4.**

Math in Motion Activity

INDEPENDENT WORK

Unit Review Name _____

Vocabulary Review

Choose the correct words to complete each sentence.

1. A **composite solid figure** is a solid figure that is made up of two or more solids. **Lesson 1-6**

2. The space occupied by a 3-dimensional figure, or solid figure, is called **volume**. **Lesson 5-6**

3. A cube with edge lengths of one unit is called a **unit cube**. **Lesson 5-6**

4. A **solid unit** is a unit for measuring volume. **Lesson 5-6**

5. A **formula** is an equation that describes the relationship between two or more quantities. **Lesson 5-6**

6. A 3-dimensional figure with six rectangular faces is called a **rectangular prism**. **Lesson 5-6**

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Review

1. Which rectangular prisms have a volume of 30 cubic units? Select all that apply. **Lesson 5-6**

A. **(A)**

B. **(B)**

C. **(C)**

D. **(D)**

E. The figure shows a rectangular prism partially filled with unit cubes. **Lesson 5-6**

(E)

What is the volume of this rectangular prism? **(E)** 27 cubic units

2. Which equation represents the difference in area of two 6-by-6 squares? **Lesson 5-6**

Block A: **(A)**

Block B: **(B)**

Block C: **(C)**

Block D: **(D)**

(A) $(6 \times 6) - (2 \times 2) = 4 \times (6 \times 6)$
(B) $(3 \times 6) \times 2 = (6 \times 3) \times 2$
(C) $6 \times (6 \times 2) = (6 \times 6) \times (2 \times 2)$
(D) $3 \times 6 \times 2 = (3 \times 6) \times (2 \times 2)$

3. A rectangular prism is 42 feet long, 6 feet wide, and 4 feet high. How many cubic feet of water can it hold? About how many tons is a depth of 2 feet? What is the volume of the water in the pool? **Lesson 5-6**

(A) 1,440 cubic feet
(B) 3,024 cubic feet
(C) 832 cubic feet
(D) 1,680 cubic feet

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Students can complete the **Unit Review** to prepare for the **Unit Assessment**. Students may complete the Review in their Interactive eBook in the Digital Student Center.

Vocabulary Review

Item Analysis

Item	Lesson
1	2-4
2	2-1
3	2-1
4	2-2
5	2-3
6	2-1

Review

Item Analysis

Item	DOK	Lesson	Standard
7	2	2-3	5.MD.C.4
8	2	2-2	5.MD.C.4
9	3	2-3	5.MD.C.5.a
10	2	2-5	5.MD.C.5.b

To review the lessons in this unit, have students watch the Math Replay video in their Digital Student Center.

Assign the Unit Review practice to students from the Digital Teacher Center.



Item Analysis (continued)

Item	DOK	Lesson	Standard
11	3	2-3	5.MD.C.5.a
12	2	2-4	5.MD.C.5.c
13	2	2-4	5.MD.C.5.c
14	3	2-4	5.MD.C.5.c

MATH GO

11. The volume of a rectangular prism is 60 cubic inches. What is the height of the prism? Select all that apply. *Circle 1-3.*

A. length = 20 inches
width = 1 inch
height = 3 inches

B. length = 6 inches
width = 8 inches
height = 4 inches

C. length = 15 inches
width = 10 inches
height = 5 inches

D. length = 12 inches
width = 2 inches
height = 3 inches

12. What is the volume of this figure?
Circle 1-4.



A. 12 cubic units

B. 18 cubic units

C. 24 cubic units

D. 36 cubic units

13. The figure shows the prism for a rectangular prism.



What will be the volume of the rectangular prism?

A. 12,000 cubic feet

B. 24,000 cubic feet

C. 36,000 cubic feet

D. 48,000 cubic feet

14. The combined volume of the two figures shown is 270 cubic inches. What is the height of the rectangular prism? Select all that apply. Circle the volume of the prism in the table.



Circle the height measurement of the 3-D box.

	Height (in.)	Volume (cubic in.)
Box A	3	36
Box B	2	18

Grade 5, Lesson 41

Performance Task

Standards: 5.MD.C.4, 5.MD.C.5.c

Rubric (4 points)

Part A – 2 points

- 2 POINTS** Student's work reflects a proficiency with determining the volume of a figure by counting unit cubes.
- 1 POINT** Student's work reflects developing proficiency with determining the volume of a figure by counting unit cubes.
- 0 POINTS** Student's work reflects a poor understanding of determining the volume of a figure by counting unit cubes.

Part B – 2 points

- 2 POINTS** Student's work reflects a proficiency with solving problems involving volume.
- 1 POINT** Student's work reflects developing proficiency with solving problems involving volume.
- 0 POINTS** Student's work reflects a poor understanding of solving problems involving volume.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

Performance Task

An isopentane-shaped block (shown) is made of unit cubes.



Part A: Use a student solving this task and explain how the figure has a volume of 7 cubic units. Use the powers of 10 to justify your thinking.

Hint: Sample answer: The student did not count the cubes that were hidden under the top layer. The figure has a volume of 10 cubic units.

Part B: The owner ordered 100 cubic units of blocks to use for the figure because it is a rectangular prism that has a length of 5 units, a width of 3 units, and a height of 2 units. How many more cubes does the owner possess now? Show your work and explain your answer.

8 more cubes; Sample answer: The volume of the figure the engineer wants is $3 \times 3 \times 2 = 18$, or 18 cubic units. There are already 10 cubic units, so they need 8 more cubes.

Reflect

Describe how you would determine the volume of each figure shown. *Answers may vary.*

Unit 3
Fluency Practice
Name: _____

Fluency Strategy
Use your knowledge to solve each problem.

Decompose to Subtract

$$346 - 234 = 7$$

$$274 + 253 + 204 =$$

$$89, 742 - 302 = 440$$

$$800 - 31 = 769$$

$$100 - 4 = 96$$

$$440 - 234 = 206$$

1. Decompose by place value to find the difference.

$$575 - 242 = 7$$

$$342 = 300 + 40 + 2$$

$$575 = 500 + 70 + 5$$

$$475 = 400 + 70 + 5$$

$$575 - 242 = 333$$

Fluency Flash
What subtraction equation is represented by the base-ten blocks?

$$249 - 125 = 124$$

Grade 4, Lesson 18

Fluency Check
What is the sum or difference?

3. $448 - 17 = 431$	8. $417 + 254 = 671$
4. $417 + 254 = 671$	9. $304 + 270 = 574$
5. $180 - 52 = 128$	10. $750 - 24 = 726$
6. $347 + 130 = 477$	11. $808 + 210 = 1,018$
7. $107 - 119 = 12$	12. $407 + 152 = 559$

Fluency Task

How would you represent a mixed five to decompose a number by using base ten blocks and two 3-digit numbers?
Explanation may vary.

How do you compare your methods you will using partial sums?
Explanation may vary.

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Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students review decomposing by place value to build fluency with subtracting.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Performance Task

Field Trip to the Science Center

Students draw on their understanding of volume. Use the rubric shown to evaluate students' work.

Standards: 5.MD.C.3, 5.MD.C.3.a, 5.MD.C.4, 5.MD.C.5, 5.MD.C.5.c

Rubric (10 points)

Part A (DOK 1) – 2 points

2 POINTS Student's work identifies which person best shows the volume. The student's explanation is reasonable.

1 POINT Student either identifies the correct person or has a reasonable explanation.

0 POINTS Student does not identify the correct person. The student's explanation is not reasonable.

Part B (DOK 3) – 2 points

2 POINTS Student's work identifies best arrangement for calculating volume. The student's explanation is reasonable.

1 POINT Student either identifies best arrangement for calculating volume or has a reasonable explanation.

0 POINTS Student does not identify the best arrangement for calculating volume. The student's explanation is not reasonable.

Part C (DOK 2) – 2 points

2 POINTS Student's explanation is reasonable. Student's work shows proficiency in finding the volume of a composite figure.

1 POINT Student's explanation is reasonable. Student's work reflects developing proficiency in finding the volume of a composite figure and an inaccurate solution is due to computational errors, rather than conceptual weaknesses.

0 POINTS Student's work shows weak proficiency in finding volume of composite figures. The student's solution is incorrect.

Part D (DOK 2) – 2 points

2 POINTS Student's work shows proficiency in calculating volume of a figure. The student's explanation is reasonable.

1 POINT Student's explanation is reasonable. Student's work reflects developing proficiency in finding the volume of a figure and an inaccurate solution is due to computational errors, rather than conceptual weaknesses.

0 POINTS Student's work shows weak proficiency with volume. The student's solution is incorrect.

Part E (DOK 3) – 2 points

2 POINTS Student's work shows proficiency in calculating volume of a figure. The student's explanation is reasonable.

1 POINT Student's explanation is reasonable. Student's work reflects developing proficiency in finding the volume of a figure. The student's solution is inaccurate due to computational errors, rather than conceptual weakness.

0 POINTS Student's work shows weak proficiency in calculating volume of a figure. The student's explanation is inaccurate.

Unit 3
Performance Task

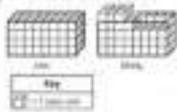
Name _____

Field Trip to the Science Center

A fifth-grade class went on a field trip to the Science Center. At the field trip, the class had to identify cubes and count cubes.

Part A

Jake and Kelly both built cube-like structures.



Which student had more cubes? Explain the volume of the structures? Explain.

Sample answer: Jake shows the volume best because there are no gaps.

Part B

Which arrangement of cubes from Part A makes it easier to calculate the volume? Which arrangement makes it easier to count the cubes, but harder to count?

Sample answer: Jake's arrangement makes it easier to calculate the volume. The second arrangement is the same volume because it is the same number of cubes.

Answer Record Book 28

Part C

At the science station, there is a built tank where scientists can study different sea creatures. Look at the diagram of the built tank.



How would you measure the volume of the built tank? How would you measure the volume of the built tank? Then, find the volume of the built tank.

Sample answer: Decompose the tank into three rectangular prisms. Find the volume of each and then, add them together. The volume of the tank is 100,000 cubic inches.

Part D

At the third station, students can do their own sea-odd hunt to get from sea creatures. The tank measuring 2 inches wide, 2 inches long, and 5 inches high. It contains already has 10 cubic inches of sea life in it. How many more sea life need to fill the tank? Show your work and explain.

The volume of the box is 20 cubic inches. Subtract the 10 cubic inches that already has to get that we need 20 cubic inches more.

Part E

At the last station, students have to find the volume of a tank. It is 3 units high, 3 units wide, and 3 units long. It has 2 different sets of dimensions that would result in a volume of 27 cubic inches. Show your work and explain.

Sample answer: $3 \times 3 \times 3 = 27$ or $3 \times 3 \times 3 = 27$. When you multiply the length, width, and height in both cases, the result is 27. Check students' drawings.

28 Answer Record Book

Unit Assessment

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

Data When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support Intervention Lesson	Standard
1	1	1	Understand Volume	5.MD.C.3
2	2	1	Understand Volume	5.MD.C.3
3	1	3	The $B \times h$ Volume Formula	5.MD.C.5.b
4	1	4	Recognize Volume as Additive	5.MD.C.5.c
5	2	2	Volume Using Unit Cubes	5.MD.C.4
6	2	2	Volume Using Multiplication	5.MD.C.4
7	2	3	The $l \times w \times h$ Volume Formula	5.MD.C.5.b
8	1	3	The $l \times w \times h$ Volume Formula	5.MD.C.5.b
9	2	4	Recognize Volume as Additive	5.MD.C.5.c
10	2	3	The $B \times h$ Volume Formula	5.MD.C.5.b
11	3	5	Solve Volume Problems	5.MD.C.5.c
12	3	3	Solve Volume Problems	5.MD.C.5

Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 2 Unit 2 Assessment, Form A

1. Which of these figures has volume? Choose all that apply.

A. B. C. D.

2. For which equation would you measure using unit cubes?

A. the amount of flour added to a batch
B. the distance between two classrooms
C. the amount of salt added to a mixture
D. the amount of space inside a box

3. Mai is filling a jar with unit-face blocks. The size of the bottom of the jar is 60 square feet. The height of the jar using unit-face blocks is 3 feet. What is the volume of the jar?

A. 177 cubic feet
B. 420 cubic feet
C. 1,800 cubic feet
D. 2,000 cubic feet

4. What is the volume of the figure?

A. 36 cubic units
B. 48 cubic units
C. 54 cubic units
D. 60 cubic units

Answer Key: 1. B, C, D; 2. D; 3. C; 4. C

5. Which rectangular prism has a volume of 63 cubic units? Choose all that apply.

A. B. C. D.

6. Each primary block is a rectangular prism with unit faces. An example is shown.

The volume of the rectangular prism is 12 cubic units.

7. The volume of a rectangular prism is 60 cubic inches. Which could be the dimensions of the prism? Choose all that apply.

A. length = 60 inches, width = 10 inches, height = 20 inches
B. length = 3 inches, width = 5 inches, height = 2 inches
C. length = 10 inches, width = 2 inches, height = 3 inches
D. length = 30 inches, width = 20 inches, height = 10 inches
E. length = 20 inches, width = 4 inches, height = 7 inches

Answer Key: 5. B, D; 6. 12; 7. C, E

Unit 2

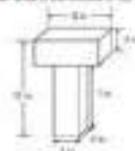
Unit 2 Assessment, Form A (continued)

Name _____

8. Laila's schoolbag is 18 inches long, 8 inches wide, and 12 inches high. What is the volume of the school bag?

- A. 42 cubic inches
 B. 320 cubic inches
 C. 216 cubic inches
 D. 480 cubic inches

9. What is the volume of the T?



- A. 200 cubic inches
 B. 100 cubic inches
 C. 120 cubic inches
 D. 280 cubic inches

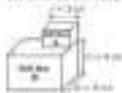
10. A box must have a volume of 48 cubic feet. How tall is the box if it is 4 feet long and 3 feet wide?



The length is 4 feet.

Answer Key Form A

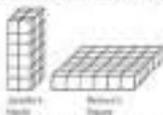
11. The toy gift boxes have a combined volume of 112 cubic centimeters. The dimensions of Gift Box B are half the dimensions of Gift Box A.



Which statement about the gift boxes is true?

- A. The volume of Gift Box A is 7 cubic cm, and the volume of Gift Box B is 4 cubic cm.
 B. The volume of Gift Box A is 64 cubic cm, and the volume of Gift Box B is 8 cubic cm.
 C. The volume of Gift Box A is 64 cubic cm, and the volume of Gift Box B is 16 cubic cm.
 D. The volume of Gift Box A is 36 cubic cm, and the volume of Gift Box B is 72 cubic cm.

12. Jerome and Robert each build a figure using unit cubes.



Jerome says that his figure has greater volume than Robert's figure because it is taller. Is Jerome correct? Explain.

No. Both figures have the same volume. Jerome is wrong. Jerome's figure is $2 \times 2 \times 3 = 36$ cubic cm. Robert's figure is $3 \times 3 \times 2 = 36$ cubic cm. Even though Jerome's figure is taller, it has the same volume as Robert's figure.

Answer Key Form A

Form B

Unit 2

Unit 2 Assessment, Form B

Name _____

1. How many unit cubes are in the figure? Choose all that apply.



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

2. How many unit cubes are in the figure? Choose all that apply.



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

3. How many unit cubes are in the figure?



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

Answer Key Form B

4. How many unit cubes are in the figure?



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

5. How many unit cubes are in the figure? Choose all that apply.



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

6. How many unit cubes are in the figure?



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

7. How many unit cubes are in the figure? Choose all that apply.



- A. 16 unit cubes
 B. 18 unit cubes
 C. 20 unit cubes
 D. 22 unit cubes

Answer Key Form B



Jerome says that his figure has greater volume than Robert's figure because it is taller. Is Jerome correct? Explain.

No. Both figures have the same volume. Jerome is wrong. Jerome's figure is $2 \times 2 \times 3 = 36$ cubic cm. Robert's figure is $3 \times 3 \times 2 = 36$ cubic cm. Even though Jerome's figure is taller, it has the same volume as Robert's figure.

Answer Key Form B

Place Value and Number Relationships

PACING: 12 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  Number Lines	Estimate decimal locations on open number lines.		
3-1 Generalize Place Value	<p>Students relate the value of a digit in a multi-digit whole number in one place value position to that of the same digit in the place to its right.</p> <p>Students relate the value of a digit in a multi-digit whole number in one place value position to that of the same digit in the place to its left.</p>	<p>Students explain how the value of a digit compares to that of the same digit in a different place-value position while answering <i>Wh-</i> and <i>yes/no</i> questions and using the academic term <i>relationship</i>.</p>	<p>Students identify personal traits that make them good students, peers, and math learners.</p>
3-2 Extend Place Value to Decimals	<p>Students relate the value of a digit in a decimal in one place value position to that of the same digit in the place to its right.</p> <p>Students relate the value of a digit in a decimal in one place value position to that of the same digit in the place to its left.</p>	<p>Students discuss how the value of a digit in a decimal compares to that of the same digit in a different decimal place-value position, using the terms <i>hundredths</i> and <i>tenths</i>.</p>	<p>Students discuss and practice strategies for managing stressful situations.</p>
3-3 Read and Write Decimals	<p>Students read and write decimals to the thousandths place in standard form, expanded form, and word form.</p>	<p>Students explain how to read and write decimals to the thousandths place while making sure to include <i>and</i>.</p>	<p>Students actively listen without interruption as peers describe how they approached a complex mathematical task.</p>
3-4 Compare Decimals	<p>Students compare two decimals to the thousandths place using place value and record the comparison using appropriate symbols.</p>	<p>Students explain how to use place value and number lines to compare two decimals, using the terms <i>greater than</i>, <i>less than</i>, and <i>equal to</i>.</p>	<p>Students engage in respectful discourse with peers about various perspectives for approaching a mathematical challenge.</p>
Math Probe Comparing Decimals	Compare two decimals by reasoning about the digits and their values based on place-value positions.		
3-5 Use Place Value to Round Decimals	<p>Students round decimals to any place value position.</p> <p>Students identify situations that call for rounding decimals and determine the place to which to round.</p>	<p>Students identify place values to the nearest whole and tenths place using <i>about</i>.</p>	<p>Students demonstrate thoughtful reflection through identifying the causes of challenges and successes while completing a mathematical task.</p>
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION:
How can I extend my knowledge
of place value to decimals?

LESSON	KEY VOCABULARY	MATERIALS TO GATHER	RIGOR FOCUS	STANDARD	
3-1	<p>Math Terms</p> digit place value place-value chart	<p>Academic Terms</p> cite relationship	<ul style="list-style-type: none"> • <i>Place-Value Chart to Millions</i> Teaching Resource • <i>10 × 10 Grids</i> Teaching Resource 	Conceptual Understanding	5.NBT.A.1
3-2	decimal decimal point tenth hundredth thousandth	contradiction infer	<ul style="list-style-type: none"> • blank number cubes • number cubes 	Conceptual Understanding	5.NBT.A.1
3-3	expanded form standard form word form	expand quality	<ul style="list-style-type: none"> • <i>Decimal Forms</i> Teaching Resources • number cubes 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.A.3.a
3-4	greater than (>) less than (<)	address negate	<ul style="list-style-type: none"> • number cube 	Conceptual Understanding	5.NBT.A.3.b
3-5	estimate round	prove variation	<ul style="list-style-type: none"> • <i>Number Cards 0–10</i> Teaching Resource • number cubes 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.A.4

Unit Overview

Focus

Decimal Concepts

Our number system is called a base-10 place-value system because it takes 10 of one unit to equal 1 unit in the place-value position to the left of the given unit.

Students in Grade 5 have several years of experience with whole-number place value and fraction concepts, and in Grade 4 they began to investigate decimals in tenths and hundredths. They learn that it takes 10 hundredths to equal 1 tenth, and it takes 10 tenths to equal 1.

As students learn more about decimals, they need every opportunity to tie current learning to established understanding. Lesson 3-1 of this unit reviews whole-number place value. Students are asked questions such as: "What pattern do you see as you move from one place to another?" "How does the value of the 3 in the thousands place compare to the value of the 3 in the hundreds place?"

Students learn that the value of a digit in a decimal, as its value in a whole number, depends upon its place in the number. So, the value of a digit is 10 times what it would be in the place to its right, and its value is $\frac{1}{10}$ what it would be to its left.

As students progress through the unit, you may want to provide them with place-value charts and digits cards to give them frequent opportunities to experience concrete correspondences among place values.

Coherence

What Students Have Learned

- **Whole Number Place Value** Students recognized that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. (Grade 4)
- **Volume** Students understood volume. (Grade 5, Unit 2)

What Students Are Learning

- **Decimal Place Value** Students understand decimal place value.
- **Reading and Writing Decimals** Students read and write decimals in number, word, and expanded form.
- **Comparing Decimals** Students compare decimals using the same strategies used for whole numbers.
- **Rounding Decimals** Students round decimals using the same strategies used for whole numbers.

What Students Will Learn

- **Add and Subtract Decimals** Students will add and subtract decimals. (Grade 5, Unit 4)
- **Add, Subtract, Multiply, and Divide Multi-Digit Decimals** Students will fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation. (Grade 6)

Rigor

Conceptual Understanding

Students develop understanding of

- understanding decimal place value;
- using place value understanding to read and write decimals to the thousandths place;
- using number sense to extend place value concepts to rounding decimals;
- using rounding strategies to understand and use to solve problems.

Procedural Skill and Fluency

Students build proficiency with

- comparing and rounding decimals.

Application

Students apply their knowledge of

- understanding decimals to solve problems with real-world contexts;
- comparing and rounding decimals to solve problems with real-world contexts;

Application is not a targeted element of rigor for the standards in this unit.

Effective Teaching Practices

Pose Purposeful Questions

Purposeful questioning facilitates effective assessment of what students know, helps advance their reasoning skills, and reinforces current learning while building bridges to future learning.

The power of purposeful questions can be as simple as the difference between asking “What answer did you get?” and “How did you find the solution?” The answer to the first question is a single number, which is either right or wrong. The answer to the second question describes a process of reasoning and action. The first is an end in itself, while the second reinforces strategies that have been used, with application to future problems and solutions.

Use the *Explore & Develop* questions to assess students’ understanding and encourage discussion.

As the lessons progress, focus on process-oriented questioning. Look for questions that will lead to connections between known concepts and new concepts, and among different aspects of current learning, such as multiple representations of decimals.

Questions focused on reasoning and process can be adapted to meet the needs of all students. Provide conceptual scaffolding as needed by breaking questions into parts. Provide verbal scaffolding by providing sentence frames for English learners.

Math Practices and Processes

Look For and Make Use of Structure

We use a base-ten number system, in which we can move from one place-value position to the next by multiplying or dividing by 10.

As students learn about decimals, they are applying and deepening their understanding of how place value works. They should already be comfortable with multiplying whole numbers by 10, 100, and 1,000. Helping them recall and practice that structure will help them gain facility with the parallel relationships among decimals.

To encourage proficiency, encourage students to find and describe structure in their own words, using their own reasoning, as much as possible.

Some suggestions include:

- Students work in pairs or groups in which each student chooses a different way to represent a decimal or series of decimals.
- Students discuss the similarities and differences between place value to the left of the decimal point and place values to the right of the decimal point.
- Students describe the structure of powers of 10, using general words and providing a specific number series as an example.
- Students write a verbal description of each place in a number with at least three places on each side of the decimal point.

Social and Emotional Learning

What Skills Will We Develop?

- **Self-Awareness: Self-Confidence** (Lesson 3-1): Self-confident students are more willing to take risks, allowing them to learn from mistakes.
- **Self-Management: Manage Stress** (Lesson 3-2): Students who can regulate their stress are resilient and better prepared for academic success.
- **Relationship Skills: Communication** (Lesson 3-3): Students who can communicate effectively are more likely to build strong relationships and contribute to a positive classroom culture.
- **Social Awareness: Develop Perspective** (Lesson 3-4): Developing perspective can help students understand different ways of thinking.
- **Responsible Decision-Making: Reflection** (Lesson 3-5): When students reflect, they can make connections between effort and achievement.

Unit Overview

Language of Math

Vocabulary

Students will be using these key terms in this unit:

- **Decimal** (Lesson 4-2): Students were introduced to decimals in Grade 4. Draw a connection between the root *dec-* (*ten*) and our base-ten number system. Students may be familiar with the word *decade*, which uses the same root.

- **Thousandths*** (Lesson 4-2): *Tenths* and *hundredths* were introduced in Grade 4; *thousandths* is a new term. Students may need reinforcement with the *-ths* ending to distinguish the terms from tens, hundreds, and thousands.

*This is a new term.

Math Language Development

A Focus on Decimal Vocabulary

Mathematical understanding and language usage may require different skills, but they can work together in students' learning of math concepts.

When learners can describe what they are learning, or teach someone else what they have learned themselves, the concepts are reinforced. Also, in describing an operation or conclusion, learners might discover a mistake in their own reasoning that they now have an opportunity to correct.

Using precise terminology—the correct word or phrase for each concept—also reinforces learning. For example, when students are referring to the decimal point, make sure they say, “decimal point” rather than simply, “decimal.”

Consistently model usage of the vocabulary from each lesson, and provide consistent opportunities for students to use each word in discussion and answers to questions.

Help English learners develop fluency with math vocabulary by providing sentence frames and prompts. Frames and prompts should focus on the target vocabulary or concept, while limiting the need for the learner to articulate the less specific parts of a sentence.

Throughout this unit, make sure that students know how to refer to tenths, hundredths, and thousandths, and how to read decimals. You may want to point out that the decimal place values are *not* “symmetric” with respect to the decimal point. Rather, they are “symmetric” with respect to the *ones* place. So, 713.524 is read, “seven hundred thirteen and five hundred twenty-four *thousandths*.” Some students incorrectly read it as, “seven hundred thirteen and five hundred twenty-four *hundredths* (because “hundreds contain three digits”—and there are three digits to the right of the decimal point). The decimal point is read “and” to separate the whole number portion from the decimal portion.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to place value and number relationships. Because many of the words (*related*, *compare*, *estimate*, *about*) and phrases (*one/another way*, *the same as*, *greater/less than*) used in this unit are likely unfamiliar or unknown to ELs, students are supported in understanding and using these words so that instruction is more accessible to them.

Lesson 3-1 – *one way, another way*

Lesson 3-2 – *related*

Lesson 3-3 – *the same as*

Lesson 3-4 – *greater than, less than, compare*

Lesson 3-5 – *estimate, about*

Unit Routines

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

Where Does It Go?

Purpose: Build estimating skills using benchmarks.

Overview: Students place a target number on number lines with different endpoints and justify their placement. In some instances, as a challenge, the target number may not actually belong on one of the number lines.

Decompose It!

Purpose: Build flexibility with numbers.

Overview: Students generate multiple (at least 3) ways to decompose given numbers and share their thinking for each decomposition. The teacher records decompositions and then facilitates a discussion of patterns in the decompositions.

Find the Pattern, Make a Pattern

Purpose: Build efficiency with recognizing and building patterns.

Overview: Students determine the rule(s) for a given pattern, then use the rule(s) to create a new pattern. The teacher records students' new patterns and facilitates a discussion to validate the pattern and its rules.

Sense-Making Routines

- **Which Doesn't Belong?** (Lesson 3-1) For this Which Doesn't Belong? routine, students compare and contrast whole numbers. The purpose of this Which Doesn't Belong? is to get students to extend their understanding of whole-number place value and understand the relationships among place values to the right and left.
- **Notice & Wonder: What do you notice? What do you wonder?** (Lessons 3-2, 3-3) In Lesson 3-2, students discuss partially-filled decimal grids. The purpose of this Notice & Wonder extend students' understanding of whole-number place value to decimals.
- **Notice & Wonder: How are they the same? How are they different?** (Lesson 3-4) Students compare and contrast the weights of backpacks. The purpose of this Notice & Wonder is to get students thinking about comparing decimals and how what they already know about whole-number place value that can help them compare decimals.
- **Notice & Wonder: What do you notice? What do you wonder?** (Lesson 3-5) Students share thoughts on the estimated cost of popcorn. The purpose of this Notice & Wonder is to get students thinking about rounding decimals and how what they already know about whole-number place value that can help them round decimals.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. These routines can also be used as formative assessment opportunities as students develop proficiency in English and mathematical language. They can be used in ways that support real-time-, peer-, and self-assessment. For more information on the Math Language Routines, see the Appendix.

- **Lesson 3–1** Students participate in MLR3: Critique, Correct, and Clarify.
- **Lesson 3–2** Students participate in MLR2: Collect and Display.
- **Lesson 3–3** Students participate in MLR1: Stronger and Clearer Each Time.
- **Lesson 3–4** Students participate in MLR8: Discussion Supports.
- **Lesson 3–5** Students participate in MLR5: Co-Craft Questions and Problems.

Item 3
How Ready Am I?

Name: _____

1. What is the number 70,000,000 written in standard form?
 A. 70,000
 B. 70,000,000
 C. 70,000,000,000
 D. 70,000,000,000,000

2. What is the product?
 10×1000
 A. 10,000
 B. 1,000
 C. 100
 D. 70

3. Which statement is not true?
 A. $700 < 10,200$
 B. $100 < 0.001$
 C. $100,000 < 1,000,000$
 D. $35.7 > 100$

4. Which of these represents $\frac{1}{10}$?
 A.  B. 
 C.  D. 

5. Which of these shows $233,000$ in expanded form?
 A. $2 \times 10,000 + 3 \times 1,000 + 3 \times 10 + 7 \times 1$
 B. $2 \times 100,000 + 3 \times 1,000 + 3 \times 100 + 7 \times 1$
 C. $2 \times 100,000 + 3 \times 10,000 + 3 \times 100 + 7 \times 1$
 D. $2 \times 10,000 + 3 \times 1,000 + 3 \times 100 + 7 \times 1$

Answered Ready Item 3

6. Which number is 100 times greater than 10?
 A. 1
 B. 10
 C. 100
 D. 1,000

7. Which number has a 4 in the ten thousands place, a 7 in the ones place, and a 4 in the hundreds place?
 A. 404,700,000
 B. 385,270,000
 C. 300,000,000
 D. 940,233,000

8. Cheryl solved a multiplication problem and got 800 for the answer. Her friend checked her work and found that the answer was actually 80,000. How many times greater is the value of 8 in 80,000 than the value of 8 in 800?
 A. $\frac{1}{10}$ times as much
 B. 10 times as much
 C. $\frac{1}{100}$ times as much
 D. 1,000 times as much

9. Which 3 numbers are equal to a total of 100. Which 3 numbers are 100 hundredths of a thousand, which comparing about the numbers is least?
 A. Fraction A is smaller than the other 2 because $100 > 100$
 B. Fraction A is smaller than the other 2 because $\frac{1}{10} < \frac{1}{100}$
 C. Fraction B is smaller than the other 2 because $100 < 100$
 D. Fraction B is smaller than the other 2 because $100 > 100$

10. Which number rounds to 800 when rounded to the nearest hundred?
 A. 735
 B. 754
 C. 801
 D. 899

Answered Ready Item 3

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

Use Guided Support Intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill		Guided Support Intervention Lesson	Standard
1	1	Write multi-digit numbers in standard form	Standard & Word Form through 999,999	4.NBT.A.2
2	1	Multiply by factor of 10	Ten Times as Great	4.NBT.A.1
3	2	Compare decimals to hundredths	Compare Fractions & Decimals in 100ths	4.NF.C.7
4	1	Represent decimals on a decimal grid	Decimal Fractions in 100ths	4.NF.C.6
5	1	Write multi-digit numbers in expanded form	Expanded Form through 999,999	4.NBT.A.2
6	2	Number sense	Ten Times as Great	4.NBT.A.1
7	2	Place value	Compare & Order Numbers through 999,999	4.NBT.A.2
8	2	Place value	Ten Times as Great	4.NBT.A.1
9	2	Compare decimals to hundredths	Compare Fractions & Decimals in 100ths	4.NF.C.7
10	2	Round multi-digit numbers	Round to Any Place	4.NBT.A.3

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.



Unit Opener

Focus Question

Introduce the Focus Question, *How can I extend my knowledge of place value to understand decimals?*

Ask students to think about what they know about decimals.

- *What do you already know about decimals?*
- *What can decimals be used for?*
- *What do you already know about place value?*
- *What do think you will be doing in the unit?*

Remind students that at the end of the unit, they will reflect back on what they learned.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

STEM in Action

Videos

Students can watch the two STEM videos.

STEM Career: Astronomer Haley talks about the work of astronomers.

Haley Researches Comets Haley explains the place value positions of decimals.

STEM Project Card

Students can complete the STEM project during their workstation time.

STEM Adventure

Students can complete the STEM adventure during their workstation time.

Unit 3

Place Value and Number Relationships

Focus Question
How can I extend my knowledge of place value to understand decimals?

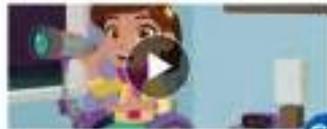
Hi, I'm Haley.
I want to be an astronomer. I will research comets to find out many things they think aren't so cool. It's important that I know how to write numbers correctly. I can use decimal points & & I will need to be able to use place value and decimals to do my job!

STEM | GO ONLINE

STEM Career: Astronomer



Haley Researches Comets



Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson
Game Station	Game Station	Students build proficiency with using decimal numbers.	
		<ul style="list-style-type: none"> • Value of a Digit Sort • Place Value with Decimals Sort • Reading and Writing Decimals Concentration • Decimal Showdown • Rounding Decimals Four in a Row 	3-1 3-2 3-3 3-4 3-5
	Digital Game	Factory Sort Students practice adding and subtracting within 1,000,000.	3-1
			
	Have students complete at least one of the Use It! activities for this unit.		
Application Station	STEM Project Card	How Far? Students research stars and create a model or drawing showing the stars and their distances from Earth.	3-5
			
	Connection Card	On Your Mark, Get Set, Go! Students create a list of times in a swimming meet and compare the times to the results of Olympic swimming events.	3-4
			
Real World Card	State Sales Tax Student investigate and compare state sales tax rates.	3-5	
			

Additional Resources

Use the resources below to provide additional support for this unit.



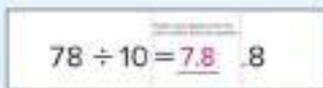
Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the key terms on the front side of the card.



Foldables

Use the unit foldable with Lessons 3-2 and 3-3.



Spiral Review

Students can complete the Spiral Review Practice at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
3-1	4.NF.C
3-2	4.OA.A
3-3	4.NBT.A
3-4	4.NBT.B
3-5	4.NF.A

Generalize Place Value

Learning Targets

- I can recognize that the value of a digit represents ten times as much as it represents in a place to its right.
- I can recognize that the value of a digit represents one-tenth as much as the place to its left.

Standards

Major Supporting Additional

Content

- 5.NBT.A** Understand the place value system.
- 5.NBT.A.1** Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Look for and make use of structure.

Vocabulary

Math Terms

digit
place value
place-value chart

Academic Terms

cite
relationship

Materials

The materials may be for any part of the lesson.

- Place-Value Charts to Millions* Teaching Resource
- 10 × 10 Grids* Teaching Resource
- index cards

Focus

Content Objectives

- Students relate the value of a digit in a multi-digit whole number in one place value position to that of the same digit in the place to its right.
- Students relate the value of a digit in a multi-digit whole number in one place value position to that of the same digit in the place to its left.

Language Objectives

- Students explain how the value of a digit compares to that of the same digit in a different place-value position while answering *Wh-* and *yes/no* questions and using the academic term *relationship*.
- In order to support cultivating conversation, ELs will participate in MLR3: Critique, Correct, and Clarify.

SEL Objective

- Students identify personal traits that make them good students, peers, and math learners.

Coherence

Previous

- Students recognized that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. (Grade 4)

Now

- Students recognize that in a multi-digit whole number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left.

Next

- Students recognize that in a decimal number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left. (Unit 3)

Rigor

Conceptual Understanding

- Students build on place-value concepts by comparing the value of a digit in one place-value position with the value of the same digit in another place-value position when the digits are adjacent or several places away.

Procedural Skill & Fluency

- Students will gain some early experience developing proficiency.
- Procedural skill and fluency is not a targeted element of rigor for this standard.*

Application

- Several problems are presented in a real-world context, and the applications for understanding place value will be further explored later in the unit.
- Application is not a targeted element of rigor for this standard.*

Number Routine

Where Does it Go?

5–7 min

Build Fluency Students determine the location of a decimal on two number lines with different marked endpoints.

Remind students that this is an estimation activity, and exact locations are not needed.

These prompts encourage students to talk about their reasoning:

- What do you notice about the two marked endpoints?*
- Will the point you mark on the top number line appear right above the point you mark on the bottom number line? Explain.*
- What point on the second number line might you mark before you estimate where 0.3 should go?*
- How do you know your answers are reasonable?*

Purpose Students compare and contrast numbers, thinking about the value each digit in a whole number represents.

Which Doesn't Belong

- Which doesn't belong?

Teaching Tip Place-value charts may guide students towards comparing and contrasting these numbers by place value.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' thinking about the value each digit in a whole number represents and are based on possible comments and questions students may make during the share out.

- Which numbers have a 7 in the tens place? Explain what the digit 7 represents in those numbers.
- For the number that does not have a 7 in the tens place, explain what each digit 7 represents in that number.

Math is... Mindset

- How can you give positive feedback to your classmates today?

Self-Awareness: Self-Confidence

Throughout the Which Doesn't Belong? routine, provide opportunities for students to feel confident in themselves. Model and encourage giving positive feedback for sharing ideas, good effort, or creative thinking. Make sure students understand that being good students can also include being helpful peers and active members of the classroom community. Remind students that some tasks are more challenging than others, and they can demonstrate self-confidence by speaking up and asking for help if they need it. Throughout their work with generalizing place value, continue to find other opportunities to allow students to give positive feedback to their classmates.

Transition to Explore & Develop

Ask questions that focus students' attention on the value of each digit in a whole number.

Establish Goals to Focus Learning

- Let's think about what each digit in a number represents and compare them.

Learn

What are some ways to describe the relationship between the values of the digits in the number eleven?

Students describe the relationship between the place-value problems.

1 One Way: Eleven 1000 is 100.

11000 = 10 × 1000

Each 1 is ten times the value of the 1 to its right.

2 Another Way: Eleven 100 is 12,000.

1100 = $\frac{1}{10}$ of 11,000.

Each 1 is $\frac{1}{10}$ the value of the 1 to its left.

A digit represents 10 times as much as it represents in the place to its right. It also represents $\frac{1}{10}$ the value of what it represents in the place to its left.

Work Together

What are two different ways to describe the relationship between the values of each digit in 440,000?

Sample answer: 400,000 is 10 times 40,000; 40,000 is $\frac{1}{10}$ of 400,000.

1 Pose the Problem

LEP Pose Purposeful Questions

- How does the place-value chart help you understand the problem?
- What patterns that you have seen before can help you solve this problem?
- Explain why the value of each digit is not 7.

2 Develop the Math

Choose the option that best meets your instructional goals.

HL5 Critique, Correct, and Clarify

Make a false claim for students to critique. Write 5,555 on the board. Say the 5 in the thousands place is $\frac{1}{10}$ the value of the 5 in the hundreds place. Ask, *Is this statement correct or incorrect? How do you know?* Have the class discuss how to correct your mistake.

3 Bring It Together

LEP Elicit Evidence of Student Thinking

- How would you explain the relationships among the digits in a multi-digit whole number?

Key Takeaway

- A digit in one place in a multi-digit whole number represents 10 times as much as it represents in the place to the right and $\frac{1}{10}$ of what it represents in the place to its left.

Work Together

Students describe the relationships between the hundred thousands and ten thousands places. Make sure that students can describe the relationship in both directions. Students can work on the problem in pairs before sharing their work.

Common Misconception Students may think that the 9 should represent $\frac{1}{10}$ as much as the 4 in the ten thousands place. Make sure they understand that the relationships discussed in this lesson are for the same digit. So, for example, a digit in one place represents 10 times as much as that *same digit* would represent in the place to the right.

LEP Language of Math

A digit and the value it represents are different things. 6 is never $\frac{1}{10}$ or ten times 6. The *value a 6 represents* in one place is 10 times or $\frac{1}{10}$ of the value a 6 represents in a place to its right or left in that number.

Activity-Based Exploration

Students explore the relationship between place-value positions.

Materials: 10×10 Grids Teaching Resource

Directions: Before comparing the values of each digit 7 in the Pose the Problem, have students take a closer look at the value of each place-value position. Provide multiple copies of 10×10 Grids Teaching Resource to each pair or small group. Have students model 1,000, 100, 10, and 1.

Support Productive Struggle

- Did you notice a pattern when determining how to use the 10×10 grids to model the numbers?
- How did you determine how many 10×10 grids are needed to make 1,000? Is there an operation you can use to explain this relationship?
- How did you determine how to partition the 10×10 grid to show 10? How can you explain this relationship using a fraction?

Math is... Structure

- What ideas have you learned before that were helpful in understanding this relationship?

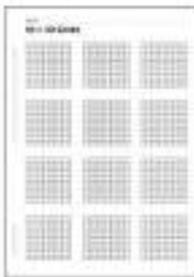
Students are looking for and using the patterns they have already discovered in the structure of the base-ten system.

Activity Debrief: Have pairs or small groups share their strategies for determining how to model each number. Encourage students to use mathematically precise language, such as *10 times* or *one-tenth* when describing their strategies.

Have students revisit the Pose the Problem question and discuss answers.

- What are some ways to describe the relationship between the values of the digits in the number shown?

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students extend their understanding of whole-number place value to the relationships place values represent to the right and to the left.

Use and Connect Mathematical Representations

- How does a place-value chart help you understand the problem?
- Are you partitioning the thousand into equal parts? How does that help you describe the relationship as a fraction?
- **Think About It:** How can you show that 1 is $\frac{1}{10}$ of 10?
- How could another model, like expanded form, help you understand the problem?

Have students state as many relationships in 7,777 as they can.

Math is... Structure

- What ideas have you learned before that were helpful in understanding this relationship?

Students are looking for and using the patterns they have already discovered in the structure of the base-ten system.



English Learner Scaffolds

Entering/Emerging Support students in understanding the meaning of the word *way*. Using manipulatives, show students one way of doing a familiar task, such as grouping. Say, *This is one way*. Then, using the manipulatives again, show students another way of doing that task. Say, *This is another way*. Then, to confirm comprehension, show students one way of doing a new task. Say, *This is one way*. Show me another way.

Developing/Expanding Support students in understanding the meaning of the word *way*. Using manipulatives, show students one way of doing a familiar task. Say, *This is one way*. Then, using the manipulatives again, show students another way of doing that task. Say, *This is another way*. Then, to confirm comprehension, ask students to show you two ways to do a task of their choice, prompting them to use *one way* and *another way* in their descriptions.

Bridging/Reaching Ask students to explain the different strategies they can use to understand the problem. Support students with relevant language as needed, such as one way and another way.

Go My Own

Name _____

Use the place value chart to complete the sentences.

1	2	3	4	5	6
1	2	3	4	5	6

1. The value of the 6 in the thousands place is $60,000$.
 What is the value of the 6 in the hundreds place?

2. Complete the sentences to describe the relationship between the values of each digit 4 and each digit 3 in the number 443,499.

3. The value of the digit 4 in the ten thousands place is the value of the digit 4 in the hundreds thousands place.

4. The value of the digit 4 in the hundreds place is 4 times the value of the digit 3 in the ones place.

Is each statement true or false?

5. The digit 3 in 6,000 is 10 times the value of the digit 3 in 243.
False

6. The digit 3 in 6,000 is $\frac{1}{10}$ the value of the digit 3 in 243.
True

7. The digit 3 in 6,000 is 10 times the value of the digit 3 in 63.
True

8. The digit 3 in 6,000 is $\frac{1}{10}$ the value of the digit 3 in 63.
False

9. On Tuesday, 600 people attended a play at the Dinosaur Theatre. The same play had 5,000 attendees on Saturday. When you compare 600 attendees to 5,000 attendees, 600 is $\frac{1}{10}$ as many as 6,000.

Unit 3 • Number and Number Relationships 65

10. How does the value of the 2 in the hundred thousands place compare to the value of the 2 in the tens thousands place?

2	2	0	0	0	0
2	2	0	0	0	0

Sample answer: 200,000 is 10 times the value of 20,000.

11. How does the value of the 4 in the hundreds place compare to the value of the 4 in the tens thousands place?

4	1	7	3	2	0
4	1	7	3	2	0

Sample answer: 400 is $\frac{1}{10}$ the value of 40,000.

12. **Write a Comparison** Explain how the first place value of today's number is 10 times as much as the first place value of yesterday's number. Write the relationship between the digits 6 in 467.

Sample answer: 60 is 10 times 6, & is $\frac{1}{10}$ of 60.

13. **Number Sense Thinking** Write a number so that the digit 5 has a value of 5,000 and is $\frac{1}{10}$ the value of the digit 4 that has a value of 50,000.

Sample answer: 555,482.

Reflect

What did I think like a mathematician today?
Answers vary.

Math is... Mindset

Write one new lesson confidence that you were encouraged today?

Unit 3 • Number and Number Relationships

Practice

Build Fluency from Understanding

Common Error: Exercise 8 Students may look only at the first digit in each number, which is a 6, and not see the $\frac{1}{10}$ relationship. Remind them that they need to look at the value of the digit 6.

Item Analysis

Item	DOK	Rigor
1–3	2	Procedural Skill & Fluency
4–7	3	Conceptual Understanding
8	3	Application
9–10	3	Conceptual Understanding
11	3	Application
12	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How did I think like a mathematician today?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you give positive feedback to your classmates today?

Students reflect on how they practiced self-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can recognize that the value of a digit represents ten times as much as it represents in a place to its right.
- I can recognize that the value of a digit represents one-tenth as much as the place to its left.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Compare the value of digits	5.NBT.A.1
2	2	Compare the value of digits	5.NBT.A.1
3	2	Compare the value of digits	5.NBT.A.1

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the or activities
2 of 3	<i>Take Another Look</i> or any of the activities
1 or fewer of 3	Small Group Intervention or any of the activities

Key for Differentiation

- Reinforce Understanding
- Build Proficiency
- Extend Thinking



Lesson 3-1
Exit Ticket

Name: _____

1. Which statement correctly compares the digit 9 in 203,276 and 47,823?

- The value of the digit 9 in 203,276 is $\frac{1}{100}$ the value of the digit 9 in 47,823.
- The value of the digit 9 in 203,276 is $\frac{1}{10}$ the value of the digit 9 in 47,823.
- The value of the digit 9 in 203,276 is 10 times the value of the digit 9 in 47,823.
- The value of the digit 9 in 203,276 is 100 times the value of the digit 9 in 47,823.

2. Complete the table for the numbers. Round to the nearest hundred.

Number	Round to the Nearest Hundred	Number	Round to the Nearest Hundred
2	0	3	0
3	0	2	0

Which of these correctly compares the values of the digit 9 in the numbers? Check all that apply.

- 900 is $\frac{1}{10}$ of 3,000.
- 3,000 is 10 times 300.
- 30 is $\frac{1}{10}$ of 300.
- 30 is 10 times 3.

3. Shelly bought 2,000 miles of cell phone service. She then bought 200 miles of cell phone service. How far has she traveled? Write a statement to correctly compare the two distances. 2,000 miles is 10 times as far as 200 miles.

Reflect On Your Learning

no confidence For all learning Understanding I got this! (confidence, etc.)

○ ————— ○ ————— ○ ————— ○

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R Reinforce Understanding

SMALL GROUP

That's the Way!

Distribute two index cards marked " $\times 10$ " and " $\times \frac{1}{10}$ " to each student. Display a large number that includes a blank space for one of the digits. Draw an arrow below a digit that is adjacent to the blank space. Ask students to raise the card that shows the multiplication that they would have to be performed to "move" that digit to the blank space. Have students explain their thinking. Repeat with other numbers and arrows. If students have difficulty, ask them to multiply 20 by 10 and describe the result, and then divide by 20 by 10 and describe the result.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Value of a Digit Sort

Students practice comparing the values of digits in adjacent places within whole numbers.



GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- One-Tenth as Much
- Digits to the Left and Right



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 11

Lesson 24 Reinforce Understanding
Generalize Place Value

Review
Compare the 3s in 36,332.
36,332
The value of the 3 in the thousands place is 30 times the value of the 3 in the hundreds place.
The value of the 3 in the hundreds place is $\frac{1}{10}$ the value of the 3 in the thousands place.

1. How does an 8 in the hundreds place compare with an 8 in the thousands place? **Sample answer:** An 8 in the thousands place is $\frac{1}{10}$ the value of an 8 in the thousands place; an 8 in the hundreds place is 10 times the value of an 8 in the hundreds place.

Write one relationship comparing the value of the 3s in each pair of numbers.

2. 3,576 and 3,587
Sample answer: The 3 in 3,576 is 10 times the value of the 3 in 3,587; the 3 in 3,587 is $\frac{1}{10}$ the value of the 3 in 3,576.

3. 4,023 and 4,015
Sample answer: The 3 in 4,023 is $\frac{1}{10}$ the value of the 3 in 4,015; the 3 in 4,015 is 10 times the value of the 3 in 4,023.

Differentiation Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 11–12

Lesson 24
Additional Practice

Review
You can recognize that the value of a digit represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ as much as it represents in the place to its left.

How does the value of the digit 4 in the thousands place compare to the value of the digit 4 in the hundreds place?

Ten-Thousand Period		Thousands Period		Hundreds Period		Tens Period	
Ten-Thousands	Thousands	Hundreds	Tens	Thousands	Hundreds	Tens	Units
		7	3	9	4	4	1
							2

The value of the digit 4 in the thousands place is 1,000 times the value of the digit 4 in the hundreds place; 4,000 is 10 times as much as 400; 400 is $\frac{1}{10}$ the value of 4,000.

1. Compare the value of the digit 3 in the ten-thousands place to the value of the digit 3 in the thousands place.
The value of the digit 3 in the ten-thousands place is $\frac{1}{10}$ times as much as the value of the digit 3 in the thousands place.
The value of the 3 in the thousands place is $\frac{1}{10}$ times as much as the value of the 3 in the ten-thousands place.

Thousands Period		Tens Period	
Thousands	Hundreds	Tens	Units
1	3	3	8
		9	5

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting within 1,000,000.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 11–12

2. Compare the value of the digit 7 in each number.

Thousands Period			Ones Period		
hundreds	tens	ones	hundreds	tens	ones
9	1	4	5	7	2
		9	3	6	7

The value of the digit 7 in the first place is 70 times as much as the value of the digit 7 in the ones place.

3. A basket has 600 oranges. $\frac{1}{10}$ of the oranges are small. How many small oranges are there? Write the number represented.

The small oranges represent 60 the value of all the oranges.

4. Which of the following are correct? Check all that apply.

- The digit 3 in 9,328 is 10 times as much as the digit 3 in 328.
- The digit 3 in 9,328 is $\frac{1}{10}$ the value as the digit 3 in 328.
- The digit 3 in 9,328 is 10 times as much as the digit 2 in 1,238.
- The digit 3 in 9,328 is $\frac{1}{10}$ the value as the digit 3 in 4,328.
- The digit 3 in 9,328 is 10 times as much as the digit 3 in 4,328.

Math at Home Activity

Use a number cube that has one face with the number 1 and one face with the number 2. Roll the number cube 10 times. Record the number of 1s and 2s that come up. Repeat this activity 10 times. How many 1s and 2s do you get in total?

Student Practice Book

Use It! Application Station

On Your Mark, Get Set, Go! Students create a list of times in a swimming meet and compare the times to the results of Olympic swimming events. *The content of this card has concepts covered later in Lesson 3-4. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Activity

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 12

Lesson 3-1 • Extend Thinking

Generalize Place Value

Write.

Carlo, Lydia, Kevin, and Gina all collect marbles. The number of marbles that each has is shown in the table.

Name	Number of Marbles
Carlo	5,000
Lydia	300,000
Kevin	10
Gina	100

- Compare the number of marbles each made to the number of marbles that Carlo has.

Lydia has 100 times the number of marbles that Carlo has.

Kevin has _____ times the number of marbles that Carlo has.
- Who has $\frac{1}{10}$ the number of marbles that Carlo has?

Kevin.
- Who has 100 times the number of marbles that Gina has?

Lydia.
- Gina has 10,000 marbles. How many the number of marbles that she compares with the number of marbles that _____?
 - Carlo has?

Gina has 10 times the number of marbles that Carlo has.
 - Kevin has?

Gina has 1,000 times the number of marbles that Kevin has.

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Extend Place Value to Decimals

Learning Targets

- I can extend the place value relationship to decimal numbers.
- I can explain the relationship of place values in decimal numbers.

Standards

Major Supporting Additional

Content

- 5.NBT.A** Understand the place value system.
- 5.NBT.A.1** Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left.

Math Practices and Processes

MPP Model with mathematics.

MPP Look for and make use of structure.

Vocabulary

Math Terms

decimal
decimal point
tenth
hundredth
thousandth

Academic Terms

contradiction
infer

Materials

The materials may be for any part of the lesson.

- blank number cubes
- number cubes

Focus

Content Objective

- Students relate the value of a digit in a decimal in one place value position to that of the same digit in the place to its right or left.

Language Objectives

- Students discuss how the value of a digit in a decimal compares to that of the same digit in a different decimal place-value position, using the terms *hundredths* and *tenths*.
- In order to support sense-making, ELs will participate in MLR2: Collect and Display.

SEL Objective

- Students discuss and practice strategies for managing stressful situations.

Coherence

Previous

- Students recognized that in a multi-digit whole number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left. (Unit 3)

Now

- Students recognize that in a multi-digit decimal number, a digit in one place represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left.

Next

- Students read and write decimals to thousandths using standard form, word form, and expanded form. (Unit 3)

Rigor

Conceptual Understanding

- Students deepen and extend their understanding of place-value patterns by reading and writing decimals, and by making multiplicative comparisons by 10 of decimals.

Procedural Skill & Fluency

- Students have some early experiences developing proficiency.
- Procedural skill and fluency is not a targeted element of rigor for this standard.*

Application

- Students apply their understanding of place value to solve contextual problems.
- Application is not a targeted element of rigor for this standard.*

Number Routine

Decompose It!

5–7 min

Build Fluency Students strengthen place-value understanding by decomposing decimal numbers. Students are given a decimal and break it apart in three different ways such that the sum of the parts is equal to the original decimal.

Remind students that there is more than one solution to the problem. As solutions are given, record them for students to evaluate and compare.

These prompts encourage students to talk about their reasoning:

- What strategy to break apart a decimal do you typically think about first?*
- How could you break apart this number to show the sum of the values of the digits? What do you call that decomposition of the number?*
- How can a pattern help you find new “break aparts?”*

Purpose Students share thinking about patterns among 1 , $\frac{1}{10}$ and $\frac{1}{100}$.

Notice & Wonder™

- What do you notice?
- What do you wonder?

Teaching Tip You may want to have students record things they notice and wonder before sharing their ideas with the class.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' noticing of the representations presented and are based on possible comments and questions students may make during the share out.

- How does the amount shaded change from square to square?
- Have you seen this type of representation before? If so, when did you use it?

Math is... Mindset

- What are some ways you can avoid or manage stress?

Self-Management: Manage Stress

After students have completed the Notice & Wonder routine, invite them to share what may have caused them stress. For example, students may have experienced stress if they did not understand a peer's reasoning for the patterns they notice or struggled with describing the patterns they noticed. Discuss ways students can avoid that stress in the future as well as how they can manage or relieve it now. Strategies such as developing a manageable plan, getting organized, taking breaks, and asking for help can help students manage emotional reactions to stress.

Transition to Explore & Develop

Ask questions that focus students' attention on the part of the whole square that is shaded.

Establish Goals to Focus Learning

- Let's think about what part of the squares are shaded and ways we can represent place value in decimal numbers.



Learn

Example: Write the fraction $\frac{1}{10}$ as a decimal.

How can you help Keagan make sense of this number?

Use a representation to show the value of each digit.

The value of the digit 1 depends on its position, not the number.

Example: Factors of 10 are 1 and 10. Factors of 100 are 1, 10, and 100. Factors of 1,000 are 1, 10, 100, and 1,000.

0.001 is one place to the right of 0.01, so it is 10 times as small as 0.01. 0.01 is one place to the right of 0.1, so it is 10 times as small as 0.1. 0.1 is one place to the right of 1, so it is 10 times as small as 1.

Work Together

Write an equation that describes the relationship between 0.1 and 0.01.

Sample answer: 0.1 is ten times 0.01 . 0.01 is $\frac{1}{10}$ of 0.1 .

1 Pose the Problem

Collect and Display

As students discuss the questions, write key words and phrases you hear, such as decimal point, fraction, tenth, hundredth, thousandth, and patterns. Display the words and phrases for student reference and use the student-generated expressions to help make connections between student language and math vocabulary. Update the collection with new understandings as the lesson progresses.

Pose Purposeful Questions

- What does the place-value chart tell you?
- What mathematical patterns about whole number place value do you know? Explain how you could use them to improve Keagan's thinking.
- Could other models or tools help improve Keagan's thinking? Explain how.

2 Develop the Math

Choose the option that best meets your instructional goals.

3 Bring It Together

Elicit Evidence of Student Thinking

- Explain the pattern you see in place values as you move to the right in a decimal number. Explain the pattern you see in place values as you move to the left.
- How could you describe the relationship between hundredths and thousandths? Tenth and thousandths? Ones and thousandths?

Key Takeaways

- The relationship between adjacent place value positions in decimal numbers is the same as in whole numbers. A digit in one place in a decimal number represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left.
- Thousandths are $\frac{1}{1,000}$ of one whole.

Work Together

Students describe the relationships among the tenths and hundredths places in a decimal number in both directions. Students can work on the problem in pairs before sharing their work.

Common Misconception Students may think that tenths, hundredths, thousandths go from right to left as tens, hundreds, thousands do for the whole number part of a decimal. Point out that to the right of the decimal point, they go the opposite way.

Language of Math

Decimal is from the Latin word *decem* meaning *ten*. Students should see *ten*'s role in place value. Other words from the same root are *December* (which was the tenth month) and *decaagon* (a 10-sided polygon).

Activity-Based Exploration

Students construct arguments to support their thinking about the values of the digits in decimal numbers.

Directions: Have students work in pairs or small groups to construct arguments to support their responses to Pose the Problem. Explain to students that they need to have at least two examples to support their arguments. Suggest that they may want to make use of base-ten blocks, drawings, or a place-value chart in their arguments.

Implement Tasks that Support Reasoning and Problem Solving

- What do you notice about the value of a digit when it is in different place-value positions in a number?
- How does the place-value chart help explain the relationship of the values of a digit in different positions in a number?
- What relationship did you notice between the values of the digits in your examples?

Math is... Patterns

- How is the name of the position related to the fractional part of the whole?

Students are seeing the connections between the name of the place and the fraction that represents it.

Activity Debrief: Have students share their arguments. Look for examples, such as the digit 1 in the tenths place has a value of 0.1, which is $\frac{1}{10}$ the value of the digit 1 in the ones place. Encourage students to use precise language, such as *decimal*, *decimal point*, *tenths*, *hundredths*, and *thousandths*.

English Learner Scaffolds

Entering/Emerging Support students in understanding the meaning of the word *related*. Using manipulatives, show two objects that are related in some way. Say *I'm going to show you how these items are related to each other*. Then explain to students how the items are related. Show another pair of objects that are related somehow. Give one statement that correctly explains how the objects are related to each other, and one statement that does not. Ask students after each sentence, *Did I explain how they are related to each other?*

Developing/Expanding Support students in understanding the meaning of the word *related*. Using manipulatives, show two objects that are related in some way. Say *I'm going to show you how these items are related to each other*. Then explain to students how the items are related. Show another pair of objects that are related somehow. Give one statement that correctly explains how the objects are related to each other, and one statement that does not. Ask students after each sentence, *Did I explain how they are related to each other?* Ask them to explain how they know and provide a sentence frame for students who may need more help or prompting.

Guided Exploration

Students extend their understanding of whole-number place value to decimal numbers.

Facilitate Meaningful Discourse

- Why do 0.1 and $\frac{1}{10}$ represent the same quantity?
- **Think About It:** How does the representation show that 0.1 is $\frac{1}{10}$ of 1?
- **Think About It:** How does the representation show that 0.01 is $\frac{1}{10}$ of 0.1?

Have students discuss patterns representing the tenths and hundredths, such as partitioning into 10 equal parts and shading 1 of those parts.

Math is... Patterns

- How is the name of the position related to the fractional part of the whole?

Students are seeing the connections between the name of the place and the fraction that represents it.

- How could you explain to Keagan the difference between the digit 1 and the values of each digit 1 in 1.111?



Bridging/Reaching To support students in answering the questions, ask them to explain how two objects of their choice can be related to each other. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, that doesn't show how they relate to each other... or No, that's not correct because...*

On My Own

Name _____

1. Which of the following statements is true?

A. 0.009 is ten times 0.008
 B. 0.09 is ten times 0.008
 C. 0.08 is $\frac{1}{10}$ of 0.009
 D. $10 \times \frac{1}{10}$ is 0.1

2. Which of the following statements is true?

A. $0.003 \times \frac{1}{10}$ is 0.003
 B. $0.03 \times \frac{1}{10}$ is 0.003
 C. 0.3 is ten times 0.03
 D. 3 is ten times 0.3

Marcello has \$1.50, Mike has \$0.50, and Benjamin has \$0.10. Use this information to complete each sentence.

3. Benjamin has $\frac{1}{10}$ of Marcelllo's money.
 4. Marcelllo has 10 times the money Mike has.

Complete each sentence.

5. \$0.10 is 10 times \$1.00.
 6. \$1.00 is $\frac{1}{10}$ of \$0.10.

7. What are two different ways to describe the relationship between the values of each digit in 0.249?

Sample answer: 0.04 is ten times 0.004, 0.004 is $\frac{1}{10}$ of 0.04.

8. What are two different ways to describe the relationship between the values of each digit in 2.267?

Sample answer: 2 is ten times 0.2; 0.2 is $\frac{1}{10}$ of 2.

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9. **Item Analysis** Why is the number 21.2 zero? Do the values of the digit 2 in the ones place is 10 times the value of the digit 2 in the tenths place. How do you know for sure?

Sample answer: I do not agree. 20 is not 10 times 2; 20 is 10 times 2; the value of the tens place is 10 times the value of the ones place.

10. For which number is the value of the digit 8 ten times the value of the digit 8 in the tenths place?

A. 8.08
 B. 0.808
 C. 0.08
 D. 0.008

11. **Write an Equation** The number 0.005 is ten times smaller than a penny of value 0.05. How do you know? Write an equation that describes the relationship between 0.005 and 0.05.

Sample answer: $0.05 = 10 \times 0.005$
 0.05 is 10 of 0.005 .

12. **Extend Your Thinking** Using only the digits 1, 4, and 5, write a number so that the value of the digit 4 is ten times the value of the digit 1 in the number 145. Write another number so that the value of the digit 4 is $\frac{1}{10}$ the value of the digit 1 in 145.

Sample answer: 1.04

Reflect

What is the relationship between the values of digits in a decimal? How is this relationship between the values of digits in a whole number?

Answers may vary.

What is the number 0.005 is ten times smaller than a penny of value 0.05. How do you know? Write an equation that describes the relationship between 0.005 and 0.05.

Sample answer: $0.05 = 10 \times 0.005$
 0.05 is 10 of 0.005 .

Practice

Build Fluency from Understanding

Common Error: Exercises 3–6 Students may extend 10 times to $\frac{1}{10}$ times. While correct ($\frac{1}{10}$ of a number is $\frac{1}{10}$ times that number), students are not aware of why yet. Encourage the use of $\frac{1}{10}$ of.

Item Analysis

Item	DOK	Rigor
1–6	2	Procedural Skill & Fluency
7–8	3	Conceptual Understanding
9	4	Conceptual Understanding
10	3	Conceptual Understanding
11	3	Application
12	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How is the relationship between the values of digits in a decimal the relationship between the values of digits in a whole number?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What are some ways you can avoid or manage stress?

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can extend the place value relationship to decimal numbers.
- I can explain the relationship of place values in decimal numbers.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Compare the value of digits of decimals	5.NBT.A.1
2	2	Compare the value of digits of decimals	5.NBT.A.1
3	2	Compare the value of digits of decimals	5.NBT.A.1

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the ✔ or ✔ activities
2 of 3	<i>Take Another Look</i> or any of the ✔ activities
1 or fewer of 3	Small Group Intervention or any of the ✔ activities

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 3-2
Exit Ticket

Name _____

1.

ones	tens	hundreds	thousands
9	5	5	6

Which option correctly compares the value of the digit 5 in 95,565 to the other options?

- ✔ The value of the digit 5 in the ones place is 10 times the value of the digit 5 in the hundreds place.
- ✔ The value of the digit 5 in the tens place is 10 times the value of the digit 5 in the ones place.
- ✔ The value of the digit 5 in the hundreds place is $\frac{1}{10}$ the value of the digit 5 in the ones place.
- ✔ The value of the digit 5 in the ones place is $\frac{1}{10}$ the value of the digit 5 in the tens place.

2. Which statements are true? Which statements are false?

0.03 is 10 times 0.3.	True	✔
0.16 is $\frac{1}{10}$ of 0.01.	True	✔
0.2 is $\frac{1}{10}$ of 2.	True	✔
5 is 10 times 0.5.	True	✔

3. Cindy's ribbon is 0.2 meters long. Hedy's ribbon is $\frac{1}{10}$ as long. How many times as long is Hedy's ribbon to Cindy's? Hedy's ribbon is **0.07** meter long.

Reflect On Your Learning

1. How confident are you about your learning today?

○ Not confident ○ Fairly confident ○ Confident ○ Very confident

24. Assessment Resources

R Reinforce Understanding

SMALL GROUP

Is It a Challenge or Not?

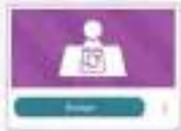
Work with students in small groups. Each student writes 0.0 on a piece of paper. The first student rolls a number cube and writes the number rolled as a digit to the left or right, then rolls an "operation cube" that has $\times 10$ and $\times \frac{1}{10}$ on its faces. That student rewrites the number, moving the digit to the appropriate place. Help the group discuss how to confirm the answer. The next student repeats this process. If students have difficulty, encourage them to think about whether the product will be greater than or less than the original number.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- One-Tenth & 10 Times as Much (Decimals)



INDEPENDENT WORK

Differentiation Resource Book, p. 13

Lesson 3.2 • Reinforce Understanding
Extend Place Value to Decimals

Review

Compare the 6s in 6,662.

6,662

The value of the 6 in the ones place is 10 times the value of the 6 in the tenths place.

The value of the 6 in the tenths place is $\frac{1}{10}$ the value of the 6 in the ones place.

1. How do the 7s in the number 5,779 compare to one another?
Simple answer: The 7 in the tenths place is 10 times the value of the 7 in the hundredths place; the 7 in the hundredths place is $\frac{1}{10}$ the value of the 7 in the tenths place.

2. How do the 2s in the number 2,226 compare to one another?
Simple answer: The 2 in the ones place is 10 times the value of the 2 in the tenths place; the 2 in the tenths place is $\frac{1}{10}$ the value of the 2 in the ones place.

3. How do the 3s in 3,333 compare to the 3s in 3,337?
Simple answer: The 3 in 3,333 is $\frac{1}{10}$ the value of the 3 in 2,333; the 3 in 2,333 is 10 times the value of the 3 in 3,333.

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Place Value with Decimals Sort
Students practice comparing the values of digits in adjacent places within decimal numbers.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



Student Practice Book, pp. 13–14

INDEPENDENT WORK

Lesson 3.2
Additional Practice

Review

You can use place value to find the relationships between different values.

Using the number 166, compare the value of the digit 6 in the tenths place to the value of the digit 6 in the hundredths place.

ones	ones	ones	tenths	hundredths	thousandths
		1	6	6	

The value of the digit 6 in the tenths place is 10 times the value of the digit 6 in the hundredths place.

The value of the digit 6 in the hundredths place is $\frac{1}{10}$ the value of the digit 6 in the tenths place.

1. Loretta weighs the weights 749 pounds, 679 pounds, and 587 pounds. Use the information to complete each sentence.

The weight 679 pounds is $\frac{1}{10}$ times as much as 749 pounds.

The weight 679 pounds is $\frac{1}{10}$ times as much as 6,749 pounds.

2. Shara weighs eight tenths of a pound = 4.08 minutes. Leah weighs eight tenths of a pound = 5.07 minutes. Compare the value of the digit 8 in each value.

The digit 8 in 4.08 is $\frac{1}{10}$ the value of the digit 8 in 5.07.

ones	ones	tenths	hundredths
4	0	8	8

ones	ones	tenths	hundredths
5	0	8	7

Student Practice Book

Read and Write Decimals

Learning Targets

- I can read and write decimals to thousandths using standard form, expanded form, and word form.
- I can make sense of decimals to the thousandths place.

Standards

Major Supporting Additional

Content

- **5.NBT.A** Understand the place value system.
- **5.NBT.A.3.a** Read and write decimals to thousandths using base-ten numerals, number names, and expanded form.

Math Practices and Processes

- MPP** Construct viable arguments and critique the reasoning of others.
- MPP** Attend to precision.

Vocabulary

Math Terms

- expanded form
- standard form
- word form

Academic Terms

- expand
- quality

Materials

The materials may be for any part of the lesson.

- *Decimal Forms* Teaching Resource
- number cubes

Focus

Content Objective

- Students read and write decimals to the thousandths place in standard form, expanded form, and word form.

Language Objectives

- Students explain how to read and write decimals to the thousandths place while make sure to include *and*.
- In order to support maximizing meta-awareness, ELs will participate in MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students actively listen without interruption as peers describe how they approached a complex mathematical task.

Coherence

Previous

- Students wrote multi-digit whole numbers using standard form, word form, and expanded form. (Grade 4)
- Students explain the relationship of the value of digits in different place value positions. (Unit 3)

Now

- Students read and write decimals to thousandths using standard form, word form, and expanded form.

Next

- Students apply their understanding of decimals to compare decimals. (Unit 3)

Rigor

Conceptual Understanding

- Students build on their understanding of place-value patterns to read and write decimals to the thousandths place.

Procedural Skill & Fluency

- Students build proficiency with decimals to the thousandths.

Application

- Students apply understanding of decimals to solve real-world problems.

Application is not a targeted element of rigor for this standard.

Number Routine

Decompose It!



5–7 min

Build Fluency

Students build place-value understanding as they decompose decimal numbers. Students decompose the given decimal in at least three different ways.

As students offer solutions, record them for students to evaluate and compare.

These prompts encourage students to talk about their reasoning:

- What strategy to break apart a decimal do you typically think about first?
- How could you decompose this number to show the sum of the values of the digits? What do you call that decomposition of the number?
- What pattern do you see as you compare the value relationship between two adjacent places?
- How can a pattern help you find new “break aparts?”

Purpose Students discuss decimal numbers, thinking about ways to read and write decimal numbers.

Notice & Wonder™

- What do you notice?
- What do you wonder?

Teaching Tip Encourage students to add onto another student's idea. This promotes opportunities for participation from a variety of students. You can ask questions, such as *Would someone like to add on?* to help elicit more discussion when few students are talking.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' thinking about ways to read and write decimal numbers and are based on possible comments and questions students may make during the share out.

- How can you read the weight of the strawberries?
- If the decimal point were changed to a comma, do you think the number is a reasonable weight for the strawberries?

Math is... **Mindset**

- Why is active listening important?

Relationship Skills: Communication

As students engage in collaborative discourse around the Notice & Wonder routine, encourage them to actively and respectfully listen to one another. Invite students to think about and share what active listening looks and sounds like. As students discuss reading and writing decimals, encourage classmates to listen as well as provide thoughtful feedback. Capitalize on opportunities to also model these behaviors when students are speaking.

Transition to Explore & Develop

Ask questions that focus students' attention on ways to read and write decimal numbers.

Establish Goals to Focus Learning

- Let's think about ways to read and write decimal numbers.




Learn
How can you read the mass of the dumbbell?

This dumbbell is 34.27 kilograms. What do you think the value of each digit is?

Some numbers can be written in expanded form.

3	4	.	2	7
30	4	0.02	0.07	0.007
30 + 4 + 0.02 + 0.07 + 0.007				

34.27 = 30 + 4 + 0.02 + 0.07 + 0.007

34.27 = $3 \times 10 + 4 + \frac{2}{100} + \frac{7}{1000}$

Decimals can be written in expanded form.

34.27

The word form helps you read decimal numbers.

ten	ones	tenths	hundredths
3	4	2	7

34.27 = 3 tens, 4 ones, 2 tenths, and 7 hundredths.

Writing and reading decimal numbers follows the same pattern as reading and writing whole numbers.

Work Together

Copy onto grid in expanded form using multiplication. It has web content boxes for your thinking.

Yes Check students' explanations.

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1 Pose the Problem

1.1 Pose Purposeful Questions

- Based on what you already know, can you make a conjecture about how to read the decimal? Explain what you base your conjecture on.
- What tool might you use to help you read the decimal? Why do you think it would help you?
- Explain how you could use patterns about place value to help you read the decimal.

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Stronger and Clearer Each Time

Ask students to write about how a place-value chart can help them identify the value of digits in decimals. Then have students share their writing with a partner, comparing their sentences, and if needed, make corrections.

3 Bring It Together

3.1 Elicit and Use Evidence of Student Thinking

- What is the last word in the word form for 34.27? Explain why.
- In word form, how are place values the same before and after the *and*? How are they different?
- Billy said expanded form can be written using just multiplication. Is he correct? Explain why or why not.

Key Takeaways

- Reading and writing decimals to thousandths in word form follows the same pattern as reading and writing numbers to 999, but are always followed by the least place value position.
- The word *and* indicates the location of the decimal point when reading and writing decimals in word form.
- Expanded form can be written using multiplication to show the value of each digit.

Work Together

Students explore writing a decimal in expanded form using multiplication. Students can work on the problem in pairs before sharing their work.

Common Misconception Students may be confused by the use of multiplication in this expanded form, and may need a quick refresh on multiplying a fraction by a whole number. Remind them that $\frac{6}{10}$ is the same as $6 \times \frac{1}{10}$.

3.2 Language of Math

Any zero digits that occur to the right of the last non-zero digit in a decimal number are called *trailing zeros*. Five and four-hundred fifty thousandths, 5.450, has a trailing zero. 007 has two *leading zeros*.

Activity-Based Exploration

Students use their understanding of different forms of whole numbers to identify different forms of decimals.

Materials: *Decimal Forms Teaching Resource*

Directions: Cut and distribute each pair or small group a set of *Decimal Forms Teaching Resource*. Students should match the standard form, word form, and expanded form for each decimal.

Support Productive Struggle

- What knowledge can you use to help you get started?
- When have you used word form or expanded form before?
- What if you started with a different number?
- What patterns do you see in the word form of each decimal number?
- What is the same about the expanded form of a decimal number and the expanded form of a whole number? What is different?

Math is... Precision

- Why is it important to include *and* when reading a decimal number?

Students practice communicating precisely to others.

Activity Debrief: After students have completed the activity, display their work for a gallery walk. Have students compare solutions. Facilitate a discussion to identify patterns to develop an understanding of writing decimals in different forms.

Have students revisit the Pose the Problem question and discuss answers.

- How can we read the mass of the strawberries?

The PDF of the Teaching Resource is available in the Digital Teacher Center.

Guided Exploration

Students extend their understanding of word form, standard form, and expanded form to decimal numbers.

Use and Connect Mathematical Representations

- Why is thirty-four and six hundred eighteen *tenths* incorrect?
- How are word form, standard form, and expanded form for decimal numbers the same as they are for whole numbers? How are they different?
- Describe the patterns you see in the denominators of the fractions in the expanded form of a decimal number using fractions.

Have students share strategies for writing a number given in expanded form in standard form. Make sure they can explain their strategies clearly and that they can understand other students' strategies.

Math is... Precision

- Why is it important to include *and* when reading a decimal number?

Students practice communicating precisely to others.



English Learner Scaffolds

Entering/Emerging Support students' understanding of the phrase *the same* as using manipulatives. Show students two objects that are exactly the same. Say *This one is the same as that one*. Show two objects that are related but different from each other. Point to one of the objects and say *This one is not the same as that one. They have differences*.

Developing/Expanding Support students' understanding of the phrase *the same* as using manipulatives.

Choose two pairs of objects, one pair being exactly the same, and one pair being different. Ask students to choose the pair of objects that are the same and explain how they know. Provide a sentence frame as needed.

Bridging/Reaching Ask students to explain how different forms for decimals are the same for whole numbers. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *I disagree because... or No, that's not correct because...*

On My Own

Name _____

What is the word form of the decimal?

1. 0.3 **right and two tenths** 1.002 **right and two thousandths**

2. 0.02 **twenty-two hundredths** 4.0002 **slightly more than four thousandths**

What is the standard form of the decimal?

3. 0.8 + 0.02 + 0.001 = **0.821** 5. 0.2 + 0.7 + 0.08 + 0.006 = **30.986**

4. 5 + 0.25 + 0.005 = **5.255** 6. 7 + $\frac{1}{10}$ + $\frac{2}{100}$ = **7.405**

What is each decimal in standard form?
What is each decimal in expanded form?

7. thirty-three and six thousandths 8. seven and eight hundred forty-six thousandths
33.006; 90 + 3 + 0.006 **7.846; 7 + 0.8 + 0.04 + 0.006**

9. two hundredthirty-two and seven thousandths 11. seven hundred thirty-one thousandths
202.035; 200 + 30 + 2 + 0.03 + 0.005 **0.731; 0.7 + 0.03 + 0.001**

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10. ITEM Connection: The first planet orbiting a star 132 light-years from Earth has a year only six decimal months in expanded form. Is it any form?

2 + 0.9 + 0.03 + 0.007;
two and five hundred thirty-seven thousandths

11. Solve on the decimal: 34.871 is read from left to right as eight hundred thirty-four and eight hundred seventy-one thousandths. Is it correct? Explain why or why not.
No: Sample answer: Isole forgot to add "and" after thirty-four.

12. Expand Four Thousand: Write the word form of 2312.5 and 2312.5. Write a real-world problem using those numbers to solve.
Sample answer: Both have three thousand twenty-one because both have the digits 2312 in either the thousands period or ones period, both have five hundred seventy-eight because both have the digits 578 in either the ones period or in the decimal position.

Reflect

How is place value used when writing decimal numbers in expanded form?
Answer may vary.

Math Talk **Estimate**
How close you get to the actual number today?

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Practice

Build Fluency from Understanding

Common Error: Exercise 7 Students may think that there is only a 1 and 9 in the decimal part of the number and write 5.19. Make sure they remember that thousandths have 3 decimal places and that they need to include a zero.

Item Analysis

Item	DOK	Rigor
1–12	2	Procedural Skill & Fluency
13	3	Application
14–15	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How is place value used when writing decimal numbers in expanded form?

Ask students to share their reflections with their classmates.

Math is... Findset

- What have you done to be an active listener today?

Students reflect on how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can read and write decimals to thousandths using standard form, expanded form, and word form.
- I can make sense of decimals to the thousandths place.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Write decimals in word form	5.NBT.A.3.a
2	2	Write decimals in standard form	5.NBT.A.3.a
3	2	Write decimals in expanded form	5.NBT.A.3.a
4	2	Write decimals in standard form	5.NBT.A.3.a
5	2	Match fractions and decimal fractions	5.NBT.A.3.a

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
5 of 5	Additional Practice or any of the U or E activities
4 of 5	<i>Take Another Look</i> or any of the U activities
3 or fewer of 5	Small Group Intervention or any of the R activities

Key for Differentiation

- U** Reinforce Understanding
- E** Build Proficiency
- R** Extend Thinking



Lesson 3-3
Exit Ticket

Name: _____

- Which is the correct word form of 0.02871?
 - A. twenty-eight and seven hundredths
 - B. two hundred and eight hundredths
 - C. twenty-eight and seven hundredths
 - D. two hundred and eight thousandths**
- Complete the sentence.
In standard form, the number *seven hundred two hundred* is written as 72,200.

What is each decimal number in standard form?

- $8 + 0.3 + 0.005 =$ 8.305
- $30 + 20 + 0.02 + 0.004 =$ 50.024

Which is the decimal form of each fraction? Draw a line to make the words match.

$\frac{7}{10}$	0.007
$\frac{1,000}{100}$	0.007
$\frac{7}{100}$	0.07
$\frac{100}{10}$	0.07
$\frac{1,000}{100}$	0.7
$\frac{7}{10}$	0.7

Reflect On Your Learning

How confident? How well learning? I understand I can teach someone else.

○ ————— ○ ————— ○ ————— ○

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R Reinforce Understanding

SMALL GROUP

Roll and Expand

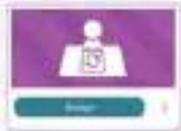
Provide pairs of students with a number cube. Have the students roll three numbers. They record each roll, placing the decimal point so the decimal is to the hundredths. Students then work together to write the decimal in expanded form. Make sure students understand the meaning of the decimal point and the value of each digit. After five successful turns, have students roll four numbers. This time, ask them to place the decimal point so the decimal is to the thousandths. Then have them write each decimal in expanded form.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Standard & Word Form (Large Numbers)
- Expanded Form of Decimal Powers of Ten



INDEPENDENT WORK

Differentiation Resource Book, p. 15

Lesson 3.8 Reinforce Understanding
Read and Write Decimals

Name: _____

Review
 Decimals numbers can be written in standard form, word form, and expanded form.
 Standard form: 12.525
 Word form: twelve and five hundred twenty-five hundredths
 Expanded form: $12 + 2 + \frac{5}{10} + \frac{2}{100} + \frac{5}{1000}$

Write each of the expressions in standard form.

1. forty-two and seventy-three hundredths: 42.73
2. 56 + 37 + 0.03 + 0.009: 56.139

Write each of the expressions in word form.

1. $80 + 8 + \frac{1}{10} + \frac{2}{100}$: eighty-eight and one hundred twenty

Write each of the expressions in expanded form.

1. ninety-seven and five hundred fifty-eight thousandths: $97 + 7 + 0.5 + 0.04 + 0.008$ or $97 + 7 + \frac{5}{10} + \frac{4}{100} + \frac{8}{1000}$
2. $300 + 2 + 0.05 + 0.004$ or $3 + \frac{2}{100} + \frac{5}{1000} + \frac{4}{10000}$

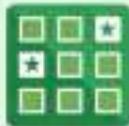
Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Reading and Writing Decimals Concentration
 Students practice matching the word form, standard form, and expanded form of decimal numbers.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 15–16

Lesson 3.8
Additional Practice

Name: _____

Review
 You can write decimals for the thousandths using standard form, expanded form, and word form.

ones	tens	hundreds	thousandths	ten-thousandths
2	7	5	4	9

In the chart, 27,549 is written in standard form. Write the number in expanded form and word form.
 Remember to write the decimal part (if any) when writing the number in word form.

Twenty-seven and five hundred forty-nine thousandths
 After writing the number in expanded form, label each digit by its place value in decimal form.
 $2 \times 10 + 7 \times 10 + 5 \times 100 + 4 \times 1000 + 9 \times 10000$

1. A piece of fabric is 3.76 feet long. Write 3.76 in expanded form using fractions: $3 + \frac{7}{10} + \frac{6}{100}$
2. Write 56.67 in expanded form. Use the place-value chart to find the value of each digit.

ones	tens	hundreds	thousandths	ten-thousandths
5	6	1	0	7

$50 + 6 + 1 + 0 + \frac{7}{1000}$

$50 + 6 + \frac{1}{10} + \frac{7}{10000}$

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting within 1,000,000.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 15–16

- Write each decimal in word form.
 - 1.10 → **one and ten hundredths**
 - 1.20 → **one and twenty hundredths**
 - 1.000 → **one thousandth**
 - 1.0000 → **ten thousandths**
- Write each decimal in decimal form.
 - two and one tenth → **2.1**
 - twenty-one and six hundredths → **21.06**
 - one and twenty-five thousandths → **1.025**
 - eight hundred forty-two thousandths → **0.842**
- Write the standard form of each number with in expanded form.
 - $1 + \frac{2}{10} = \frac{12}{10} = \mathbf{1.2}$
 - $20 + 6 + \frac{6}{100} = \mathbf{26.06}$
 - $100 + 230 + 4500 = \mathbf{79,000}$
 - $1 + 100 + 0.008 = \mathbf{101.008}$
- Colly says that $\frac{1}{10}$ is written in word form as twenty-seven hundredths. Do you agree? Explain.
No. Sample answer: Since the denominator is 100, the fraction is written in word form as twenty-seven hundredths.



Math at Home Activity

Student Practice Book

E

Extend Thinking

Use It! Application Station

How Far? Students research stars and create a model or drawing showing the stars and their distances from Earth. *The content of this card has concepts covered later in Lesson 3-5. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Activity

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 16

Lesson 3-3 Extend Thinking Read and Write Decimals

Name _____

For each planet, write the weight of Pluto's satellites.

Planet	Weight (kg)
Mercury	$3.4 \times 10^2 + 10^3$
Venus	1,000
Mars	$2 + 600 + 4,000$
Jupiter	three and twenty-eight hundredths

- Which two books weigh the same amount?
the math and science books
- Which books weigh 1.25 pounds?
the math and science books
- Which books weigh 1,000 pounds?
the history book
- Which books weigh a 2 in the tenths place?
the math book, English book, and the science book
- Which books weigh two 2 in the hundredths place?
the history book
- Which books weigh an 8 in the hundredths place?
the math and science books

Differentiation Resource Book

INDEPENDENT WORK

Compare Decimals

Learning Target

- I can compare two decimals to the thousandths place using place value.

Standards

Major Supporting Additional

Content

- 5.NBT.A** Understand the place value system.
- 5.NBT.A.3.b** Compare two decimals to thousandths based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons.

Math Practices and Processes

- MPP** Reason abstractly and quantitatively.
- MPP** Use appropriate tools strategically.

Vocabulary

Math Terms greater than ($>$) less than ($<$)

Academic Terms address negate

Materials

The materials may be for any part of the lesson.

- number cube

Focus

Content Objective

- Students compare two decimals to the thousandths place using place value and record the comparison using appropriate symbols.

Language Objectives

- Students explain how to use place value and number lines to compare two decimals, using the terms greater than, less than, and equal to.
- In order to support cultivating conversation, ELs will participate in MLR8: Discuss Supports.

SEL Objective

- Students engage in respectful discourse with peers about various perspectives for approaching a mathematical challenge.

Coherence

Previous

- Students compared two multi-digit numbers based on meanings of the digits in each place, using $>$, $<$, and $=$ symbols to record the results of comparisons. (Grade 4)
- Students read and wrote decimals to thousandths using standard form, word form, and expanded form. (Unit 3)

Now

- Students apply their understanding of decimals to compare decimals.

Next

- Students use place value understanding to round decimals to any place. (Unit 3)

Rigor

Conceptual Understanding

- Students build on their number sense by examining patterns that extend place-value concepts from previous lessons to decimals in the thousandths.

Procedural Skill & Fluency

- Students build proficiency in comparing decimals to the thousandths place using $>$, $<$, and $=$ symbols to record the results of comparisons.

Application

- Students apply their knowledge of using patterns to compare decimals based on real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

Find the Pattern, Make a Pattern

5-7 min

Build Fluency Students build number sense as they determine a pattern and find missing terms. Students then create a new sequence that follows the pattern but uses different numbers.

Remind students that there is more than one way to create a new sequence based on the pattern.

These prompts encourage students to talk about their reasoning:

- What did you notice first?*
- What did you do first? What did you do next? How do you know your pattern works?*
- How did you choose your numbers for the new pattern?*

Purpose Students compare and contrast backpacks, thinking about how to compare decimal numbers.

Notice & Wonder™

- How are they the same?
- How are they different?

Teaching Tip You may want to implement a Turn and Talk routine, which allows students to think about the problem and then turn to a classmate to talk about their thinking. This provides students an opportunity to engage in student-to-student discourse before sharing ideas with the whole group.

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students' thinking about how to compare decimal numbers and are based on possible comments and questions students may make during the share out.

- How are the place values of the numbers similar? How are they different?
- How did you decide that the bags have different weights?

Math is... Mindset

- How can you recognize and respond to the emotions of others?

Social Awareness: Develop Perspective

After the Notice & Wonder routine, invite students to share and discuss the emotions they have experienced as they compared the weights of the bookbags. Collectively discuss how these emotions may make them feel or behave. Engaging in open discourse about their feelings can help students recognize, understand, and respond appropriately to the emotions of others

Transition to Explore & Develop

Ask questions that focus students' attention on how to compare decimal numbers.

Establish Goals to Focus Learning

- Let's think about how to compare decimal numbers.



Launch
Which bag weighs more?



3.28 kg 3.09 kg

Compare the weights by using place value with the greatest place value first.

Place	3	2	8	1
	3	0	9	5

3.28 > 3.09, so the purple bag weighs more than the red bag.

You left a space behind the decimal for the one you compare next digit numbers.

Math & Thinking
Why was 0 not necessary to compare the hundredths place?

3.28 > 3.09, so the purple bag weighs more than the red bag.

Work Together
Compare the weights of these bags.

Place	3	2	8	1
	3	9		

3.28 kg 3.09 kg

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1 Pose the Problem

Discussion Supports

As students engage in discussing the answers to the questions, prompt them to think about how what they learned about comparing whole numbers can help them to compare decimal numbers. Encourage students to challenge each other's ideas when warranted, as well as to elaborate on their ideas and give examples.

Pose Purposeful Questions

- Based on what you know, can you make a conjecture about how to compare decimal numbers? Explain how you would do it and why you think it would work.
- What tools do you think would help you compare decimal numbers? Explain why you think they would help.
- What symbols do you think are used to compare decimal numbers? Explain why.

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit Evidence of Student Thinking

- How would you explain to a friend how to use a place-value chart to compare decimal numbers?

Key Takeaway

- Comparing decimals follows the same process as comparing multi-digit numbers; one compares digits in the same place value position starting with the greatest place value.

Work Together

Students use place value to compare decimal numbers. Students can work on the problem in pairs before sharing their work. Ask students to write the comparison statement they have found another way.

Common Misconception Students may be confused by there being no digits in the hundredths or thousandths places in the lower number. It may help them to write 3.9 as 3.900 and compare, 281 thousandths to 900 thousandths.

Language of Math

Exercise 9 provides an opportunity to discuss metric prefixes and their relationships and how they are similar to place value. A *kilometer* is 1,000 meters. A *centimeter* is $\frac{1}{100}$ of a meter.

Activity-Based Exploration

Students extend their understanding of comparing whole numbers using place value to decimal numbers.

Materials: number cube

Directions: Each student rolls a number cube five times. Students use those five digits to create the greatest possible number that includes a digit in each position from tens to thousandths. If time permits, have students complete the activity to create the least possible number.

Implement Tasks that Support Reasoning and Problem Solving

- What strategies did you use to determine the best position for each digit? Will your strategy always work?
- How would you change your strategy if you could not use the same digit twice?
- How would you change your strategy if you could not use the same digit as your partner?

Math is... thinking

- How did your understanding of place value relationships help you determine the best position for each digit?

Students are making sense of quantities and their relationships.

Activity Debrief: Have students share their strategies for creating the greatest possible decimal. Identify similarities in their strategies, such as placing the greatest digit in the greatest place value position.

Have students revisit the Pose the Problem question and discuss answers.

- Which bag weighs more?

English Learner Scaffolds

Entering/Emerging Use manipulatives such as counting chips to support students' understanding of the terms *greater than*, *less than*, and *compare*. Put two unequal groups of counting chips on the table. Say, *I'm going to compare these two groups*. Count each group and say the numbers aloud. Point to the group with more and say *This group has more chips. [5] is greater than [3]*. Point to the group with fewer chips and say *This group has fewer chips. [3] is less than [5]*. Repeat the task, and ask *Is [4] greater than or less than [6]?*

Developing/Expanding Use manipulatives such as counting chips to support students' understanding of the terms *greater than*, *less than*, and *compare*. Put two unequal groups of counting chips on the table. Say *I'm going to compare these two groups*. Count each group and say the numbers aloud. Point to the group with more and say *This group has more chips. [5] is greater than [3]*. Point to the group with fewer chips and say *This group has fewer chips. [3] is less than [5]*. Have students repeat the task, using the counting chips, by having them compare two groups using *greater than* or *less than*.

Guided Exploration

Students extend their understanding of comparing whole numbers using place value to decimal numbers.

Pose Purposeful Questions

- What different ways can you write the comparison statement? How are they the same? How are they different? Explain your reasoning.
- **Think About It:** Are there other models or tools you could use to compare decimal numbers? How could writing them in expanded form help?

Have students work in pairs or groups to share tips or mnemonic devices to remember whether to use $>$ or $<$ in a comparison statement, e.g., *one side of the sign is bigger... that side goes by the greater number.*

Math is... thinking

- Why was it not necessary to compare to the hundredths place? Students are making sense of quantities and their relationships.



Bridging/Reaching To support students in responding to questions regarding comparing digits, ask students to explain the meaning of the word *compare* and how it relates to decimal numbers. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, to compare means to... and, No, you compare the numbers by...*

On My Own

Name: _____

Write $>$, $<$, or $=$ in each \square to make a true comparison. You can use a place-value chart to help.

1. $1790 \square 8,7$ 2. $1,627 \square 1,000$
 3. $0.03 \square 0.05$ 4. $0.8 \square 0.08$
 5. $7.07 \square 7.07$ 6. $2,000 \square 2,000$

For exercises 7–9, use the cost of each school supply.



7. On the number line, mark the price of each highlighter.

Highlighters

8. Write a comparison statement for the cost of the pens and the pencils.

Sample answer: $1.25 < 1.47$

9. Which school supply is the most expensive? Which school supply is the least expensive? Explain how you know.

Highlighters are the most expensive. Pens are the least expensive. Sample answer: 9 cents is greater than 4 tenths and greater than 1 tenth.

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90. Error Analysis An astronomer calculated a comet traveled 102.40 kilometers. The astronomer wrote 102.4 kilometers on a chart. How do you respond to the astronomer?

Sample answer: I agree with the astronomer because $102.40 = 102.4$.

91. When a comparison statement compares the weight of a number to the weight of a fish.



Sample answer: $22.5 > 20.5$

92. Which of the following comparisons are true?

A. $370 > 1,070$
 B. $85,000 < 100,000$
 C. $0.05 < 0.04$
 D. $0.07 < 0.0007$

93. **Open-Ended Thinking** Write the numbers 500, 5, 72, and 8 to make the greatest possible number.

(8) (5) (7) (5)

Reflect

How is comparing numbers similar to comparing whole numbers?
Answers may vary.

Math Replay
 Watch this 5-minute video to see how to use a place-value chart to compare numbers.

Practice

Build Fluency from Understanding

Common Error: Exercises 1–6 Students often neglect the whole number part of decimal numbers and will conclude that $6.55 < 5.66$ because the first decimal place in 5.66 is greater. Make sure they compare the whole number part first, and, if they are different, the comparison can be made without looking at the decimal part at all.

Item Analysis

Item	DOK	Rigor
1–6	2	Procedural Skill & Fluency
7–8	3	Application
10	4	Application
11	3	Application
12	3	Conceptual Understanding
13	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How is comparing decimals similar to comparing whole numbers?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you recognize and respond to the emotions of others?

Students reflect on how they practiced social awareness.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can compare two decimals to the thousandths place using place value.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Compare decimals	5.NBT.A.3.b
2	2	Compare decimals	5.NBT.A.3.b
3	3	Compare decimals	5.NBT.A.3.b

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

- 3 of 3 Additional Practice or any of the **U** or **E** activities
- 2 of 3 *Take Another Look* or any of the **U** activities
- 1 of 3 Small Group Intervention or any of the **R** activities

Key for Differentiation

- R** Reinforce Understanding
- U** Build Proficiency
- E** Extend Thinking



Lesson 3.4
Exit Ticket

Name: _____

- Is each comparison True or False?

	True	False
$0.8 < 0.76$		<input checked="" type="checkbox"/>
$0.77 < 0.777$	<input checked="" type="checkbox"/>	
$0.025 < 0.026$	<input checked="" type="checkbox"/>	
$0.008 < 0.07$		<input checked="" type="checkbox"/>
- The table shows the amount of water over 8 days.

Day	Amount of Water (in)
Monday	2.25
Tuesday	1.75
Wednesday	2.4
Thursday	2.8

How can you compare the decimal? Complete with $<$, $>$, $=$.

 - A. $2.05 < 2.01$
 - B. $2.05 > 2.4$
 - C. $3.04 < 2.4$
 - D. $2.01 > 2.4$
- Sam swam one length of the pool in 48.23 seconds. Jason swam one length of the pool in 48.84 seconds. Who swam faster?
Jason

Reflect On Your Learning

One worded One exit ticket I understand I need more help

1. _____

R Reinforce Understanding

SMALL GROUP

Place Value War

Work with students in pairs. Provide each student with a stack of number cards between 0–9. Each student draws 3 cards from the stack and places them in numerical order. Have students determine which number is greater. Remind students to compare place values from left to right. If students have difficulty comparing the numbers, help them draw a place-value chart for tenths, hundredths, and thousandths and place their cards inside the chart. Repeat until all cards have been played.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Compare Decimal Numbers in Tenths
- Compare Decimal Numbers (100ths)



INDEPENDENT WORK

Differentiation Resource Book, p. 17

Lesson 34 • Reinforce Understanding
Compare Decimals

Name _____

Review
When comparing decimals, go from left to right comparing digits in the same place.

7	1	5	6
1	1		
4	4		
7	1	8	3
5			8

$7.156 < 7.183$

Circle the words that complete each mathematical sentence.

- 3,725 is greater than 7 ten-thousandths. **greater than**
- 0.45 is greater than 4 tenths. **equal to**
- 9.05 is greater than 9 tenths. **greater than**
- 7.2 is greater than 7 tenths. **greater than**

Select the true statement.

A. $1.98 < 1.97$	A. $2.087 > 2.076$
B. $3.85 < 3.858$	B. $0.3 < 0.038$
C. $0.85 > 31$	C. $6.75 < 6.756$
D. $0.85 < 0.85$	D. $51 > 5.025$

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Decimal Showdown
Students practice comparing decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 17–18

Lesson 34
Additional Practice

Name _____

Review
You can compare two decimals to the thousandths place.

9	3	7	5
9	3	7	6

$9.375 < 9.376$

1. After the 0.3 amount of water and 0.38 amount of salt, use up the numbers on the dice to make a number which amount is less than the other amount.

0.3
0.38

0.3 is less than 0.38 is more.

2. Write the number which is the greatest. Write the number which is the least. Write the number which is the middle.

Write the number greater than 0.3 but less than 0.457.
Help me see and help me talk about it.

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Own It! Digital Station

Build Fluency Games

Assign the digital game to build fluency with adding and subtracting within 1,000,000.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 17–18

- Write a decimal that is closer to 1.5. Explain your answer.
Sample answers: 1.501 to round to 1.5 because anything in 0 to the right of 5 does not change the value of the decimal.
- Which of the following are correct? Check all that apply.
 A. $1.40 < 1.500$
 B. $1.5 > 1.25$
 C. $1.999 > 2.000$
 D. $1.50 < 1.481$
 E. $1.50 < 1.500$
- Lizbeth had \$20.00 for her piggy bank. She had \$10.00 in the piggy bank. Compare the amounts.
\$20.00 $>$ \$10.00
- Lincoln lives 24.28 miles on Monday and 24.30 miles on Tuesday. Compare the distances.
24.30 $>$ 24.28
- Andre and Mal are playing a game. Andre has 15.42 points. Mal has 15.428 points. Compare the number of points. Write the greater number of points.
15.42 $>$ 15.428
Mal has the greater number of points.
- Sheila is 4.20 feet tall. Her cousin Tom is 4.05 feet tall. Compare the heights. Who is taller?
4.20 $>$ 4.05
Sheila is taller.



Use your strategies to solve each problem and check your work. If you are unsure, write a number sentence to help you. Write a number sentence to help you. Write a number sentence to help you. Write a number sentence to help you.

Student Practice Book

E

Extend Thinking

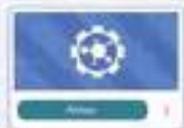
Use It! Application Station

On Your Mark, Get Set, Go! Students create a list of times in a swimming meet and compare the times to the results of Olympic swimming events.



STEM Activity

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 18

Lesson 3-4 • Extend Thinking Compare Decimals

Name _____

The table shows the distance from the store to the city for the following cities.

City	Distance from the store
Monday	$250 + 50 + 4 + 8 + 10 + 4 + 50$
Tuesday	250
Wednesday	How much less than my city and how much less than Monday?
Thursday	$250 + 50 + 4 + 50 + 4 + 50 + 50$
Friday	www.random.com/area-and-concentrations

- Circle the city that is closest to the store (smallest number of miles) **Thursday**.
- Circle the city that is farthest from the store (largest number of miles) **Tuesday**.
- Did Monday drive more or less miles on Monday than the city on Thursday? **less**.
- Write a comparison statement using the distances listed for Monday and Wednesday. Write the numbers in standard form and add $>$, $=$, or $<$.
Sample answer: $250.6 > 250.406$; $250.406 < 250.6$
- Write a comparison statement using the distances listed for Monday and Thursday. Write the numbers in standard form and add $>$, $=$, or $<$.
Sample answer: $250.609 < 249.6$; $249.6 > 249.609$
- Put the greatest number above in order from least to greatest in standard form. **249.606 ; 249.6 ; 250.406 ; 250.53 ; 250.6**

Differentiation Resource Book

Unit 3
Comparing Decimals

Write

Compare the decimals by choosing $>$, $<$, or $=$.

1. 0.006 0.008
Circle the symbol that goes in the .

2. 0.47 0.470
Circle the symbol that goes in the .

3. 0.47 0.470
Circle the symbol that goes in the .

4. 0.47 0.470
Circle the symbol that goes in the .

Explain or show why you chose that symbol.
Explanations may vary.

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1. 0.06 0.070
Circle the symbol that goes in the .

2. 0.47 0.470
Circle the symbol that goes in the .

3. 0.47 0.470
Circle the symbol that goes in the .

4. 0.47 0.470
Circle the symbol that goes in the .

Explain or show why you chose that symbol.
Explanations may vary.

Reflect On Your Learning

100% Confident 75% Confident 50% Confident 25% Confident

○ ——— ○ ——— ○ ——— ○

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Analyze the Probe ✔ Formative Assessment

Targeted Concept Compare two decimals by reasoning about the digits and their values based on place-value positions.

Targeted Misconceptions Compare two decimals by reasoning about the digits and their values based on place-value positions.

Authentic Student Work

Below are examples of correct student work and explanations.

Sample A

4. 0.47 0.470
Circle the symbol that goes in the .

Explain or show why you chose that symbol.

47 470
same thing really
like 4 and 40
4 tenths 4 hundredths

$>$ $<$ $=$

Sample B

1. 0.035 0.35
Circle the symbol that goes in the .

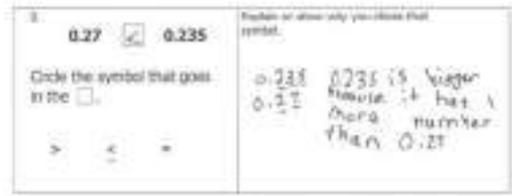
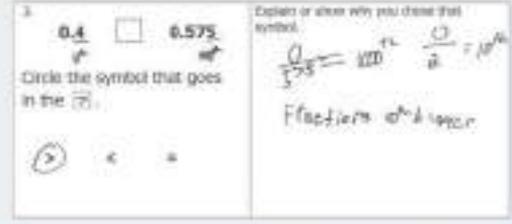
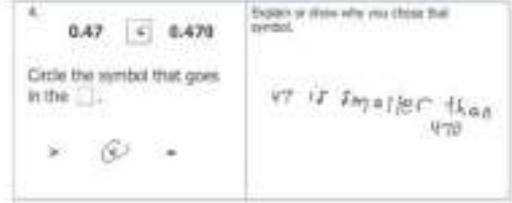
Explain or show why you chose that symbol.

035 = 3¢
35 = 35¢
35 is a greater number of cents

$>$ $<$ $=$

Collect and Assess Student Work

Collect and review student response to determine possible misconceptions. See examples in If-Then chart.

IF incorrect... THEN the student likely...	Sample Misconceptions
<p>1. > thinks that the decimal that contains more digits to the right of the decimal point is the <i>greater</i> decimal. This student does not compare decimals by first considering the digits in the greatest place-value position. Note that this misconception leads to the correct answer for Exercise 3.</p> <p>2. <</p> <p>4. <</p>	
<p>3. > thinks that the decimal that contains more digits to the right of the decimal point is the <i>smaller</i> decimal. The student reasons that because 0.4 extends only to the tenths place, it is therefore greater than 0.575 that extends to the thousandths place (because thousandths are smaller than tenths). This student does not compare decimals by first considering the digits in the greatest place-value position. Note that this misconception leads to the correct answers for Exercises 1 and 2.</p>	
<p>1. =</p> <p>4. > or <</p> <p>OR</p> <p>does not realize that annexing a 0 to the right of a decimal does <i>not</i> change its value. For example, in Exercise 4, a 0 can be annexed to the right of 0.47 without changing its value ($0.47 = 0.470$). However, in Exercise 1, inserting a 0 to the left of the 3 in 0.35 changes its value ($0.035 \neq 0.35$).</p>	

Many of the above difficulties result in a combination of correct and incorrect responses.

For correct responses, be sure to check for sound reasoning.

Take Action

Choose from the following resources or suggestions:

- Revisit a place-value chart, number lines, and other representations in Lessons 3-2 and 3-3 to build decimal place-value ideas and the comparison of decimals.
- Support students in representing decimals with money and interpreting the meaning of digits in various place-value positions.
- Build place-value ideas by using language that reinforces place value. For example, rather than reading 3.45 as *three point four five*, students should read it as *three and forty-five hundredths*.
- Provide a variety of decimals with 0s in different locations. Discuss cases where inserting a 0 changes the value of a number (such as the 0 in 1.405) and cases where it does not (such as the 0 in 1.450).

Revisit the Probe after additional instruction. Have students review their initial answers to the Probe. Use these questions for discussion:

- Are there any answers you would like to change? Explain why you might want to change them.
- Are there any questions that you still have about any of the exercises on this Probe?

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Use Place Value to Round Decimals

Learning Targets

- I can use rounding strategies to round decimals.
- I can explain how to apply rounding strategies to decimals.

Standards Major Supporting Additional

Content

- **5.NBT.A** Understand the place value system.
- **5.NBT.A.4** Use place value understanding to round decimals to any place.

Math Practices and Processes

MPP Attend to precision.

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

round
estimate

Academic Terms

prove
variation

Materials

The materials may be for any part of the lesson.

- number cubes
- *Number Cards 0–10* Teaching Resource

Focus

Content Objectives

- Students round decimals to any place value position.
- Students identify situations that call for rounding decimals and determine the place to which to round.

Language Objectives

- Students identify place values to the nearest whole and tenths place using *about*.
- In order to support optimizing output, ELs will participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students demonstrate thoughtful reflection through identifying the causes of challenges and successes while completing a mathematical task.

Coherence

Previous

- Students used place value understanding to round multi-digit whole numbers to any place. (Grade 4)
- Students applied their understanding of decimals to compare decimals. (Unit 3)

Now

- Students use place value understanding to round decimals to any place.

Next

- Students add and subtract decimals. (Unit 4)

Rigor

Conceptual Understanding

- Students learn that rounding decimals can make them easier to understand and use to solve problems.

Procedural Skill & Fluency

- Students build proficiency with rounding decimals using a place value.

Application

- Students apply their understanding of rounding decimals based on real-world contexts.

Application is not a targeted element of rigor for this standard.



Number Routine

Find the Pattern, Make a Pattern

5–7 min

Build Fluency

Students build number sense as they determine the pattern and find missing terms. Students then create a new sequence that follows the pattern but uses different numbers.

These prompts encourage students to talk about their reasoning:

- *How do you know your pattern works?*
- *How did you choose your numbers for the new pattern?*
- *Will other numbers fit into this pattern? Explain.*

Purpose Students share thoughts on estimated cost of popcorn.

Notice & Wonder™

- What do you notice?
- What do you wonder?

Teaching Tip You may want to encourage other students to repeat other’s ideas by asking *Can you repeat what they just said in your own words?*

Pose Purposeful Questions

The questions that follow are not intended to be asked in the sequence presented. They are meant to help advance students’ thinking about how to round decimal numbers and are based on possible comments and questions students may make during the share out.

- Why do you think they are using the word *about*?
- What do you think the cost of the popcorn might be?

Math is... Mindset

- What was challenging for you? What have you enjoyed?

Responsible Decision-Making: Reflection

After working through the Notice & Wonder routine, allow students time to thoughtfully reflect on their work. Invite them to think about what may have been challenging as well as the ways in which they were successful and why. Encourage students to also consider what parts of the Notice & Wonder routine that they enjoyed and why.

Transition to Explore & Develop

Ask questions that focus students’ attention on thinking about how to round decimal numbers.

Establish Goals to Focus Learning

- Let’s think about how to round decimal numbers.



Learn
Maya and her sister want to buy a medium popcorn.
How far must they walk to get a good estimate?

You can round decimals to get a good estimate.

One Way Use a number line.
Round to the ones.

The bag of popcorn costs about \$5.00.

Another Way Use place value.
Round to the ones. $5.45 \rightarrow 5$
Round to the tenths. $5.45 \rightarrow 5.5$

Rounding to the nearest whole gives a better estimate.
Maya and her sister need about \$5.00 to buy a medium popcorn.

You can round decimals using number lines to make reasonable estimates. Think about how close the estimate will be to the actual number to which you are rounding.

Work Together
What is the weight of the pumpkin rounded to the nearest whole number? Explain your answer.
 8.6 , 8.5

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1 Pose the Problem

1.1 Pose Purposeful Questions

- How have you rounded whole numbers in the past?
- Based on what you know, can you make a conjecture about how to round decimal numbers? Explain how you would do it and why you think it would work.
- What tools do you think would help you round decimal numbers? Explain why you think they would help.

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Co-Craft Questions and Problems

Have pairs co-create a problem similar to the one on the student page. Have them work together to solve their problem and then trade their problem with another pair.

3 Bring It Together

3.1 Elicit Evidence of Student Thinking

- How is rounding decimals based on place value the same as rounding whole numbers based on place value?

Key Takeaway

- Rounding decimals to any place follows the same process as rounding multi-digit numbers.

Work Together

Students round a decimal number to the ones and tenths places. Students can work on the activity in pairs before sharing their work.

Common Misconception Students may use front-end estimation to round to the nearest one by ignoring the decimal part of 8.62 and finding 8. That is a reasonable estimate, but it is not the process of rounding.

3.2 Language of Math

Estimate and *round* are two different things. An estimate is a reasonable guess. Estimates of the weight of an 18.62 pound pumpkin could be *about 18 pounds* (front-end), *about 19 pounds* (rounding to the ones place), or *about 20 pounds* (rounding to the tens place). Even *about 15 pounds* is a reasonable estimate. Rounding is a very specific process. 18.62 rounded to the nearest whole number is exactly 19.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students look for patterns when rounding decimals.

Material: *Number Cards 0–10* Teaching Resource

Directions: Using only the digits 0–9, each student selects one card to create a decimal number between 4 and 5. Students will sort their decimals into two categories; decimals that are closer to 4 and decimals that are closer to 5.

Implement Tasks that Support Reasoning and Problem Solving

- What strategies did you use to determine whether your decimal number was closer to 4 or closer to 5? Will it always work?
- What generalizations can you make about decimal numbers that are closer to 4 than to 5?
- How can you use your generalizations to write rules for rounding decimals?

Math is... Precision

- What language can you use to explain your generalizations to others?

Students are thinking about precise language when explaining their reasoning.

Activity Debrief: Have students look for patterns of decimals that are closer to 4 and decimals that are closer to 5. Discuss methods for rounding decimals.

Have students revisit the Pose the Problem question and discuss answers.

- About how much money do they need?

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students extend their understanding of rounding whole numbers using place value to decimal numbers.

Facilitate Meaningful Discourse

- **Think About It:** What are some tools and strategies you use to help round whole numbers?
- **Think About It:** What if the price of the medium popcorn was \$5.65, would you round to \$5.00 or \$6.00?
- **Think About It:** Is \$5.50 a useful estimate?

Have students explain why \$5.00 is a good estimate, even though it is not useful for this problem.

Math is... Precision

- What do you notice about the estimate when rounding to lesser place value positions?

Students are thinking about the degree of precision appropriate for a problem context.



English Learner Scaffolds

Entering/Emerging Support students in their comprehension of the word *about* as it is used when estimating. Put \$4.65 on the table. Say, *I'm going to give an estimate. This is about \$5.00.* Then count the money. Say *This is \$4.65. That's close to, or about, \$5.00.* Repeat the task again with a new amount, giving both the estimated amount using the word *about*, and the actual amount. Ask students, *Which number is the estimate?*

Developing/Expanding Support students in their comprehension of the word *about* as it is used in estimating. Put \$4.65 on the table. Say *I'm going to give an estimate. This is about \$5.00.* Then count the money. Say *This is \$4.65. That's close to, or about, \$5.00.* Repeat the task again with a new amount, giving both the estimated amount using the word *about*, and the actual amount. Ask students which number is the estimate and to explain how they know. Provide sentence frames to students who need more prompting or support.

Bridging/Reaching To support students in using the word *about* when expressing an estimate. Ask students to talk about similar-meaning words that they may have already learned in the past that are appropriate for both math and everyday language. Examples may include *approximately*, *not exactly*, *close to*, and *around*.

On My Own

Name _____

What is each decimal rounded to the nearest whole number? You can use a number line or place value.

1. 75.33 → **75** 2. 437.4 → _____

3. 22.7 → **23** 4. 15.91 → _____

What is each decimal rounded to the nearest tenth? You can use a number line or place value.

5. 42.85 → **42.9** 6. 245.27 → _____

7. 82.1 → **82.1** 8. 101.1 → **101.2**

9. Darin rounded a number to the nearest cent to get \$4.2. What number could she have rounded to get the answer?
Sample answer: 4.25

10. Which statements are true?

A. The decimal 432.75 rounded to the nearest tenth is 433.

B. The decimal 432.75 rounded to the nearest cent is 432.75.

C. The decimal 432.75 rounded to the nearest cent is 432.76.

D. The decimal 432.75 rounded to the nearest tenth is 433.0.

Lesson 2 • Rounding and Number Relationships 49

11. The breed of two different dogs are shown. Round each name to the nearest whole number.

33.25; 27.36; 27

12. **STEM Connection:** The area of the red table is about 20.89 ft² of the living room table system. What is 20.89 rounded to the nearest tenth?
20.9

13. Which of the following numbers are closer to 100 than to 90?

93.01, 92.57, 95.44, 95.77, 95.51

93.01, 95.72 are closer to 100; 92.57, 94.05, 94.98, 95.27 are closer to 90.

14. **Extend Your Thinking:** The price of a pair of jeans is rounded to the nearest cent is \$3.00. Between what two amounts could the actual price be?
Between \$2.50 and \$3.49

Answer

How is rounding a number similar to rounding a decimal number?
Answers may vary.

Math is... *Replay!*

Take the lesson Replay or go to [www.illustrativemathematics.org](#) for more practice!

Lesson 2 • Rounding and Number Relationships 49

Practice

Build Fluency from Understanding

Common Error: Exercises 5–8 Students may incorrectly identify the range in which the decimal numbers fall on a number line. Writing the decimal in expanded form and focusing on the value of the digit in the tenths place can help students identify the lesser end point of the range.

Item Analysis

Item	DOK	Rigor
1–8	2	Procedural Skill & Fluency
9–10	3	Conceptual Understanding
11–12	3	Application
13	3	Conceptual Understanding
14	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How is rounding decimals similar to rounding whole numbers?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What have you done well today? What did you do that helped you?

Students reflect on how they practiced responsible decision-making.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use rounding strategies to round decimals.
- I can explain how to apply rounding strategies to decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1–2	1	Round decimals	5.NBT.A.4
3	2	Round decimals	5.NBT.A.4
4–7	2	Round decimals	5.NBT.A.4
8	2	Round decimals	5.NBT.A.4

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

8 of 8 Additional Practice or any of the **U** or **F** activities

7 of 8 *Take Another Look* or any of the **U** activities

6 or fewer of 8 Small Group Intervention or any of the **U** activities

Key for Differentiation

U Reinforce Understanding

F Build Proficiency

F Extend Thinking



Lesson 3-5
Exit Ticket

Name: _____

What is the rounded decimal?

- 0.844 rounded to the nearest tenth is **0.8**.
- 0.844 rounded to the nearest hundredth is **0.84**.
- Do the decimals round to 0.0 when rounded to the nearest tenth? **Circle Yes or No.**

	Yes	No
0.000	✔	
0.001		✔
0.002		✔
0.003	✔	
0.004	✔	

What is the decimal rounded to the nearest whole number?

- 0.02 rounds to **0**.
- 0.002 rounds to **0**.
- 1.84 rounds to **2**.
- 0.025 rounds to **0**.

8. Rounded to the nearest dollar, one quart costs \$4.00 at the store. How much more does the other quart cost? (Circle all that apply.)

\$11.00
 \$11.04
 \$4.00
 \$14.00

Reflect On Your Learning

On a scale of 1 to 4, how confident are you about your understanding of this concept?

1 2 3 4

1 2 3 4

1 2 3 4

1 2 3 4

Lesson Review 3-5

R Reinforce Understanding

SMALL GROUP

On a Roll!

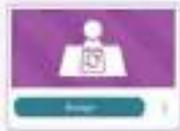
Work with students in pairs. Have students roll a number cube three times to create a number. The first digit rolled goes in the ones place, the second digit goes in the tenths place, and the third digit goes in the hundredths place. Have students round the number to the nearest whole number and to the nearest tenth. Make sure students recognize that the process for rounding decimals is the same as the process for rounding whole numbers. Repeat for other rolls.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Round Decimals to Nearest Whole > 1
- Round Decimals to Nearest Tenth > 1
- Round Decimals to Nearest Hundredth



INDEPENDENT WORK

Differentiation Resource Book, p. 19

Lesson 26 • Reinforce Understanding
Use Place Value to Round Decimals

Name _____

Review

When rounding decimals, look to the number that is to the right of the place you are rounding. Round 5.842 to the nearest tenth.

5.842

500ths The 4 rounds the number down to 5.8.

Round to the nearest tenth, look at the hundredths place.
 The number of hundredths is 4, so round down to 5.8.

Complete each mathematical statement.

- When rounding to the nearest whole number, look to the number in the **tenths** place.
- When rounding to the nearest hundredth, look to the number in the **thousandths** place.

Round the numbers to the nearest whole number.

3. 7.66 **8** 4. 0.75 **1**

Round the numbers to the nearest tenth.

5. 16.75 **16.8** 6. 89.12 **89.1**

Round the numbers to the nearest hundredth.

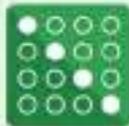
7. 1.45 **1.50** 8. 2.21 **2.21**

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Rounding Decimals Four in a Row
 Students practice rounding decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 19–20

Lesson 26
Additional Practice

Name _____

Review

You can round decimals.

Mary has 10.75 feet of yarn. Round the length of the yarn to the nearest tenth.

10.75 feet rounds to the nearest tenth: 10.8 feet.

10.75

10.8

10.7

1. Round each decimal to the nearest whole number.

a. 2.84 **3** b. 20.71 **21**
 c. 4.75 **5** d. 88.7 **89**
 e. 3.01 **3** f. 10.67 **11**
 g. 11.48 **11** h. 60.71 **61**
 i. 22.67 **23** j. 75.81 **76**
 k. 18.87 **19** l. 90.57 **91**

2. Round each decimal to the given place value.

a. Round 15.27 to the nearest tenth: **15.3**
 b. Round 4.57 to the nearest hundredth: **4.57**
 c. Round 78.22 to the nearest tenth: **78.2**
 d. Round 4.57 to the nearest hundredth: **4.57**
 e. Round 11.58 to the nearest tenth: **11.6**

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting within 1,000,000.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 19–20

1. Round each number to the given place.

a. 241	ones	<u>241</u>
	hundreds	<u>200</u>
b. 72,076	tens	<u>72,076</u>
	hundreds	<u>72,100</u>
c. 89,882	ones	<u>89,882</u>
	tens	<u>89,880</u>
d. 74,645	ones	<u>74,645</u>
	hundreds	<u>74,600</u>

4. A puppy weighs 16.41 pounds. Write the weight, about four more than the puppy weight.
20.5 pounds

6. On a map that 30,294 rounded to the nearest hundredth is 30.29. Do you agree? Explain.
No. Sample answer: I disagree because 30.294 rounded to the nearest hundredth is 30.29.

8. There is a \$78.65 in a checking account. The account holder is interested in the nearest whole dollar. Betty says that is about \$79 and says that \$78.65 is closer to \$79 than \$78. Do you agree? Explain.
No. Sample answer: Since \$78.65 is closer to \$79 than to \$78, the amount rounded to the nearest whole dollar is \$79.

Math at Home Activity

Read the instructions and complete the activity with a partner. Use the information in the Student Practice Book to help you. You may use a calculator for this activity. Write your answers on a separate sheet of paper. Do not write on this page.

Student Practice Book

Extend Thinking

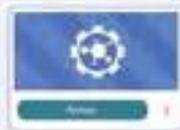
Use It! Application Station

State Sales Tax Student investigate and compare state sales tax rates.



STEM Activity

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 20

Lesson 3-5 • Extend Thinking

Use Place Value to Round Decimals

Notes:

Quentin gives \$32.079 to buy some fruit. Approximate. (Rounded to the Nearest) Round each to the nearest whole dollar. \$32.32 to the Nearest Whole is \$32. How much more do you need?

1. What number is the rounded price number, which city did Quentin take the greater distance? **They are the same.**
2. What number is the rounded price number, which city did Quentin take the greater distance? **\$32.32**
3. Round the distance Quentin traveled on the first day to the nearest tenth. **632.1**
4. Round the distance Quentin traveled on the second day to the nearest hundredth. **632.07**
5. Which number is greater? **632.1**
6. Write the distance Quentin traveled on the first day and rounded to \$32.079, what is a possible distance for each measurement on the day?
Sample answer: 632.079 (any number that is less than 632.0745 and equal to or greater than 632.0739)
7. Write the distance Quentin traveled on the second day and rounded to 632.32, what is a possible distance for each measurement on the day?
Sample answer: 632.324 (any number that is less than 632.325 and equal to or greater than 632.319)

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Unit Review

Vocabulary Review

Choose the correct words to complete each sentence.

decimal tenth
place value place value
hundredths hundredths

- A **decimal point** is a point that separates the ones and the tenths in a decimal number.
- Tenths** is a place value position. It represents $\frac{1}{10}$ of a whole.
- Hundredths** is a place value position. It represents $\frac{1}{100}$ of a whole.
- The value given to a digit by its position is called **place value**.
- A number that has a digit in the tenths place, hundredths place, and beyond is called a **decimal**.
- Tenths** is a place value position. It represents $\frac{1}{10}$ of a whole.

Review

- Which statement correctly compares values of the digit 8 in 284,568 and 128,777?
 - The value of the digit 8 in 284,568 is $\frac{1}{10}$ the value of the digit 8 in 128,777.
 - The value of the digit 8 in 284,568 is 10 times the value of the digit 8 in 128,777.
 - The value of the digit 8 in 284,568 is 100 times the value of the digit 8 in 128,777.
- Complete the sentence. $356,814$ is rounded from the number thirty-six thousand, eight hundred and **14**.
- Classmate whether each comparison is true or false.

Comparison	True	False
$555 < 555$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$1,000 > 999$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$1,000 < 1,000$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$1,000 > 1,001$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
$1,000 < 1,000$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$1,000 > 1,000$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
- Compare each number.

3,127 rounded to the nearest hundredth is **3.13**.

8,727 rounded to the nearest tenth is **8.7**.
- Use the number line to round 84 when rounded to the nearest ten.

	Ten	One	Two
700			<input checked="" type="checkbox"/>
800			<input checked="" type="checkbox"/>
900	<input checked="" type="checkbox"/>		
1,000			<input checked="" type="checkbox"/>
1,100			<input checked="" type="checkbox"/>
- Use the number line to round 25 when rounded to the nearest ten.

	Ten	One	Two
200			<input checked="" type="checkbox"/>
250			<input checked="" type="checkbox"/>
300	<input checked="" type="checkbox"/>		
350			<input checked="" type="checkbox"/>
400			<input checked="" type="checkbox"/>

Students can complete the **Unit Review** to prepare for the **Unit Assessment**. Students may complete the Review in their Interactive eBook in the Digital Student Center.

Vocabulary Review

Item Analysis

Item	Lesson
1	3-2
2	3-2
3	3-2
4	3-1
5	3-2
6	3-2

Review

Item Analysis

Item	DOK	Lesson	Standard
7	2	3-1	5.NBT.A.1
8	2	3-3	5.NBT.A.3.a
9	2	3-4	5.NBT.A.3.b
10	2	3-5	5.NBT.A.4
11	2	3-5	5.NBT.A.4
12	2	3-4	5.NBT.A.3.b

To review the lessons in this unit, have students watch the Math Replay video in their Digital Student Center.

Assign the Unit Review practice to students from the Digital Teacher Center.



Item Analysis (continued)

Item	DOK	Lesson	Standard
13	2	3-2	5.NBT.A.1
14	2	3-2	5.NBT.A.1
15	2	3-2	5.NBT.A.1
16	2	3-3	5.NBT.A.3.a
17	2	3-3	5.NBT.A.3.a
18	2	3-3	5.NBT.A.3.a
19	2	3-5	5.NBT.A.4
20	2	3-3	5.NBT.A.3.a

Performance Task

Standards: 5.NBT.A.3.a; 5.NBT.A.3.b

Rubric (4 points)

Part A – 2 points

- 2 POINTS** Student's work reflects a proficiency in reading and writing decimals. The student can write a number in word and expanded form.
- 1 POINT** Student's work reflects developing proficiency in reading and writing decimals. The student can write a number in either word or expanded form.
- 0 POINTS** Student's work reflects a poor understanding in reading and writing decimals. The student cannot write a number in word or expanded form.

Part B – 2 points

- 2 POINTS** Student's work reflects a proficiency in comparing decimals. The student's solution is accurate and can explain their answer.
- 1 POINT** Student's work reflects developing proficiency in comparing decimals. The student's solution may be accurate but may not be able to explain their answer.
- 0 POINTS** Student's work reflects a weak understanding of comparing decimals. The student's solution is inaccurate, and they are not able to explain their answer.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

18. Write the decimal number in standard form: $4 \times \frac{1}{10} + 9 \times \frac{1}{100} + 0.009$

19. Write the decimal number in standard form: $4 \times \frac{1}{10} + 9 \times \frac{1}{100} + 0.009$

20. Write the decimal number in standard form: $4 \times \frac{1}{10} + 9 \times \frac{1}{100} + 0.009$

17. Why is 4,218 in scientific notation?

16. Why is 4,218 in scientific notation?

15. Forty five and two hundred fifty nine thousandths

Sample answer: 45.259

Performance Task

There are eight planets in our solar system. Each planet orbits the sun at different speeds. Earth orbits the sun once every 365.25 days. Use $>$, $<$, or $=$ to compare the orbit speeds. Explain your answer.

Planet	Orbital Period (Days)	Orbit Speed (mi/hr)	Orbit Speed (mi/hr)
Earth	365.25	67,000	$67,000 + 1 + 0.00 = 67,001$
Jupiter	4,333	49,000	$49,000 + 9 + 0.6 = 49,009.6$

18.15. Jupiter orbits the sun once every 4,333 days. Use $>$, $<$, or $=$ to compare the orbit speeds. Explain your answer.

Sample answer: $67,001$ is greater than $49,009.6$.

Default

System has either not been pre-processed by readability, or the readability score is too low.

Answers may vary.

Unit 3
Fluency Practice

Name _____

Fluency Strategy

You can use an **algorithm** to add. Add the digits in the same place value. Add hundreds, tens, hundreds, and tens.

Subtract 0 is necessary to borrow.

$$\begin{array}{r} 244 \\ + 127 \\ \hline 371 \end{array}$$

$$\begin{array}{r} 200 \\ + 200 \\ \hline 400 \end{array}$$

Fluency Flash

What is the sum?

1.

3	9	0	2
4	1	9	0
7	9	9	2

2.

9	9	2	0
1	2	6	0
7	0	9	0

Unit 3 • Practice with Number Relationships 48

Fluency Check

What is the sum or difference?

1. $1,237 + 238 =$ **1,475**

2. $239 + 345 =$ **584**

3. $197 + 402 =$ **599**

4. $2,345 + 243 =$ **2,588**

5. $409 - 045 =$ **364**

6. $20 + 632 =$ **652**

7. $10,897 + 4,999 =$ **15,896**

8. $4,898 + 1,079 =$ **5,977**

9. $81,000 + 21,668 =$ **102,668**

10. $192 + 294 =$ **486**

Fluency Talk

8 points to a float base (see Know/You/Need to Know) when adding using an algorithm.

Answers may vary.

How is adding using partial sums similar to adding using an algorithm?

Answers may vary.

Unit 3 • Practice with Number Relationships 49

Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students practice using an algorithm to add.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Performance Task

A Trip to the Movies

Student draw on their understanding of decimal place value and number relationships. Use the rubric shown to evaluate students' work.

Standards 5.NBT.A.1, 5.NBT.A.3.a, 5.NBT.A.3.b, 5.NBT.A.4

Rubric (10 points)

Part A (DOK 2) – 2 points

- 2 POINTS** Student's explanation reflects a proficiency with understanding rounding in context.
- 1 POINT** Student's explanation reflects developing proficiency with understanding rounding products in context.
- 0 POINTS** Student's explanation reflects a poor understanding of rounding products in context.

Part B (DOK 3) – 2 points

- 2 POINTS** Student's work shows proficiency in extending place value to decimals. The student's explanation is reasonable.
- 1 POINT** Student's work shows developing proficiency in extending place value to decimals. The student's explanation is reasonable.
- 0 POINTS** Student's work shows weak proficiency in extending place value to decimals. The student's explanation is incorrect.

Part C (DOK 2) – 2 points

- 2 POINTS** Student's work identifies correct range of place values for rounding decimals. The student's explanation is reasonable.
- 1 POINT** Student either identifies correct range of place values for rounding decimals or has a reasonable explanation.
- 0 POINTS** Student does not identify the correct range of place values for rounding decimals. The student's explanation is not reasonable.

Part D (DOK 2) – 2 points

- 2 POINTS** Student's work shows proficiency in generalizing place value. The student's explanation is reasonable.
- 1 POINT** Student's work shows developing proficiency in generalizing place value. The student's explanation is reasonable.
- 0 POINTS** Student's work shows weak proficiency in generalizing place value. The student's explanation is incorrect.

Part E (DOK 4) – 2 points

- 2 POINTS** Student's explanation shows proficiency in generalizing place value.
- 1 POINT** Student's explanation shows developing proficiency in generalizing place value.
- 0 POINTS** Student's explanation does not show proficiency in generalizing place value.

Unit 3
Performance Task

Name _____

A Trip to the Movies
Jackson and Frank go to the movies before finding a seat. Their budget for the movie is \$100.

Part A
Jackson estimates a large drink costs about \$5. The actual price is \$6.75. Jackson estimates a medium drink costs about \$4.50. The actual price is \$5.25. Jackson estimates a small drink costs about \$3.50. The actual price is \$4.25. Jackson estimates a large popcorn costs about \$10. The actual price is \$12.50. Jackson estimates a medium popcorn costs about \$7.50. The actual price is \$8.75. Jackson estimates a small popcorn costs about \$5.50. The actual price is \$6.25. Jackson estimates a large candy costs about \$5. The actual price is \$6.25. Jackson estimates a medium candy costs about \$3.50. The actual price is \$4.25. Jackson estimates a small candy costs about \$2.50. The actual price is \$3.25. Jackson estimates a large ice cream costs about \$5. The actual price is \$6.25. Jackson estimates a medium ice cream costs about \$3.50. The actual price is \$4.25. Jackson estimates a small ice cream costs about \$2.50. The actual price is \$3.25. Jackson estimates a large drink costs about \$5. The actual price is \$6.75. Jackson estimates a medium drink costs about \$4.50. The actual price is \$5.25. Jackson estimates a small drink costs about \$3.50. The actual price is \$4.25. Jackson estimates a large popcorn costs about \$10. The actual price is \$12.50. Jackson estimates a medium popcorn costs about \$7.50. The actual price is \$8.75. Jackson estimates a small popcorn costs about \$5.50. The actual price is \$6.25. Jackson estimates a large candy costs about \$5. The actual price is \$6.25. Jackson estimates a medium candy costs about \$3.50. The actual price is \$4.25. Jackson estimates a small candy costs about \$2.50. The actual price is \$3.25. Jackson estimates a large ice cream costs about \$5. The actual price is \$6.25. Jackson estimates a medium ice cream costs about \$3.50. The actual price is \$4.25. Jackson estimates a small ice cream costs about \$2.50. The actual price is \$3.25.

Sample answer: No because \$5 would not be enough to purchase a large drink. \$6 would leave them a maximum reasonable guess in this instance, as it would be more than enough.

Part B
Jackson pays \$3.75 for his snack, while Frank pays \$4.50. There are two different ways to describe the relationship between the values of the digit 7 in each number. Explain your answer.

Sample answer: The 7 in the tenths place of \$3.75 is $\frac{1}{10}$ the value of the 7 in the ones place of \$4.50. The 7 in the ones place of \$3.75 is 10 times the value of 7 in the tenths place of \$3.75.

Part C
Jackson and Frank paid \$10 combined and the tickets cost \$11.50 each. Did Jackson and Frank have enough money for their snacks? Write a number line showing all the ways to explain your answer.

Sample answer: After rounding, they will spend at \$10 on tickets and will not have enough money left to purchase snacks.

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Part D
Last week, the movie theater sold 1,234 tickets. This week, the movie theater sold 1,234 tickets. When comparing sales, it was found that the sales for this week were 1,234 more than the sales for last week. Why is it not necessary to compare the digits in the ones place? Explain your answer.

Sample answer: The values in the respective thousand's places of the 1,234 are the same.

Part E
Jackson's and Frank's book codes each have a five-digit code. Jackson's five-digit code has the first digit 9 in the thousands place and the last digit 6 in the ones place. Frank's code has a value of 90,000. Explain how you know that the value of the digit 9 in Jackson's code is less than the value of the digit 9 in Frank's code. Write an example of a five-digit number that has the thousands digit 9 and the ones digit 6. Explain how you know that the value of the digit 9 in your number is greater than the value of the digit 6 in your number.

Sample answer: Jackson - 90,006, Frank - 92,006. A fully correct response will be any five-digit number with the underlined digits in the given places. The value of the digit 9 in Frank's code is greater than any possible given digit that could be used in the ten thousands place of Jackson's code. So, Frank's code is greater.

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Unit Assessment

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

Data When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support Intervention Lesson	Standard
1	2	1	Digits to the Left and Right	5.NBT.A.1
2	1	3	Standard & Word Form (Large Numbers)	5.NBT.A.3.a
3	2	1	Digits to the Left and Right	5.NBT.A.1
4	2	2	One-Tenth & 10 Times as Much	5.NBT.A.1
5	2	4	Compare Decimal Numbers (1,000ths)	5.NBT.A.3.b
6	2	2	One-Tenth & 10 Times as Much	5.NBT.A.1
7	2	3	Expanded Form of Decimal Powers of Ten	5.NBT.A.3.a
8	2	5	Round Decimals to Nearest Tenth > 15.NBT.A.4	
9	1	3	Standard & Word Form (Large Numbers)	5.NBT.A.3.a
10	3	4	Compare Decimal Numbers (100ths)	5.NBT.A.3.b
11–12	2	5	Round Decimals to Any Place	5.NBT.A.4
13	1	3	Standard & Word Form (Large Numbers)	5.NBT.A.3.a
14	3	5	Round Decimals to Nearest Whole > 1	5.NBT.A.4
15	3	5	Round Decimals to Nearest Tenth > 15.NBT.A.4	



Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 3
Unit Assessment, Form A

Name: _____

1. Which statement about the digits in the number 25,350 is true?

A. The value of the digit 5 in the thousands place is 5,000. The value of the digit 5 in the hundreds place is 500.

B. The value of the digit 5 in the thousands place is $\frac{1}{10}$ the value of the digit 5 in the hundreds place.

C. The value of the digit 5 in the thousands place is 100 times the value of the digit 5 in the hundreds place.

D. The value of the digit 5 in the thousands place has the same value as the digit 5 in the hundreds place.

2. How can you write the number in standard form?
In standard form, the number nine hundred thousand fifty-two is written **902,051**.

3. Look at the digit 7 in the number shown in the place value chart.

Standard Form	Ten Thousands	Thousands	Hundreds	Tens	Ones
7	3	7	2	1	4
7	0	1	3	8	

Which statement is true? Choose all that apply.

A. $7,000 = \frac{1}{10}$ of 70,000

B. 20,000 is 10 times 2,000

C. $7,000 = \frac{1}{10}$ of 70,000

D. $20,000 = \frac{1}{10}$ of 200,000

E. $2,000 = 10$ times 200

4. Use the place value chart to complete the statement.

Ten Thousands	Thousands	Hundreds	Tens	Ones	Tenths	Hundredths
4	6	5	8	5	6	1

The value of the digit 5 in the hundreds place is $\frac{1}{10}$ the value of the digit 5 in the _____ place.

A. ones B. tens C. hundredths

5. Is each comparison true or false?

	True	False
$372 < 0.37$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$3,800^2 > 3,800$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
$3,288 < 0.06$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$0.01 < 0.001$	<input checked="" type="checkbox"/>	<input type="checkbox"/>
$0.002 < 0.001$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
$0.28 < 0.008$	<input checked="" type="checkbox"/>	<input type="checkbox"/>

6. A centimeter is 0.01 meter. A millimeter is 0.001 meter.
How does the length of 1 centimeter compare to the length of 1 millimeter? Explain your answer.
1 centimeter is 10 times the length of 1 millimeter. Simple answer: The digit 1 in 0.01 is ten times the value of the digit 1 in 0.001. So 1 centimeter is 10 times the length of 1 millimeter.

7. What is the expanded form of 412,631?

A. $400 + 10 + \frac{7}{100} + \frac{3}{1,000}$

B. $400 + 10 + \frac{7}{100} + \frac{3}{10}$

C. $400 + 2 + \frac{7}{100} + \frac{3}{1,000}$

D. $400 + 10 + \frac{7}{100} + \frac{3}{1,000}$

80 Assessment Resource Book

Add and Subtract Decimals

PACING: 14 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  How Far?	Estimate the width of the classroom using the number of steps.		
4-1 Estimate Sums and Differences of Decimals	Students estimate decimal sums and differences using the same strategies used with whole number sums and differences.	Students discuss estimating sums and differences of decimals while answering <i>Wh-</i> questions and using the verb <i>rounding</i> .	Students set a focused mathematical goal and make a plan for achieving that goal.
Math Probe Estimating Decimal Sums and Differences	Use estimation to determine if the sum of two decimal numbers is greater than or less than a benchmark number.		
4-2 Represent Addition of Decimals	Students use decimal grids to represent addition of decimals with the same number of decimal places.	Students discuss using decimal grids to represent addition of decimals while answering <i>Wh-</i> and Yes/No questions.	Students identify and discuss the emotions experienced during math learning.
4-3 Represent Addition of Tenths and Hundredths	Students use decimal grids to represent addition of decimals with different numbers of decimal places.	Students discuss using decimal grids to add decimals while answering <i>Wh-</i> questions and using the adjective <i>similar</i> .	Students collaborate with peers to complete a mathematical task and offer constructive feedback to the idea posed by others.
4-4 Use Partial Sums to Add Decimals	Students use addition strategies they know, such as partial sums, to add decimals.	Students discuss addition strategies, such as partial sums, to add decimals while answering <i>Wh-</i> questions.	Students recognize and work to understand the emotions of others and practice empathetic responses.
4-5 Represent Subtraction of Decimals	Students use decimal grids to represent subtraction of decimals with the same number of decimal places.	Students explain how to use decimal grids to represent subtraction of decimals while answering <i>Wh-</i> and using <i>how much</i> .	Students collaborate with peers and contribute to group effort to achieve a collective mathematical goal.
4-6 Represent Subtraction of Tenths and Hundredths	Students use decimal grids to represent subtraction of decimals with different numbers of decimal places.	Students discuss using patterns to solve problems while answering <i>Wh-</i> questions and using <i>longer</i> .	Students break down a situation to identify the problem at hand.
4-7 Strategies to Subtract Decimals	Students can use subtraction strategies they know, such as partial differences, to subtract decimals.	Students discuss using subtraction strategies while answering <i>Wh-</i> and Yes/No questions and using adjectives such as <i>efficient</i> and <i>easier</i> .	Students recognize personal strengths through thoughtful self-reflection.
4-8 Explain Strategies to Add and Subtract Decimals	Students can explain their choice of strategy to solve.	Students discuss their choice of strategy to solve a problem while answering <i>Wh-</i> questions and using the adjective <i>efficient</i> .	Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing feedback.
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION: How do I add and subtract decimals?

LESSON	KEY VOCABULARY		MATERIALS TO GATHER	RIGOR FOCUS	STANDARD	
4-1	Math Terms	Academic Terms	<ul style="list-style-type: none"> • <i>Decimal Cards</i> Teaching Resource 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7	
	decimal estimate	analyze infer reasonable				
Math Probe						
4-2	decimal grid hundredths tenths	benefit drawback evaluate	<ul style="list-style-type: none"> • number cube • <i>Tenths and Hundredths</i> Teaching Resource 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7	
4-3	decimal grid	debate infer	<ul style="list-style-type: none"> • base-ten blocks • decimal grid • 10×10 Teaching Resource 	<ul style="list-style-type: none"> • index cards 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7
4-4	decompose partial sums	emphasize procedure	<ul style="list-style-type: none"> • <i>Decimal Cards</i> Teaching Resource 		Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7
4-5	decimal grid	assert prove	<ul style="list-style-type: none"> • <i>Blank Number Lines</i> Teaching Resource • number cubes 	<ul style="list-style-type: none"> • <i>Tenths and Hundredths</i> Teaching Resource 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7
4-6	decimal grid	accurate evaluate	<ul style="list-style-type: none"> • <i>Decimal Grids</i> Teaching Resource 	<ul style="list-style-type: none"> • 10×10 Teaching Resource 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7
4-7	decompose	analyze prove	<ul style="list-style-type: none"> • <i>Blank Open Number Lines</i> Teaching Resource 	<ul style="list-style-type: none"> • <i>Decimal Cards</i> Teaching Resource 	Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7
4-8	decomposition partial sums	evaluate procedure	<ul style="list-style-type: none"> • <i>Explain and Show Your Strategies</i> Teaching Resource 		Conceptual Understanding Procedural Skill & Fluency	5.NBT.B.7

Unit Overview

Focus

Adding and Subtracting Decimals

As students approach learning to add and subtract decimals, they are equipped with the understanding of whole-number operations and decimal place value. They have experience with using number lines, grids, and other visual representations to help them add and subtract. Students build on this prior knowledge as they develop strategies for adding and subtracting decimals.

The explorations with multiple representations provide students opportunities to visualize and internalize how decimals behave during addition and subtraction. This allows for a much deeper understanding than merely memorizing and applying algorithms.

Students estimate sums and differences by using rounded numbers and compatible numbers. Estimation strategies are taught prior to finding exact results so that students have tools to use to check for reasonableness.

Students learn to find exact sums and differences using multiple representations including tenths and hundredths grids and number lines. Students also learn how to decompose decimals to perform operations on their parts.

Allow students plenty of time to explore the strategies in each lesson. When they ultimately use the standard algorithm for each decimal operation, this learning will give them a foundation of deeper understanding.

Coherence

What Students Have Learned

• Add and Subtract Whole Numbers

Students fluently added and subtracted multi-digit whole numbers using the standard algorithm. (Grade 4)

• Understand Decimal Place Value

Students extended place-value understanding to decimals. (Grade 5, Unit 3)

What Students Are Learning

• Estimate Sums and Differences of Decimals

Students use and describe place-value strategies to estimate sums and differences of decimals.

• Use Representations to Add and Subtract Decimals

Students use representations including decimal grids and number lines to add and subtract decimals.

• Use Strategies to Add and Subtract Decimals

Students use strategies including decomposition, partial sums, and partial differences to add and subtract decimals.

What Students Will Learn

• Multiply Multi-Digit Whole Numbers

Students will fluently multiply multi-digit whole numbers. (Grade 5, Unit 5)

• Add, Subtract, Multiply, and Divide Multi-Digit Decimals

Students will fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation. (Grade 6)

Rigor

Conceptual Understanding

Students develop understanding of:

- using place-value understanding to estimate sums and differences of decimals;
- using representations to add and subtract decimals;
- using strategies to add and subtract decimals.

Procedural Skill and Fluency

Students build proficiency with:

- procedures for estimating sums and differences of decimals;
- adding and subtracting decimals.

Application

Students apply their knowledge of:

- estimating sums and differences of decimals to solve problems with real-world contexts;
- adding and subtracting decimals to solve problems with real-world contexts;

Application is not a targeted element of rigor for the standards in this unit.

Effective Teaching Practices

Build Procedural Fluency from Conceptual Understanding

It can be tempting to revert to reliance upon memorization of rules and rigid application of those rules. After all, many students have been taught to “line up the decimal points and add or subtract as usual” and succeeded in their math classes.

Students will, however, develop greater fluency and more transferrable skills and understanding when they are allowed and encouraged to explore concepts on a deeper level.

In the early grades, children learn to count, add, and subtract whole numbers by using concrete representations.

Teachers would not expect, for example, for children to learn $2 + 3 = 5$ as a purely abstract concept. Instead, children are presented with a group of two objects and a group of three objects—and are then allowed to count the five objects. Only after this concrete understanding has been established are children guided toward using only the numerical representation of addition within 5.

In the same way, when students work with decimals or fractions, they should be encouraged to explore the fractional parts represented by the numerals and how those parts are taken apart or put together.

When students work with decimals or fractions, too much focus on procedure can lead to lack of conceptual foundation. In contrast, students who focus more on conceptual understanding are often able to articulate procedural explanations based on their own experience. As such, encourage students to use visual representations for decimals whenever possible—even in situations where a problem may be presented with numerals only.

Guide students to continue using estimation for checking their sums and differences, and to maintain their understanding of the magnitude of the numbers they are adding and subtracting. Estimation plays a key role in helping students avoid errors involving place value and the placement of the decimal point.

Math Practices and Processes

Use Appropriate Tools Strategically

This unit provides varied tools and representations to help students understand what is happening when decimals are added and subtracted.

Each student has a unique way of learning and may gravitate toward one or another type of representation or strategy. For example, some students may relate better to decimal grids than to number lines, while others may find it easier to decompose and add than to use a visual representation for each decimal.

Encourage students to gain fluency in using every tool and strategy available to them. Explain that although they may develop preferences, each visual representation may prove valuable—and they will not be able to determine their favorites without experiencing each. In particular, to gain overall fluency, there is value in encouraging students to use tools with which they are *least* comfortable. Students should be encouraged to compare and contrast how each tool shows numbers and operations.

Some suggestions for using tools strategically and choosing appropriate tools include:

- Students work with partners to solve a decimal addition or subtraction problem. Each partner chooses a method and completes the operation. Partners articulate their strategies to one another, including evaluating and comparing tools.
- Students are given a number line that shows a decimal addition or subtraction. Students use the information on the number line to write one or more matching equations.
- Students are given a decimal addition or subtraction problem and are asked to discuss as a class the tools they would choose and explain the reasoning behind their choices.

Social and Emotional Learning

What Skills Will We Develop

- **Self-Management – Goal Setting** (Lesson 4-1): Setting goals can help motivate students to take initiative and stay focused.
- **Self-Awareness – Identify Emotions** (Lesson 4-2): Students who can identify and understand their own feelings and emotions can better manage the reactions to those feelings and emotions.
- **Relationship Skills – Social Engagement** (Lesson 4-3): Engaging with others allows students to develop relationships and establish a sense of security and belonging in the classroom community.
- **Social-Awareness – Empathy** (Lesson 4-4): Students who can empathize with others are more able to build positive relationships.

- **Relationship Skills – Teamwork** (Lesson 4-5): When students work effectively as a team, they establish a stronger learning community.
- **Responsible Decision-Making – Identify Problems** (Lesson 4-6): A key step in problem solving is analyzing information to identify the task.
- **Self-Awareness – Recognize Strengths** (Lesson 4-7): When students recognize their own strengths, they can see themselves as resourceful and may be more willing to attempt to problem solve and help others.
- **Social Awareness – Respect Others** (Lesson 4-8): When students are respectful of one another, they strengthen their class community.

Language of Math

Mathematical Nouns

Students will be using these key terms in this unit:

- **Estimate** (Lesson 4-1): This is a review term, which students should be familiar with. Ask students to explain how they have used estimation in the past to better understand number relationships and to help check if a solution is reasonable.
- **Round** (Lesson 4-1): Students have used this term throughout previous grades. In the context of estimation, students *round* decimals to the nearest whole number. Students should recognize the difference between rounding and using compatible numbers.

- **Decompose addends** (Lesson 4-4) Students should be familiar with decomposing numbers from earlier grades. Remind them of the meaning of *addends* and how decomposing addends can facilitate finding a sum, especially as they apply this strategy to using partial sums in decimal addition.

Math Language Development

A Focus on Estimation Vocabulary

Help students identify the methods and steps they use in estimation.

Ask students to discuss the difference between the words *exact* and *approximation*, and between *determine* and *guess*. Have them use the word *estimate* as a verb in a sentence. Have them use the word *estimate* as a noun and the word *about* in a sentence. Also have them use the words *calculate* and *exactly* in a sentence.

Guide students to articulate that estimating enables us to quickly determine a “ballpark” result that is close to the actual answer. Students should explain why different estimation strategies may produce different estimates that are all reasonable.

Students may be familiar with the expressions *wild guess* and *educated guess*. Explain that estimation involves using a sound strategy to make an educated guess whereas a wild guess generally does not involve a strategy that would produce a reasonable result.

This module includes other terminology that refines students' understanding of estimation.

Students have used the term *benchmark* before. Encourage them to think of benchmarks in concrete terms: markings on a measurement line with which they can compare other numbers.

The terms *round*, *halfway point*, and *target number* should need little explanation, but help students attend to their meaning and use them in sentences when describing an estimation process.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to adding and subtracting decimals. Because many of the words (weight, cost, lengths, farther) and phrases (take up, how far, how much more, the difference) used in this section are likely unfamiliar or unknown, students are supported in understanding and using these words so that the instruction is more accessible.

Lesson 4-1 – *take up*

Lesson 4-2 – *how far*

Lesson 4-3 – *weight, lb.*

Lesson 4-4 – *cost (n)*

Lesson 4-5 – *how much more*

Lesson 4-6 – *lengths*

Lesson 4-7 – *the difference*

Lesson 4-8 – *farther*

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

About How Much?

Purpose: Build estimating skills.

Overview: Students estimate the value of expressions (with operations) shown, explaining their strategies and thinking. The teacher records students' estimates, then reveals the value of the expression. Students analyze the estimates and discuss which are closest to the actual value of the expression.

Would You Rather?

Purpose: Build flexibility with number sense and mental math operations; enhance decision-making.

Overview: Students choose between two options, both of which require mental computation. Students explain their choice and their rationale for their choice.

Which Benchmark Is It Closest To?

Purpose: Enhance rounding and reasoning skills.

Overview: Students determine to which benchmark the given number is closest and explain their reasoning.

Can You Make the Number?

Purpose: Build flexible thinking and efficiency with operations.

Overview: Students use all the given numbers to build expressions with a value matching the target number. Students can use a range of operations in their expressions. The teacher records students' expressions, then facilitates a discussion about students' expressions.

Sense-Making Routines

Notice & Wonder: What do you notice? What do you wonder? (Lessons 4-1, 4-5, 4-6) In Lesson 4-1, students notice and wonder about the relationship between different amounts of data storage on a cell phone. The prompt for Lesson 4-5 has students noticing and wondering about relating pixel art on a decimal grid to decimals. In Lesson 4-6, students notice and wonder about what decimals represent and the similarities and differences between decimals with a different number of decimal places.

Numberless Word Problem (Lessons 4-2, 4-8) In Lesson 4-2, students discuss and share their thoughts about a map and the numbers included on a map. In Lesson 4-8, students think about the strategies and operations they can use to solve the problem.

Notice & Wonder: How are they the same? How are they different? (Lesson 4-3) Students consider the same decimal represented as tenths and as hundredths on grids. The decimal grids give students the opportunity to visualize tenths and hundredths on concrete models before they use the decimal grids to add them in the lesson.

Which Doesn't Belong? (Lessons 4-4, 4-7) In Lesson 4-4, students think about the meaning of decimals and ways to represent decimals. In Lesson 4-7, students look for connections among whole-number addition and subtraction equations.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. For more information on the Math Language Routines, see the Appendix.

- Lesson 4-1 – Students participate in MLR8: Discussion Supports.
- Lesson 4-2 – Students participate in MLR1: Stronger and Clearer Each Time.
- Lesson 4-3 – Students participate in MLR2: Collect and Display.
- Lesson 4-4 – Students participate in MLR7: Compare and Connect.

- Lesson 4-5 – Students participate in MLR4: Information Gap.
- Lesson 4-6 – Students participate in MLR3: Critique, Correct, and Clarify.
- Lesson 4-7 – Students participate in MLR7: Compare and Connect.
- Lesson 4-8 – Students participate in MLR5: Co-Craft Questions and Problems.

170 8
How Ready Am I?

1. Which shows 4.26 expanded form?
 A. $4 + 0.2 + 0.06$ B. $4 + 0.2 + 0.006$
 C. $40 + 4 + 0.2 + 0.06$ D. $40 + 4 + 0.2 + 0.006$

2. Which decimal grid represents 0.26 ?

A.  B. 

C.  D. 

3. The table shows the population of two neighboring cities.

Year	Population
2010	412,784
2015	512,879

What is the total population change?
 A. 100,095 B. 100,094
 C. 100,093 D. 100,092

4. The box office reports that 228 people attended the Friday performance of the school musical. They were 45 fewer people who attended the Saturday performance. How many people attended the Saturday performance?
 A. 183 B. 182
 C. 181 D. 180

Answer Key: 1-4

5. In the number $1,234$, which digit is in the hundreds place?
 A. 1 B. 2 C. 3 D. 4

6. What number is $1,230,000$ when rounded to the nearest ten thousand?
 A. $1,230,000$ B. $1,230,000$
 C. $1,230,000$ D. $1,230,000$

7. Jackson's baseball team earned 12,222 hits in January and 10,000 hits in February. What difference is shown by the total number of hits the athletes received during that two months?
 A. 2,222 B. 2,220
 C. 2,000 D. 2,200

8. James has $\$1,152$ in his savings account. If James withdraws $\$500$ for a new computer, what will be the balance in his savings account?
 A. $\$1,152$ B. $\$1,302$
 C. $\$652$ D. $\$2,152$

9. A delivery company has 2,070 packages to deliver today. By 2:00 p.m., they have 820 packages left to be delivered. How many packages were delivered before 2:00 p.m.?
 A. 1,250 packages B. 1,250 packages
 C. 1,250 packages D. 1,250 packages

10. Francis has had excellent success in tennis. The table shows the amount of money she has made so far for 2016.

Day	Money
Monday	\\$10
Tuesday	\\$10
Wednesday	\\$10
Thursday	\\$10

How much money does Francis still need to make to make $\$100$ for the goal of $\$200$ for the week?
 A. $\$80$ B. $\$80$ C. $\$80$ D. $\$80$

Answer Key: 5-10

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

Use Guided Support intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill		Guided Support Intervention Lesson	Standard
1	1	Write decimals in expanded form	Expanded Form of Decimal Powers of Ten	5.NBT.A.3
2	1	Identify decimal grid representation	Expanded Form of Decimal Powers of Ten	5.NBT.A.3.a
3	2	Add whole numbers to hundred thousands	Add Multi-Digit Numbers	4.NBT.B.4
4	2	Subtraction and addition of whole numbers to thousands	Multi-Step Word Problems with Addition and Subtraction	4.OA.A.3
5	1	Identify place value of a digit	Expanded Form of Decimal Powers of Ten	5.NBT.A.3.a
6	2	Round numbers to ten thousands	Round to Any Place	4.NBT.A.3
7	2	Estimate sums	Reasonableness in One-Step Word Problems	4.OA.A.3
8	2	Subtract whole numbers	Subtract Multi-Digit Numbers	4.NBT.B.4
9	2	Subtract whole numbers	Subtract Multi-Digit Numbers	4.NBT.B.4
10	2	Add and subtract whole numbers	Multi-Step Word Problems with Addition and Subtraction	4.OA.A.3

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.



GO ONLINE

Unit Opener

Focus Question

Introduce the Focus Question: *How do I add and subtract decimals?*
Ask students to think about what they know about decimals.

- What do you already know about decimals?
- When do you think you might need to add and subtract with decimals?
- What do you think you will be learning in the Unit?

Remind students that at the end of the unit, they will reflect back on what they learned in this unit.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

STEM in Action

Videos

Students can watch the two STEM videos.

STEM Career: Veterinarian Ruby talks about the work of veterinarians.

Ruby Subtracts Decimals Ruby explains how to subtract decimals.

STEM Project Card

Students can complete the STEM Project Card during their workstation time.



STEM Career: Veterinarian



Ruby Subtracts Decimals



IGNITE!

Name: _____

How Far? Answers may vary.

A. Walk a path. How many steps do you think it would take you to walk across the width of your classroom? _____ steps
 What number of steps would probably be best? _____ steps
 What number of steps would definitely be best? _____ steps

B. Measure the number of steps for each student who walked across the room.
 _____ steps _____ steps _____ steps
 _____ steps _____ steps _____ steps
 _____ steps _____ steps _____ steps
 _____ steps _____ steps _____ steps

C. Why do you suppose each student did not walk the same number of steps?

D. A common step length for a fifth grader is 1.9 feet. Use this information, along with one of the measurements listed in Part B, to estimate the width of your room in feet.
 Estimated width of the room: _____ feet

E. The actual width of the classroom given to you by your teacher is _____ feet. Discuss how close your estimate was to the actual distance.

© Ignite! - How Far?

Ignite!

How Far?

Students review addition, rounding, and estimation. They also apply nonstandard units of measurement and decimals in preparation for their work with adding and subtracting decimals.

- Before beginning the activity, measure the width of the classroom to the nearest tenth of a foot.
- Have students observe the four walls of the classroom.
 - How could you measure the width of our classroom without any standard measuring tools such as a ruler or meter stick?
- Explain that the earliest known units used to measure length were body parts, such as the cubit (the length of the forearm from the elbow to the tip of the middle finger). Explain that the use of an actual foot is how the standard foot came into being. Mention that one unit that people often use to measure distance is the length of their step when they walk (either from heel to heel or from toe to toe).
 - Make a guess as to how many steps it would take for you to walk across the width of the classroom. Record your guess in Part A, and answer the rest of the questions in Part A.
- Have up to twelve students, representing varying heights, measure the width of the classroom by walking across the room and counting their steps. Record the measurements on the board to the nearest number of complete steps. Have students record the measurements in Part B.
 - What do you notice about the measurements?
- Have students complete and discuss Part C.
- Inform students that a common step length for a fifth grader is 1.9 feet. Then have them complete Part D. Have students share their strategies.
 - Why do you suppose our estimates are not all the same?
- Have students discuss which estimates they prefer. Then reveal the actual width of the classroom and have students complete Part E.

Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson		
Game Station		Students build proficiency with adding and subtracting decimal numbers.			
		• Estimating Sums and Differences of Decimals Race	4-1		
		• Represent Addition of Decimals Task Cards	4-2		
		• Add Tenths and Hundredths Race	4-3		
		• Decimal Addition Tic Tac Toe	4-4		
		• Represent Subtraction of Decimals Task Cards	4-5		
		• Subtract Tenths and Hundredths Race	4-6		
		• Decimal Subtraction Tic Tac Toe	4-7		
• Add or Subtract Decimal Word Problems Race	4-8				
Digital Game		Batting Practice Students practice adding and subtracting decimals.	4-1		
Have students complete at least one of the Use It! activities for this unit.					
Application Station		STEM Project Card	Let's Get Organized! Students use decimals to measure and create organizers.	4-8	
		Connection Card		Cost of Living Depends on Where You Live Students use equations to compare the cost of living in rural towns and urban cities.	4-8
				Real World Card	Balance a Checkbook Students research checking accounts and practice balancing a checkbook.
					

Additional Resources

Use the resources below to provide additional support for this unit.



Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the key terms on the front side of the card.



Foldables

Use the unit foldable with Lessons 4-2 and 4-3.



Spiral Review

Students can complete the Spiral Review at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
4-1	5.MD.C.3
4-2	5.MD.C.4
4-3	5.MD.C.5
4-4	5.NBT.A.1
4-5	5.NBT.A.3
4-6	5.NBT.A.4
4-7	5.MD.C.4
4-8	5.NBT.B.7

Estimate Sums and Differences of Decimals

Learning Targets

- I can estimate sums and differences of decimals.
- I can explain how to estimate sums and differences of decimals.

Standards

Major Supporting Additional

Content

- ◊ **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- ◊ **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Reason abstractly and quantitatively.

MPP Use appropriate tools strategically.

MPP Attend to precision.

Vocabulary

Math Terms

decimal
estimate

Academic Terms

analyze
infer
reasonable

Materials

The materials may be for any part of the lesson.

- *Decimal Cards Teaching Resource*

Focus

Content Objectives

- Students estimate sums and differences of decimals using the same strategies used to estimate sums and differences of whole numbers.
- Students describe why estimation is useful.

Language Objectives

- Students discuss estimating sums and differences of decimals while answering *Wh-* questions and using the verb *rounding* as needed.
- To support maximizing cognitive and linguistic meta-awareness, ELs participate in MLR8: Discussion Supports.

SEL Objective

- Students set a focused mathematical goal and make a plan for achieving that goal.

Coherence

Previous

- Students fluently added and subtracted multi-digit whole numbers using the standard algorithm (Grade 4).
- Students generalized their understanding of place value in decimals (Unit 3).

Now

- Students use place-value strategies to estimate sums and differences of decimals.
- Students describe and explain estimation strategies.

Next

- Students use representations to add with decimals and explain their strategies (Unit 4).
- Students fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of decimals and begin to understand operations with decimals by estimating sums and differences.

Procedural Skill & Fluency

- Students build fluency with place-value concepts and learn procedures for estimating sums and differences of decimals.

Application

- Students estimate sums and differences of decimals to solve problems with real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

About How Much?

5–7 min

Build Fluency Students are given three expressions involving subtraction and are asked to estimate each difference.

Remind students that this is a mental activity, and that exact answers are not needed.

These prompts encourage students to talk about their reasoning:

- How did you estimate the differences?
- How else could you estimate the differences?
- Are the calculated answers reasonable? Why or why not?



Purpose Students explore various quantities shown in a real-world context.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may want to have students work in pairs as they notice and wonder. This can help build a collaborative classroom culture. It also allows for greater participation among students as they share their thinking with their partners.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' noticing and wondering about estimating sums and differences of decimals and are based on possible comments or questions that students may make during the share out.

- About how many gigabytes are used for photos? Explain your reasoning.
- About how many gigabytes are used for music? Explain your reasoning.
- Which is using more gigabytes, photos or music? Explain your reasoning.
- Is more than 16 gigabytes being used by photos and music? Explain your reasoning.

Math is... Mindset

- What goal do you want to achieve today?

Self-Management: Goal Setting

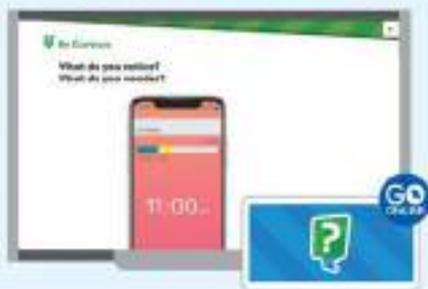
Before students begin the Notice & Wonder routine, invite them to share or write down one mathematical goal they have for the day. Have students create a plan for how they will work toward achieving their goal. Encourage students to focus their goals around estimating sums and differences of decimals.

Transition to Explore & Develop

Ask questions to get students thinking about how they have used estimation previously. Guide students to think about how estimation might relate to operations with decimals.

Establish Mathematics Goals to Focus Learning

- Let's think about why estimating sums and differences is helpful and what strategies we can use to estimate sums and differences of decimals.



Laurel
 She spent her 22 gigabytes of storage. Photos take up 8.25 gigabytes of this storage, and music takes up 13.5 gigabytes.

How can you determine about how many gigabytes of storage she left?

Find another way to find how much storage she has left.

Use rounding to estimate the sum.

8.25 → 8
 13.5 → 14

The photos and music take about 22 gigabytes of storage.

Use compatible numbers to estimate the difference.

13.5 → 13.5
 8.25 → 8.25

The total storage of photos and music is 22 gigabytes in the sum above.

The photos use about 22 gigabytes of storage left.

Strategy used to estimate sums and differences of whole numbers can also be used to estimate sums and differences of decimals. Estimating helps assess the reasonableness of calculated solutions.

Work Together

About how much more does the dog weigh than Light? How did you determine what's reasonable? Strategy to use?

Simple answer: about 4 lbs. I used rounding to estimate. Rounding both numbers were close to a whole number.

Light: 35.5 lb
 Fred: 40 lb

1 Pose the Problem

Discussion Supports

As students talk about how they know what's needed to solve the problem, restate statements they make as a question to seek clarification and provide vocabulary or grammar prompts for students who need more guidance.

Pose Purposeful Questions

- Will you need an exact answer or an estimate to solve the problem? Explain how you know.
- Which operations are needed to solve the problem? Explain how you know.

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How can you determine if an answer you calculated is reasonable?
- How is estimating sums and differences of decimals similar to estimating sums and differences of whole numbers?

Key Takeaways

- Estimating sums and differences of decimals helps assess the reasonableness of the calculated solution.
- Strategies used to estimate sums and differences of whole numbers can also be used to estimate sums and differences of decimals.

Work Together

Students work together to think about how to estimate a difference using decimal numbers. After students estimate the difference, have them share and explain the strategies they chose and how they chose them.

Common Error Students often are not sure which place to round when estimating by rounding. Point out that rounding to the nearest one will product a better estimate than rounding to the nearest ten.

Language of Math

Students may not remember common words or phrases used to identify if a problem is asking them to add or subtract. Review words such as all together, in total, combine, and remain. Have students identify what words could be used with addition or subtraction problems.

Activity-Based Exploration

Students explore estimating sums or differences of decimals.

Material: *Decimal Cards* Teaching Resource

Directions: Students select two decimal cards and write an addition expression. Repeat with new decimal cards until students have 5 addition expressions. Have students order the sums of their addition expressions from least to greatest. Students should use estimation and number sense when ordering the sums. If time permits, have students repeat by ordering subtraction expressions.

Math is... Choosing Tools

- What strategies do you know for estimating sums?

Students are thinking about the strategies they will use to aid and assist them in solving the problem.

Implement Tasks That Promote Reasoning and Problem Solving

- What strategy did you use to determine whether a sum would be greater than or less than another sum?
- How did you organize your thinking?
- Did you adjust your thinking or strategy after you started? If so, what made you adjust your thinking or strategy?

Activity Debrief: Have students share their addition expressions ordered from least to greatest. Encourage students to challenge their classmates' decisions around ordering their sums. Ask students to share their strategies for estimating the sums so that they were able to order the expressions.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine about how many gigabytes of storage is left?

The PDF of the Teaching Resource is available in the Digital Teacher Center.

3.88	9.14
2.7	8.01
5.85	7.3
9.13	9.6
6.7	2.23

Guided Exploration

Students extend strategies they learned for estimating sums and differences of whole numbers to estimating sums and differences of decimals.

Facilitate Meaningful Mathematical Discourse

- What steps do you need to take to solve this problem?
- What operation do you use to find about how much storage the photos and music take up? How do you know?
- Could you have used $3.62 + 8.25 = s$ to represent the amount of storage used by photos and music? Explain why.
- **Think About It:** When would an estimate be more useful than an exact answer?
- Explain why rounding to the nearest tenth would give a more precise estimate than rounding to the nearest whole number.

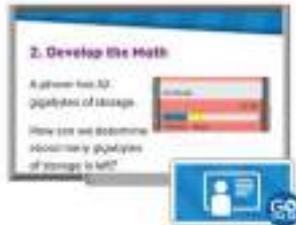
After students have explored estimating the sum by rounding, have students estimate the sum using compatible numbers. Remind students that compatible numbers are numbers that are easy to work with mentally. Have students compare and contrast the estimate by rounding to the estimate by compatible numbers.

- What would be the estimated difference if you used rounding to estimate?

Math is... Choosing Tools

- What strategies do you know for estimating sums?

Students are thinking about the strategies they will use to aid and assist them in solving the problem.



English Learner Scaffolds

Entering/Emerging Demonstrate the phrasal verb *take up* using gestures and classroom objects. Point to the desks. Say *The desks take up a lot of space*. Then point to a small object such as a laptop. Say *The laptop doesn't take up a lot of space*. Repeat, pointing to items that take up a lot of space and items that don't. Ask *Does this / Do these take up a lot of space?*

Developing/Expanding Demonstrate the phrasal verb *take up* using gestures and classroom objects. Point to the desks. Say *The desks take up a lot of space*. Then, point to a small object, such as a laptop. Say *The laptop doesn't take up a lot of space*. Repeat once. Then ask students to talk about other classroom objects using *take up*. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students which objects take up the most space and the least space in their desks. Then ask students to express the same idea using *occupy with most/least*. Validate and correct answers as necessary and provide sentence prompts for students who may need some extra help.

On My Own

Name _____

What is a reasonable estimate for the sum or difference? Explain the strategy you used. **Sample answers are shown. Check students' strategies.**

1. $3.08 + 4.02$ 2. $43.05 + 58.07$
 $0.3 + 4 = 4.3$ $43 + 58 = 101$

3. $330 + 434$ 4. $327 + 665$
 $3 + 4 = 7$ $25 + 26 = 51$

5. $4.01 - 5.9$ 6. $664 - 996$
 $8 - 6 = 2$ $88 - 99 = 11$

7. $9.28 - 5.9$ 8. $5.42 + 3$
 $9 - 6 = 3$ $5 + 2 = 7$

9. **STEM Connection** A baby chick weighs 24 grams. A veterinarian predicts the chick will weigh about 84 grams by the next day. About how much weight will the chick gain?
Sample answer: 60 g



10. The park around a lake is 200 yards and 200 feet. About how long is the path around the lake?
Sample answer: about 160 mi



11. Vermont's population is about 644,000, or the population of Iraq. They have about 2007 miles. About how many more miles does Vermont have than Iraq has?
Sample answer: about 544 mi

12. The winner of a mathematics game often scores 8700 points. Her second-place teammate scored 8150 points. About how long does the game usually last? Do you agree with the winner's answer?
Sample answer: about 6 more points

13. About how many people are in the United States? Do you agree with the winner's answer?
Sample answer: 2 more of people and 1 more of million

14. **Number Theory** (Challenge) 1000 is to be spent on the sale. He could cost \$1.25, another game \$1.00 for each. Chetan wants to spend about \$5.00 on the (Challenge) number of money? (Money = \$1.00) (Money = 100 cents) Do you agree with the winner's answer?
Ms. Sample answer: $11 + 4 = 15$, but 15 is less than the actual game, he has less than \$5 to spend.

Reflect

How would you explain to a friend how to estimate the sum of two decimals? **Answers may vary.**

Monitor
 How have you worked to achieve your goal today?
 How do you feel about your work today?

Practice

Build Procedural Fluency from Conceptual Understanding

Common Misconception: Exercises 1–8 Students may think there is only one “correct” estimate to these problems. Remind them that their estimates and the estimates of their classmates may, and will, be different since they are based on different estimation strategies.

Item Analysis

Item	DOK	Rigor
1–8	2	Procedural Skill and Fluency
9–13	3	Application
14	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How would you explain to a friend how to estimate the sum of two decimals?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you worked to achieve your goal today?

Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can estimate sums and differences of decimals.
- I can explain how to estimate sums and differences of decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Estimate difference of decimals	5.NBT.B.7
2	2	Estimate sum of decimals	5.NBT.B.7
3	2	Estimate difference of decimals	5.NBT.B.7
4	3	Estimate sum of decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 4		Then have students do	
4 of 4		Additional Practice or any of the ✔ or ✔ activities	
3 of 4		<i>Take Another Look</i> or any of the ✔ activities	
2 or fewer of 4		Small Group Intervention or any of the ✔ activities	

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 4-1
Exit Ticket

Name _____

- The baby panda at the zoo weighs 10.8 pounds. The baby lion at the zoo weighs 16.2 pounds. Which equation would give the most reasonable estimate of the difference between the weight of the baby panda and the weight of the baby lion?

A. $16 - 10 = 6$	B. $16 + 10 = 26$
C. $16 - 10 = 26$	D. $16 + 10 = 6$
- The box of books weighs 24.82 pounds. A second box of books weighs 34.22 pounds. Which equation best estimates the total weight of the two boxes of books?

A. $24 + 34 = 6$	B. $24 + 34 = 102$
C. $24 + 34 = 59$	D. $24 + 34 = 59$
- The height of a building is about 26.47 centimeters. The lowest part is 9 centimeters tall. About how many floors is the rest of the building?

A. About 50 centimeters	B. About 56 centimeters
C. About 56 centimeters	D. About 100 centimeters
- Each item in the toy store costs \$0.99. How many \$1.00 bills do you need to pay for 10 items?

Sample answer: about 20 bills because $0.99 \times 20 = 19.80$ rounds to 20 and 19.80 rounds to 20, and $9 + 10 = 19 = 20$.

Reflect On Your Learning

1. ✔ I'm confused

2. ✔ I'm still learning

3. ✔ I understand

4. ✔ I can teach someone else

Assessments Book 18

R Reinforce Understanding

SMALL GROUP

What are the Compatible Numbers?

Provide students with digit cards and calculators. Each student is dealt two cards to create addends in tenths.

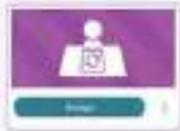
Students use compatible numbers to estimate the sum of their two numbers. If necessary, remind students to look for ways to adjust the numbers to get sums or differences that end in 5 or 10. Students add with a calculator and compare whether the calculated sum is close to their estimated sum. Repeat the activity several times.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Estimate Sums and Differences of Decimals



INDEPENDENT WORK

Differentiation Resource Book, p. 21

Lesson 4.1 • Reinforce Understanding
Estimate Sums and Differences of Decimals

Review

When estimating sums and differences of decimals, you can round each decimal number to the nearest whole number.

$4.61 + 9.25 = ?$
 Round each whole number to 5.
 $4.61 \approx 5$ and $9.25 \approx 9$.
 $5 + 9 = 14$.
 The sum is about 14.

$13.21 - 4.87 = ?$
 Round each whole number to 13.
 $13.21 \approx 13$ and $4.87 \approx 5$.
 $13 - 5 = 8$.
 The difference is about 8.

Estimate the sum or difference. Round to the nearest whole number.

- Jason and the teacher have 10 digit cards. They write 4.36 percent. They roll 1.70 percent of the ball. About how much more will be left in the tank? **$4 - 2 = 2$, about 2 percent**
- Emily and Janelle are playing basketball in a game. Emily points 10.57 percent and Janelle points 13.58 percent. About how many percent of the game did Emily and Janelle play? **$11 + 13 = 24$, about 24 percent**
- Chris needs 0.76 percent of sugar to make fruit bars. He has 0.58 percent of sugar. About how many percent of sugar does he need to complete the recipe? **$11 - 9 = 2$, about 2 percent**

B Build Proficiency

WORKSTATIONS

Practice It Game Station
Estimating Sums and Differences of Decimals Race

Students practice estimating sums and differences of decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 21–22

Lesson 4.1
Additional Practice

Review

Two car models have different gas mileage.

Car A has 28 mpg and Car B has 32 mpg. The distance between the cities is 150 miles. How far will Car A travel before it runs out of gas?
 $150 \div 28 = 5.35$
 $5 \times 28 = 140$
 $150 - 140 = 10$
 Car A will travel about 100 miles before it runs out of gas.

Car B has 32 mpg and Car A has 28 mpg. The distance between the cities is 150 miles. How far will Car B travel before it runs out of gas?
 $150 \div 32 = 4.68$
 $4 \times 32 = 128$
 $150 - 128 = 22$
 Car B will travel about 128 miles before it runs out of gas.

Estimate each sum or difference. Write the estimate and show work.

- $0.61 + 2.71 = ?$ $1.88 + 2.12 = ?$
 $0.6 + 2.7 = 3.3$ $1.9 + 2.1 = 4.0$
- $10.20 - 4.80 = ?$ $50.08 - 47.12 = ?$
 $10 - 5 = 5$ $50 - 50 = 0$
- $1.2 + 1.75 = ?$ $24.07 + 0.23 = ?$
 $1.2 + 1.8 = 3.0$ $25 + 0.2 = 25.2$
- $3.12 - 1.8 = ?$ $64.07 - 24.07 = ?$
 $3.1 - 1.8 = 1.3$ $64 - 24 = 40$

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 21–22

Solve each problem.

9. Mikah worked 14 hours yesterday, 14½ hours today, and 16½ hours tomorrow. How many hours did he work last week?
Sample answer: about 4 weeks

10. A flower shop ordered 240 roses on Monday, 250 roses on Tuesday, and 260 roses on Wednesday. How many roses did the shop order during the week?
Sample answer: about 5 cartons

11. Donnie has \$20.25 in his pocket. He buys lunch food and pays \$4.75. How much money did he have left?
His Sample answer: He will have about \$20 - \$4.75 = \$15.25 left, so he will not have enough money to buy the hat.

12. Henry has \$20.00 to spend at the store. He buys a hat for \$12.50 and a shirt for \$4.95. About how much money will he have left?
Sample answer: About \$10; he spends about \$12.50 + \$4.95 = \$17.45, and so will have about \$20 - \$17.45 = \$2.55 left.

Math in Motion Activity

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M

Extend Thinking

Use It! Application Station

Balancing a Checkbook Students research checking accounts and practice balancing a checkbook.

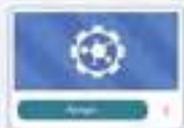
The content of this card has concepts covered later in Lesson 4-7. You may want to assign this card to students ready to explore content covered later in this unit.



WORKSTATIONS

Web sketch Exploration

Assign a web sketch exploration to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 22

Lesson 4-1 • Student Thinking

Estimate Sums and Differences of Decimals

Problem

1. Carter has a \$20 gift card to use for downloading music. He wants to spend as much as he can of his gift card without going over. How many dollars can he spend?

The cost of the album Carter wants to download is:

A	B	C	D	E	F	G
\$5.94	\$4.21	\$1.57	\$4.58	\$4.44	\$1.77	\$5.75

What is the greatest number of albums Carter can buy? Round each price to the nearest whole dollar and make your selection. Supply your answer.

Sample answer: Round to the nearest whole dollar:

A	B	C	D	E	F	G
\$6	\$4	\$2	\$5	\$4	\$2	\$6

Carter should buy albums A, B, C, and F because $\$6 + \$4 + \$2 + \$4 = \$16$. Any more albums would put him over the \$20 limit.

2. Round the sum of each album to the nearest whole dollar. How many albums can Carter buy now?

A	B	C	D	E	F	G
\$6.0	\$4.2	\$1.6	\$4.6	\$4.4	\$1.8	\$5.8

Sample answer: Carter can still only buy 4 albums: A, C, D, and F.

3. Which method makes you prefer why? **Sample answer:** I would round to the nearest tenth of a dollar because that gives you a more precise idea of how much you can spend.

Differentiated Instruction

INDEPENDENT WORK

Level 4
Estimating Decimal Sums and Differences

Name _____

For each problem, use what you know about decimals and estimation to choose the better estimate. Do not perform the exact calculation or round.

1. $0.04 + 0.02$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
Explanations may vary.

2. $0.99 + 0.01$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
Explanations may vary.

For each problem, use what you know about decimals and estimation to choose the better estimate. Do not perform the exact calculation or round.

3. $0.07 + 0.03$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
Explanations may vary.

4. $0.97 + 0.03$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
Explanations may vary.

Reflect On Your Learning

The feedback _____ the skills _____ confidence _____ I can work on _____

Analyze the Probe ✔ Formative Assessment

Targeted Concept Determine approximate sums and differences by reasoning about the magnitude of decimals to compare decimal sums and differences to common benchmarks.

Targeted Misconceptions Some students have conceptual misunderstandings with decimal place-value ideas required for reasoning about the size of a decimal. Some students have difficulty comparing decimals to common decimal benchmarks such as 0.5 or 0.25. Watch for students who show exact calculations in their explanations rather than using reasoning about the estimates without actually calculating.

Authentic Student Work

Below are examples of correct student work and explanations.

Sample A

1. $0.04 + 0.02$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
 b because you will need to take greater than 0.2 to get less than $\frac{1}{2}$.

Sample B

1. $1.567 + 0.89$
 Circle a or b to show the better estimate.
 a. less than $\frac{1}{2}$
 b. greater than $\frac{1}{2}$

Explain or show your thinking.
 b because still doesn't take away 1 whole. $1.5 + 0.5 = 2$

Collect and Assess Student Work

Collect and review student response to determine possible misconceptions. See examples in If-Then chart.

IF incorrect... THEN the student likely...	Sample Misconceptions
<p>1. b connects an addition problem to the phrase “greater than” and a subtraction problem to the phrase “less than”—without considering the values being added or subtracted in relation to the benchmarks.</p> <p>2. b</p> <p>3. a</p> <p>4. a</p>	<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>4. 1.58 <input checked="" type="radio"/> 1.89</p> <p>Circle a or b to show the better estimate.</p> <p><input type="radio"/> a. less than $\frac{1}{2}$</p> <p><input checked="" type="radio"/> b. greater than $\frac{1}{2}$</p> </div> <div style="width: 50%;"> <p>Explain or show your thinking.</p> <p>I chose less than $\frac{1}{2}$ because it IS about "LESS Than"</p> </div> </div>
<p>1. b rounds the numbers but does not consider the precision needed. For example, in Exercise 1, a student may round 0.603 to 1; in Exercise 2, a student may round 0.99 to 1. In both cases, the student concludes that the sum is greater than 1.</p> <p>2. b</p>	<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>1. 0.04 + 0.603</p> <p>Circle a or b to show the better estimate.</p> <p><input type="radio"/> a. less than 1</p> <p><input checked="" type="radio"/> b. greater than 1</p> </div> <div style="width: 50%;"> <p>Explain or show your thinking.</p> <p>I rounded to the closest number and added up from that. 1.000 + 0.040.</p> </div> </div>
<p>1. b does not consider the impact of place value in determining a digit's value. In Exercise 1, a student assumes the answer will be greater than 1 because $6 + 4 = 10$. In Exercise 2, a student concludes that the sum must be greater than 1 because there are several 9s. In Exercise 3, a student may conclude that subtracting 0.085 has a much greater impact on the difference than it really has.</p> <p>2. b</p> <p>3. a</p>	<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>2. 0.99 + 0.009</p> <p>Circle a or b to show the better estimate.</p> <p><input type="radio"/> a. less than 1</p> <p><input checked="" type="radio"/> b. greater than 1</p> </div> <div style="width: 50%;"> <p>Explain or show your thinking.</p> <p>0 because 99 + 9 is greater than 100.</p> </div> </div>

Many of the above difficulties result in a combination of correct and incorrect responses. For correct responses, be sure to check for sound reasoning.

Take Action

Choose from the following resources or suggestions:

- Revisit the activities for rounding decimals and estimating decimal sums and differences in Lesson 4-1.
- Help students develop visual images of decimal place-value ideas by using base-ten blocks. When base-ten blocks are used to represent decimals, you may want a large cube to be worth 1, a flat to be worth 0.1, a rod to be worth 0.01, and a small cube to be worth 0.001.
- Do estimation activities in small and large groups, providing opportunities for students to discuss their reasoning strategies.

Revisit the Probe after additional instruction. Have students review their initial answers to the probe. Use these questions for discussion:

- *Are there any answers you would like to change? Explain why you might want to change them.*
- *Are there any questions that you still have about any of the items on this probe?*

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Represent Addition of Decimals

Learning Targets

- I can represent addition of decimals using decimal grids.
- I can represent addition of tenths and hundredths.

Standards

Major Supporting Additional

Content

- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Model with mathematics.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms

decimal grid
hundredths
tenths

Academic Terms

benefit
drawback
evaluate

Materials

The materials may be for any part of the lesson.

- number cube
- *Tenths and Hundredths* Teaching Resource

Focus

Content Objective

- Students use decimal grids to represent addition of decimals with the same number of places.

Language Objectives

- Students discuss using decimal grids to represent addition of decimals while answering *Wh-* and *Yes/No* questions.
- Support optimizing output, MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students identify and discuss the emotions experienced during math learning.

Coherence

Previous

- Students fluently added and subtracted multi-digit whole numbers using the standard algorithm (Grade 4).
- Students estimated sums and differences of decimals and explained estimation strategies (Unit 4).

Now

- Students use representations to add decimals.
- Students describe and explain their strategies for adding decimals.

Next

- Students add decimals using drawings and strategies based on place value (Unit 4).
- Students add, subtract, multiply, and divide decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students create and use representations to build their understanding of addition with decimals.

Procedural Skill & Fluency

- Students build fluency with place-value concepts and start to develop skills for adding decimals.

Application

- Students represent addition of decimals to solve problems in real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine About How Much?



5–7 min

Build Fluency Students estimate sums involving 3-digit whole numbers.

Remind students that this is a mental activity, and that exact answers are not needed.

These prompts encourage students to talk about their reasoning:

- How did you estimate the sums?
- Is there more than one way to estimate a sum? Explain.
- How can you tell if an estimate is reasonable?

Purpose Students explore what a map can tell them. They consider how numbers might be incorporated into the map.

Numberless Word Problem

- What could you ask?
- What math do you use in this problem?

Teaching Tip You may want to have students to create a list of questions individually first. Then have them form small discussion groups where they can share their questions about the map.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about using decimal grids to represent addition of decimals and are based on possible comments and questions that students might make during the share out.

- What information can you learn from the map?
- What questions could you ask about the map?
- What information would you need to answer your questions?
- How could you find the total distance of the route shown?

Math is... Mindset

- How can my math skills or interests help me with my work?

Self-Awareness: Identify Emotions

Give students opportunities to share about themselves to reinforce their sense of identity and belonging. As students work collaboratively to complete the Numberless Word Problem routine, invite them to share a personal skill or interest related to math. Encourage them to think about how that skill can help them with their work on adding decimals today.

Transition to Explore & Develop

Ask questions to get students thinking about determining the total distance of the route. Ask them to think about what operations would be used to determine the total distance. Guide students to think about the different kinds of tools they can use to solve distance questions.

Establish Mathematics Goals to Focus Learning

- Let's think about how we can use decimal grids to represent addition of decimals.

Lesson 4-2
Represent Addition of Decimals

Be Curious
What's the question?

Home School Park Grandpa's

What do you know about the route?

Be Curious
What's the question?

Home School Park Grandpa's

GO ON!

Learn
 Draw three maps showing the distances between locations.

How can you determine how far Deja walks from home to the bookstore, then to the playground?
 How can you determine how far she walks from the playground to her school, then to her home?

Draw a grid for home to the bookstore, then to the playground.

Grid worked: 0.2 miles.

Draw a grid from the playground to school, then to the park.

Grid worked: 0.2 miles.

You can use decimal grids to help solve word problems involving addition.

Work Together

Read tonight's problems and discuss. How much do the potatoes and carrots weigh? Use decimal grids to solve.

1.2 kg

1.1 kg

1.1 kg

Multi-Step Choosing Topics: How are decimal grids helpful in determining the cost of her purchases?

1 Pose the Problem

Pose Purposeful Questions

- What are the problems asking you to find? How do you know?
- How can you find the distance from Deja's home to the bookstore?
- How do you know how far it is from the bookstore to the playground?
- Which operation will you use to determine the answer? How do you know?

2 Develop the Math

Choose the option that best meets your instructional goals.

Stronger and Clearer Each Time

Pair students and have them solve an addition equation involving decimals using decimal grids. Ask each to work individually and write about how they solved the problem. Then have students share their writing with their partner, comparing their sentences, and if needed, make corrections. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How could you explain to a friend how to represent addition of decimals?

Key Takeaway

- Addition of decimals can be represented using concrete models or drawings, such as decimal grids.

Work Together

You may wish to provide copies of the *Tenths and Hundredths* Teaching Resource for students to use as they solve this problem. Have students to explain how they determined which grid to use to represent 0.9 and 0.3.

Common Misconception Students may think that each small square is a tenth or that each column is a hundredth in a decimal grid. Remind students that the big square represents the whole. Since there are 10 columns and 100 little squares, each column represents 0.1 and each little square represents 0.01.

Language of Math

Encourage students to read each addend using mathematically precise language, such as *nine tenths* and not informal language, such as *zero point nine*. Using precise language can help students understand the value of the quantities, which can then be used to help assess reasonableness of answers.

Activity-Based Exploration

Students will write addition expressions and then use models to add the decimals.

Materials: number cube (labeled 1–6), *Tenths and Hundredths Teaching Resource*

Directions: Have students roll the number cube once to create a decimal number to the tenths with a 0 in the ones place. Students roll again to make another decimal number to the tenths. Have students work together to use decimal grids to find the sum of the decimals. Repeat by rolling two number cubes and using the digits to make a decimal number to the hundredths.

Support Productive Struggle

- How did you determine which grid to use to represent the problem?
- Could you have used the hundredths grid to show tenths? Explain why or why not.
- Explain how you know that is the sum.
- How can you show that your calculated sum is reasonable?

Math is... Choosing Tools

- How are decimal grids helpful in determining the sum of two decimals?

Students are explaining the process for choosing and using decimal grids as tools to aid and assist them in solving an addition problem.

Activity Debrief: After students work through their solutions, encourage them to share their strategies and answers with others. Have students revisit the Pose the Problem question and discuss their answers.

- How can you determine how far Deja walks from home to the bookstore, then to the playground?
- How can you determine how far she walks from the playground to the school, then to the park?

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students use concrete models or drawings, such as decimal grids, to add decimal numbers with the same number of decimal places.

Use and Connect Mathematical Representations

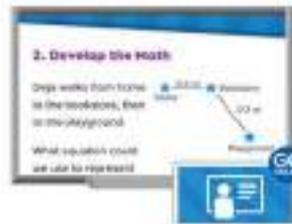
- How do you know that the equation you wrote for the problem is correct?

Provide copies of the *Tenths and Hundredths Teaching Resource*. Have students shade the decimal grids as they work through determining the distance from the playground to the school, then to the park.

Math is... Choosing Tools

- How are decimal grids helpful in determining the sum of two decimals?
- How do the decimal grids represent the amounts in the problem?
- **Think About It:** Are there tools other than decimal grids you could use to solve the problem? Explain how you would use them.

Students are explaining the process for choosing and using decimal grids as tools to aid and assist them in solving an addition problem.



English Learner Scaffolds

Entering/Emerging Support students' understanding of *how far*. Standing by your desk, point to your door and say *Let's see how far the door is from the desk*. Measure and say *The door is [ten feet] from the desk*. Repeat with new objects. Then prompt students to find the distance between two classroom objects. Ask *How far is the [bookshelf] from [the closet]?*

Developing/Expanding Support students' understanding of *how far*. Standing by your desk, point to your door and say *Let's see how far the door is from the desk*. Measure and say *The door is [ten feet] from the desk*. Repeat with new objects. Then prompt students to choose two classroom items to measure distance and have pairs take turns asking and answering about the distance.

Bridging/Reaching Have students work with maps, either real or drawn, and ask them to talk about how far different places are from a central location. Validate or correct as necessary.

On My Own

Name _____

What is the sum? Use the decimal grids. *Complete shading above.*

$0.07 + 0.14 = 0.21$ $0.09 + 0.04 = 0.13$


$0.003 + 0.02 = 0.023$ $0.076 + 0.04 = 0.116$


What is the sum? Use decimal grids to show the sum.

$0.12 + 0.2 = 0.32$ $0.23 + 0.1 = 0.33$
 $0.338 + 0.15 = 0.488$ $0.076 + 0.04 = 0.116$
 $0.020 + 0.04 = 0.06$ $0.046 + 0.20 = 0.246$

16. Write the addition equation represented by the decimal grids.
 $0.56 + 0.07 = 0.63$

17. **ITIN Connection:** A subtraction story: 12 million (12,000,000) with 1.5 million (1,500,000) has many millions are in the world? Use decimal grids to solve. 2.7 mil.

18. **Extend Your Thinking:** Write a word problem that could be solved using this decimal grid. *Hint: solve the problem.*
 Sample answer: George ran 0.2 mile on Monday, 0.6 mile on Tuesday, and 0.3 mile on Wednesday. How much did he run over those three days? He ran 0.9 mile.

Reflect

How did using decimal grids help you add decimals?
 Answer in my own words.

Math Practice
 How has your learning changed?
 (Discuss with a partner)

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 7 Students may incorrectly try to add tenths instead of hundredths. They may assume that since there is only one non-zero digit, that they are adding tenths instead of hundredths. Remind students that the zeros are not just placeholders. Encourage them to say each addend aloud before modeling it on a decimal grid.

Item Analysis

Item	DOK	Rigor
1–4	2	Procedural Skill and Fluency
5–11	2	Conceptual Understanding
12	3	Application
13	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How did using decimal grids help you add decimals?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did my math skills or interests help me with my work today?

Students reflect on how they practiced self-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can represent addition of decimals using decimal grids.
- I can represent addition of tenths and hundredths.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Add decimals with the same number of decimal places using decimal grids	5.NBT.B.7
2	2	Add decimals with the same number of decimal places using decimal grids	5.NBT.B.7
3	2	Add decimals with the same number of decimal places using decimal grids	5.NBT.B.7
4	3	Add decimals with the same number of decimal places using decimal grids	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

- If students score 4 of 4** Then have students do Additional Practice or any of the ✔ or ✔ activities
- 3 of 4** *Take Another Look* or any of the ✔ activities
- 2 or fewer of 4** Small Group Intervention or any of the ✔ activities

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 4.2
Exit Ticket

Name: _____

1. Which number represents the sum shown by the decimal grid?

A. $0.03 + 0.07 = 0.10$
B. $0.3 + 0.7 = 1.0$

C. $0.03 + 0.07 = 0.10$
D. $0.3 + 0.7 = 1.0$

2. Use the decimal grid to solve the equation.

$0.8 + 0.2 = \underline{\hspace{2cm}}$

A. 0.8
B. 0.2

C. 0.8
D. 0.2

3. We have an apple for \$0.09 and an orange for \$0.12. How much more do we pay for each piece of fruit?

\$1.25

Reflect On Your Learning

How confident are you about your understanding of this lesson?

1 (Not confident) 2 (Somewhat confident) 3 (Confident) 4 (Very confident)

18 Assessment Resources

R Reinforce Understanding

SMALL GROUP

Move It

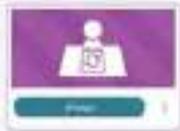
Use two hundredths number lines from 0 to 2. Roll two number cubes to create a decimal in hundredths. Decompose the decimal and show the decimal on a decimal grid. So, if 0.52 is rolled, students may shade 0.5 on one grid and 0.02 on the other, or shade 0.52 on one decimal grid. Make sure students understand the relationships between hundredths, tenths, and ones. Students build on each other's moves. Play ends when 2 full grids are shaded. Then students may repeat the activity.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Model Adding Decimals



INDEPENDENT WORK

Differentiation Resource Book, p. 23

Lesson 4.2 Reinforce Understanding
Represent Addition with Decimals

Name: _____

Review
Use simplified drawings of tenths and hundredths to find the sum of decimals.
Add: $0.22 + 0.18$
You can draw a tenths grid to represent 0.2.
You can draw a hundredths grid to represent 0.18.
To add $0.22 + 0.18$, use simplified drawings.
Exchange 10 hundredths for one tenth to regroup.
 $0.22 + 0.18 = 0.40$

Add the decimals using simplified drawings. Then write the sum as a decimal.

6. $0.41 + 0.28$
 $0.41 + 0.28 = 0.69$

8. $0.49 + 0.20$ 9. $0.45 + 0.30$
 $0.49 + 0.20 = 0.69$ $0.45 + 0.30 = 0.75$

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Represent Addition of Decimals Task Cards
Students practice representing the addition of decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 23–24

Lesson 4.2
Additional Practice

Name: _____

Review
Use one and two decimals using decimal grids.
Andrew bought 4 one-dollar books. He also bought one book that cost \$0.45. How much did he spend?
Use an addition equation to represent the problem. Use decimal grids to solve the equation. Compare the grids to explain the sum.

Andrew: $4.00 + 0.45 = 4.45$ Daria: $4.00 + 0.45 = 4.45$

Do you agree? Explain.

Use decimal grids to solve each equation. Complete shading squares.

1. $0.31 + 0.27 = 0.58$ 2. $0.07 + 0.07 = 0.14$

3. $0.24 + 0.07 = 0.31$ 4. $0.5 + 0.5 = 1.0$

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Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 23–24

Use decimal grids to solve each equation.

6. $0.8 + 0.4 = 1.2$ 7. $0.6 + 0.9 = 1.5$

8. $0.9 + 0.9 = 1.8$ 9. $0.8 + 0.7 = 1.5$

10. Write the addition equation represented by the decimal grids.

11. Use base-ten blocks to solve each problem. Find the total weight of the fish in each tank. Show your work.

12. 0.83 pounds

Math in Motion Activity

Use your understanding of decimal grids to solve a real-world problem. Write an addition equation to solve the problem. Use a decimal grid to help you. Show your work.

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E

Extend Thinking

Use It! Application Station

Cost of Living Depends on Where You Live

Students use equations to compare the cost of living in rural towns and urban cities.

The content of this card has concepts covered later in Lesson 4-8. You may want to assign this card to students ready to explore content covered later in this unit.



WORKSTATIONS

Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 24

Lesson 4-2 • Extend Thinking

Represent Addition with Decimals

Write:

1. Robert takes care of the 4 fish in his aquarium. He must find the total weight of the fish to determine how much food to feed them.

Fish's name	Weight	Length	Age	Color
Redfish	0.35	12.5	1.5	Red
Bluefish	0.25	10.0	1.0	Blue

Find the total weight of the fish in his aquarium using the decimal grid. Show your work.

The total weight is 0.60 grams.

2. Robert has 3 fish tanks in his garden. He has a total of 0.25 pounds, 0.25 pounds, and 0.25 pounds. Find the total weight of the fish using the decimal grid. Show your work.

The weight of the fish tanks is 0.75 pounds.

3. Robert's cousin has 3 beautiful fish in her tank. The fish weigh 0.23 pounds, 0.23 pounds, and 0.23 pounds. Find the total weight of the fish using the decimal grid. Show your work.

The weight of the beautiful fish is 0.67 pounds.

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INDEPENDENT WORK

Represent Addition of Tenths and Hundredths

Learning Targets

- I can explain how to use various strategies to add decimals.
- I can demonstrate how to use various strategies to add decimals.

Standards

Major Supporting Additional

Content

- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Attend to precision.

MPP Look for and make use of structure.

Vocabulary

Math Term

decimal grid

Academic Terms

debate

infer

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- decimal grid
- index cards

Focus

Content Objective

- Students use decimal grids to represent addition of decimals with different number of decimal places.

Language Objectives

- Students discuss using decimal grids to add decimals while answering *Wh-* questions and using the adjective *similar*.
- Support sense-making, MLR2: Collect and Display.

SEL Objective

- Students collaborate with peers to complete a mathematical task and offer constructive feedback to the mathematical ideas posed by others.

Coherence

Previous

- Students added and subtracted whole numbers using the standard algorithm (Grade 4).
- Students used representations to add decimals with the same number of decimal places (Unit 4).

Now

- Students add decimals in hundredths using concrete models, drawings, and strategies based on place value.

Next

- Students use addition strategies to add decimals (Unit 4).
- Students add, subtract, multiply, and divide decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of place value, decimals, and operations with decimals.

Procedural Skill & Fluency

- Students build fluency with place-value concepts and develop their skills for adding decimals.

Application

- Students represent addition of decimals to solve problems in real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Would You Rather?

5–7 min

Build Fluency Students build number sense as they compare numbers to products of multiplication expressions,

These prompts encourage students to talk about their reasoning:

- What strategies did you use to find your answers?
- How could you use estimation to compare the amounts?

Purpose Students consider how each decimal is represented on the decimal grids to identify similarities and differences.

Notice & Wonder

- How are they the same?
- How are they different?

Teaching Tip You may want to have students use their own decimal grids to display the numbers. This can help reinforce what each grid represents.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' noticing and wondering about representing addition of tenths and hundredths on decimals grids, and are based on possible comments and questions that students may make during the share out.

- What do you notice about the decimal grids?
- What do you think the shaded parts of the decimal grids represent?
- Do you think both decimal grids are shaded equally? Explain.

Math is... Mindset

- Why should you value the ideas of others?

Social Engagement: Value Ideas of Others

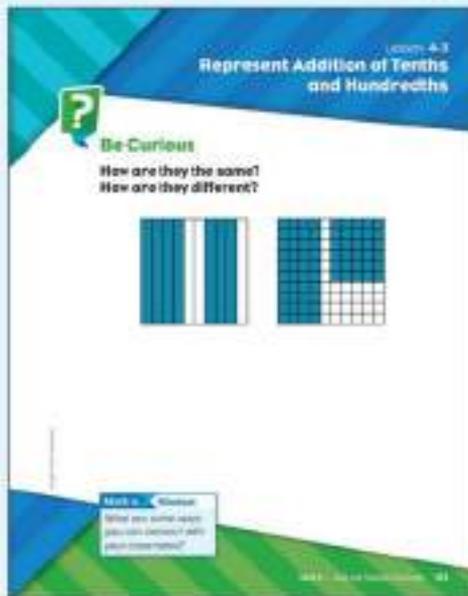
As students engage in collaborative discourse about the Notice & Wonder routine, remind them that valuing ideas of others is an important part of being an effective and respectful communicator. Explain that one way to do this is by listening attentively when other are sharing their ideas about what how the decimals are the same and how they are different.

Transition to Explore & Develop

Ask questions that get students thinking about the uses of decimal grids. Guide students think about how decimal grids can be used to represent addition. Students may recall that there are other ways to visually represent math problems, such as using number lines.

Establish Mathematics Goals to Focus Learning

- Lets think about how decimal grids could be useful when representing addition problems that involve decimals that have a different number of decimal places.



Lesson 4-3
Represent Addition of Tenths and Hundredths

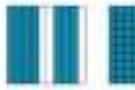
 **Be Curious**
How are they the same?
How are they different?



Math is... Mindset
What are some ways you can value others' ideas?



 **Be Curious**
How are they the same?
How are they different?





Learn
How can you determine the sum of $0.7 + 0.08$?

You can use decimal grids to help you determine the sum.

Sometimes you need to represent tenths as hundredths to help when adding numbers having tenths.

Math **Networks**
How is adding tenths similar to adding whole hundredths?

Work Together
Which is the better way of how a one dollar bill and a quarter? Why is a decimal grid helpful?

Operation	Amount
Change 80¢	0.8
Change 20¢	0.20

1 Pose the Problem

Collect and Display

As students discuss the questions, record relevant words and phrases they may use such as *represent*, *shade*, *less than*, and *greater than*. Display the words for student reference. Use the student-generated expressions to help students make connections between student language and math vocabulary.

Pose Purposeful Questions

- Is this question asking to add or subtract? How do you know?
- Do you think the sum will be less than or greater than 1? Why?

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How is representing and solving addition of decimals having different numbers of decimal places similar to representing and solving addition of decimals having the same of decimals places? How is it different?

Key Takeaway

- Addition of decimals with different numbers of decimal places can be represented using concrete models or drawings, such as decimal grids.

Work Together

You may wish to provide *Decimal Grids* Teaching Resource for students to use for the Work Together. Have students share their thinking when determining how to represent 0.6 using a grid that shows hundredths.

Common Misconception When students see words or phrases such as *more*, *all together*, *total*, *combine*, *increased by*, *plus*, and *sum*, they may assume the problem is looking for a solution that requires addition but that is not always the case. Remind students that they need to carefully consider the meaning of the language in a problem before deciding what operations to use.

Language of Math

Ask students what they look for in a problem to decide that its solution requires addition. They may say they look for particular words. While some addition contexts are communicated using words and phrases such as “more,” “all together,” “in total,” “combine,” “increased by,” “plus,” and “sum,” remind students that they need to carefully consider the meaning of the language in a problem before deciding what operations to use.

Activity-Based Exploration

Students will explore using decimal grids to solve addition equations involving decimal with tenths and hundredths.

Materials: 10×10 Teaching Resource

Directions: Provide copies of the 10×10 Teaching Resource to each pair or small group. Have students solve the Pose the Problem.

Support Productive Struggle

- How did you determine how to represent 0.7 on a decimal grid showing hundredths?
- Will your strategy for adding tenths and hundredths on a decimal grid always work?
- Is there another way to solve the problem?
- How can you prove that your solution is correct?

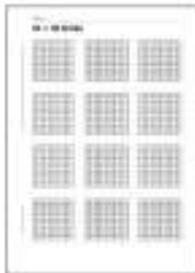
Math is... Structure

- How is adding decimals similar to adding whole numbers?

Students are thinking about and discussing the structure of mathematics that makes adding decimals and adding whole numbers almost identical processes.

Activity Debrief: After groups work through their solutions, encourage them to share their decimal grids and answers with others. Facilitate a discussion to ensure students understand that when using representation to add tenths and hundredths, it is necessary to represent the tenths as an equivalent hundredths.

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students extend strategies they learned in Grade 4 for adding decimal fractions. They also think about the different strategies they could use to find their solutions.

Provide 10×10 Teaching Resource for students to shade decimal grids as they work through the problem together. Encourage students to shade the two decimal values within the same grid. Students should shade an additional grid only when the first one is completely shaded.

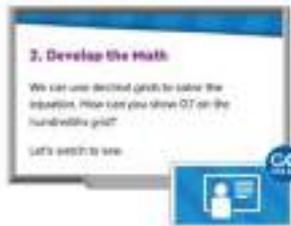
Use and Connect Mathematical Representations

- **Think About It:** How many hundredths should be shaded to show 0.7?
- What are some other strategies you could use to find your answer?
- How could you use estimation to help you assess the reasonableness of your calculated solution?
- How did the different number of decimal places in the numbers affect the solution strategy?

Math is... Structure

- How is adding decimals similar to adding whole numbers?

Students are thinking about and discussing the structure of mathematics that makes adding decimals and adding whole numbers almost identical processes.



English Learner Scaffolds

Entering/Emerging Ensure students know what *weight* means by weighing classroom objects between 1–3 pounds. First, weigh a book. Say *This weighs one and a half pounds. The weight is one and a half pounds.* Be sure to point out that *lb* on the Learn page is short for *pound*. Repeat with another object. Then weighing other objects, ask *What is the weight of this—[two pounds] or [three pounds]?*

Developing/Expanding Ensure students know what *weight* means by weighing classroom objects between 1–3 pounds. First, weigh a book. Say *This weighs one and a half pounds. The weight is one and a half pounds.* Be sure to point out that *lb* on the Learn page is short for *pound*. Repeat with another object. Then, ask students to weigh other objects and tell you their weight.

Bridging/Reaching Ensure comprehension of the words *weigh*, *weight*, and *pound* by asking students to weigh objects and tell you their weight. Then discuss with students other weight measurements such as ounces, grams, etc. Finally, ask students to work together to sort the words into two groups: metric and imperial, and to include abbreviations of measurements that they know, such as *lb*, *oz*, and *g*.

On My Own

Name _____

What is the sum? Use decimal grids to solve.

1. $0.8 + 0.2 = 1.0$ 3. $0.6 + 0.4 = 1.0$




2. $0.95 + 0.05 = 1.0$ 4. $0.4 + 0.06 = 0.46$




What is the sum? Use decimal grids to solve.

5. $0.7 + 0.3 = 1.0$ 6. $0.8 + 0.2 = 1.0$

7. $0.8 + 0.2 = 1.0$ 8. $0.1 + 0.9 = 1.0$

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9. Add 1 gram (100 milligrams) and 1 gram (100 milligrams) and find an additional 100 milligrams. What is the total weight? **2.00 g**

10. You bought 1.6 pounds of peanuts and 2.75 pounds of almonds. What is the total weight of the nuts you bought? **3.35 lb**

11. **Area analysis** Add 100 centimeters (1 meter) and 100 centimeters (1 meter) and find an additional 100 centimeters (1 meter). **Sample answer:** This model correctly shows 0.33, but shows 0.32 added instead of 0.3. Also should shade 3 additional squares.

12. **Extend Your Thinking** Jorge ran a triathlon consisting of 10 miles each day. She then ran 10 miles and another 10 miles. How far does she run each day? **Sample answer:** Jorge runs 30 miles each day. She runs 10 miles each day and 10 miles each day and 10 miles each day.

Yes, Sample answer: by using 10×30 number grids and shading 20 squares, 100 squares, and 20 squares, I see that Jorge traveled 1.75 miles, which is more than 1.6 miles.

Reflect

How do you think you did on this practice? **Answers may vary.**

How do you think you did on this practice? **Answers may vary.**

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 5 Students may focus on adding only the tenths place and forget to add the hundredths place on the decimal grid. Remind students that the second decimal place after the decimal relates to hundredths. Also, encourage them to say the decimals out loud in order to remember to add all of the numbers.

Practice Item Analysis

Item	DOK	Rigor
1–8	1	Procedural Skill and Fluency
9–10	3	Application
11–12	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How do you think like a mathematician when adding decimals?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you worked to show others that you value their ideas?

Students reflect on how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain how to use various strategies to add decimals.
- I can demonstrate how to use various strategies to add decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Add decimals with different number of decimal places using decimal grids	5.NBT.B.7
2	2	Add decimals with different number of decimal places using decimal grids	5.NBT.B.7
3	3	Add decimals with different number of decimal places using decimal grids	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 3 or 4 Then have students do

3 of 3 Additional Practice or any of the **A** or **B** activities

2 of 3 *Take Another Look* or any of the **C** activities

1 or fewer of 3 Small Group Intervention or any of the **D** activities

Key for Differentiation

- A** Reinforce Understanding
- B** Build Proficiency
- C** Extend Thinking



Lesson 4-3
Exit Ticket

Name: _____

1. Which equation is shown by the decimal grid?

A. $7 + 0.02 = 1.5$ B. $0.02 + 0.07 = 0.02$
 C. $1.0 + 0.02 = 1.02$ D. $7 + 0.07 = 1.07$

2. Which is $0.4 + 0.25$ on the decimal grid below?

A. 0.75 B. 1.15
 C. 1.75 D. 4.75

3. A frog jumped 175 meters. Then the frog jumped another 288 meters. What is the total distance that the frog jumped?

1,063 meters

Reflect On Your Learning

No confidence Getting better Getting good I can teach someone else.

Assessment Source: 4-3-3

R Reinforce Understanding

SMALL GROUP

Addition Relay

Create a set of index cards labeled 0.14, 0.72, 0.08, 0.4, and 0.56. Have a student draw two cards and add their numbers. Another student draws a card and adds its number to the sum. Continue until all cards have been drawn. Help students to use decimal grids, if necessary, to model the addition. Repeat with new numbers if students need further reinforcement.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Add Tents and Hundredths Race
Students practice adding decimals.

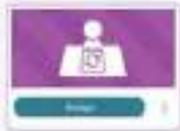


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Represent Adding and Subtracting (Tenths and Hundredths)



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 25

Lesson 4.2 Reinforce Understanding
Represent Addition of Tenths and Hundredths

Review

Use simplified drawing to find the sum of decimal numbers.

Sum: $1.24 + 0.46$

Draw 10: Draw 100: $1.24 + 0.46 = 1.70$

Draw 1000: $1.24 + 0.46 = 1.70$

Use the blocks to add using simplified drawing.

1. $3.5 + 3.28 = 6.78$

2. $3.04 + 3.7 = 6.74$

3. $1.6 + 0.2 = 1.8$

4. $0.75 + 0.23 = 0.98$

INDEPENDENT WORK

Student Practice Book, pp. 25–26

Lesson 4.2
Additional Practice

Review

Use tent and hundredths and hundredths using decimal grids.

The distance between a soccer field is approximately 0.8 miles. There is a parking lot for 0.3 miles. What is the distance between the school and the parking lot?

You can represent the problem with the equation $0.8 + 0.3 = 1.1$ miles or the number of tenths = number of hundredths, 8 tenths = 80 hundredths, and 30 = 300 (use decimal grid) or use

The distance between the school and the parking lot is 1.1 miles.

Use decimal grids to find each sum. Ex. 1–2 sample shading shown.

1. $0.7 + 0.28 = 0.98$ $0.7 + 0.28 = 0.98$

2. $0.22 + 0.1 = 0.32$ $0.22 + 0.1 = 0.32$

Own It! Digital Station**Build Fluency Games**

Assign the digital game to develop fluency with adding and subtracting decimals.

**Spiral Review**

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.

**Student Practice Book, pp. 25–26**

Use hundred grids to solve.

1. $0.2 + 0.19 = 0.39$ 4. $0.36 + 0.3 = 0.66$

2. A frog jumped 0.2 meters and then jumped 0.08 meters. What is the total distance that the frog jumped? **0.28 meters**

3. Don is buying school supplies at the bookstore. He buys 1.00 notebook and 0.25 pencil. How much will he pay? **\$1.25**

4. Scott drove 8.8 miles to work during the week. He also drove 0.2 miles to work during the weekend. How many miles did he drive during the week? **9.0 miles**

MATH
MATH
MATH

Math in Motion Activity

Use a hundred grid to represent a decimal. Shade the hundredths. Write the decimal. Then use the hundredths to solve the problem. Show your work on the back of the page.

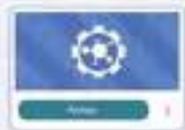
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Use It! Application Station

Let's Get Organized! Students use decimals to measure and create organizers. *The content of this card has concepts covered later in Lesson 4-8. You may want to assign this card to students ready to explore content covered later in this unit.*

**Websketch Exploration**

Assign a websketch exploration to apply skills and extend thinking.

**Differentiation Resource Book, p. 26**

Lesson 4-3 • Extend Thinking

Represent Addition of Tenths and Hundredths

Problem

1. In one week, Carson jumps 0.2 meters in one day and 0.08 meters. How far does he jump in the first week? Use the hundred grid to find the answer. Show your work.

0.28 meters 0.20 meters 0.08 meters 0.28 meters

2. What is the total distance Carson jumps in one week? Use the hundred grid to find the answer. Show your work.

0.28 meters 0.20 meters 0.08 meters 0.28 meters

Math in Motion Activity

Use a hundred grid to represent a decimal. Shade the hundredths. Write the decimal. Then use the hundredths to solve the problem. Show your work on the back of the page.

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Use Partial Sums to Add Decimals

Learning Targets

- I can use strategies to add decimals.
- I can explain the strategy I use to add decimals.

Standards

Major Supporting Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Construct viable arguments and critique the reasoning of others.

MPP Model with mathematics.

Vocabulary

Math Terms

decompose
partial sums

Academic Terms

emphasize
procedure

Materials

The materials may be for any part of the lesson.

- *Decimal Cards* Teaching Resource

Focus

Content Objective

- Students use addition strategies they know, such as partial sums, to add decimals.

Language Objectives

- Students talk about addition strategies they know, such as partial sums, to add decimals while answering *Wh-* questions.
- To support optimizing output, ELs participate in MLR7: Compare and Connect.

SEL Objective

- Students recognize and work to understand the emotions of others and practice empathetic responses.

Coherence

Previous

- Students fluently added and subtracted multi-digit whole numbers using the standard algorithm (Grade 4).
- Students added decimals in hundredths using concrete models, drawings, and strategies based on place value (Unit 4).

Now

- Students extend their understanding of addition strategies to add decimals.

Next

- Students extend their understanding of decimals by representing subtraction of decimals (Unit 4).
- Students fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of addition as they use strategies to add decimals.

Procedural Skill & Fluency

- Students build proficiency in using decomposed numbers to represent decimal addition.

Application

- Students are expected to apply their understanding of addition strategies to add decimals with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Would You Rather?



5–7 min

Build Fluency Students build number sense as they compare numbers to products of multiplication expressions.

These prompts encourage students to talk about their reasoning:

- What strategies did you use to find your answers?
- How can you use estimation to compare the distances?

Purpose Students compare and contrast different expressions to determine which does not belong.

Which Doesn't Belong?

- Which doesn't belong?

Teaching Tip You may want to have students work in pairs as they look at the expressions. This will allow students to collaborate and share ideas.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' exploration of choosing and using strategies they know to add decimals and are based on possible comments and questions that students may make during the share out.

- What types of numbers are represented by the expressions?
- What is similar about all the expressions?
- Can you determine a reason for each expression to not belong?

Math is... Mindset

- How can you recognize and respond to the emotions of others?

Social Awareness: Empathy

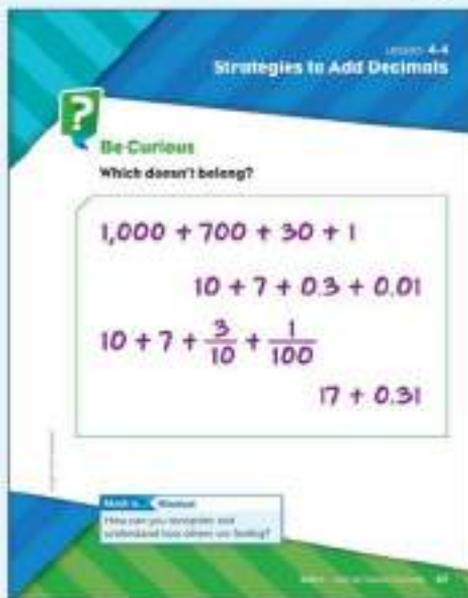
Establish a classroom culture that welcomes openness and empathy by encouraging students to share and discuss their emotions. After students participate in the Which Doesn't Belong? routine, invite them to share the emotions they were experiencing. Encourage students to think about their own experiences with the emotions being shared. Their work throughout the lesson with adding decimals may be challenging, and they may feel emotions such as happy, excited, or frustrated. Sharing and listening can help students build understanding of their own emotions as well as empathy for others.

Transition to Explore & Develop

Ask questions that get students thinking about adding decimals. Ask them to think about ways to add, without using the standard algorithm. Guide students to think about the different strategies they can use to add decimals.

Establish Mathematics Goals to Focus Learning

- Let's think about how we can choose and use strategies we know to add decimals.



LESSON 4-4
Strategies to Add Decimals

Be Curious
Which doesn't belong?

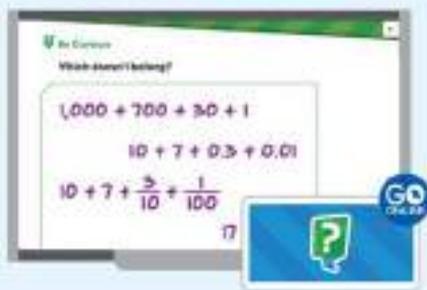
$$1,000 + 700 + 30 + 1$$

$$10 + 7 + 0.3 + 0.01$$

$$10 + 7 + \frac{3}{10} + \frac{1}{100}$$

$$17 + 0.31$$

Math is... Mindset
How can you recognize and respond to the emotions of others?



Be Curious
Which doesn't belong?

$$1,000 + 700 + 30 + 1$$

$$10 + 7 + 0.3 + 0.01$$

$$10 + 7 + \frac{3}{10} + \frac{1}{100}$$

$$17$$

GO ON!

Learn

How can you determine the total cost of the hamburger and salad?

Math is... Modeling

What equation can you use to represent the problem?

How can you use place value to determine the total cost?

One Way Compose by place value.

$10.21 + 12.88 = 23.09$

$10.21 = 10 + 0.2 + 0.01$ $12.88 = 12 + 0.08 + 0.00$

$10 + 12 = 22$ $0.2 + 0.08 = 0.28$ $0.01 + 0.00 = 0.01$

$22 + 0.28 + 0.01 = 22.29$

Another Way Decompose into whole numbers and decimals.

$10.21 + 12.88 = 23.09$

$10 + 12 = 22$ $0.21 + 0.88 = 1.09$

$22 + 1.09 = 23.09$

We can decompose decimals different ways to find partial sums.

Work Together

Michael spent \$3.10 on a hamburger and \$6.99 on a salad. How much did he spend in total?

\$10.09

1 Pose the Problem

Pose Purposeful Questions

- Can you describe the problem in your own words?
- Do you have all of the information needed to solve the problem? How do you know?

Math is... Modeling

- What equation can you use to represent the problem?

Students are using an equation as a representation to help them better understand the problem.

2 Develop the Math

Choose the option that best meets your instructional goals.

Compare and Connect

Pair students and give them an equation to solve similar to the one on the Learn page. Instruct one student to decompose by place value and the other into whole numbers and decimals. Then have them compare their strategies. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- What are some ways to decompose decimals?
- How can you use decomposing decimals to help you add decimals?
- How is this strategy to add decimals similar to the strategies you used to add whole numbers?

Key Takeaways

- Finding partial sums and then adding the partial sums to determine the total is one addition strategy.
- Strategies used to add decimals are the same as those used to add whole numbers.

Work Together

Have students explain how they used partial sums to solve the problem. Invite volunteers who decomposed differently to share their work. Have students look for similarities among the different methods.

Common Error Students may incorrectly decompose by place value. For example, students may add $0.6 + 0.3 + 0.08$, instead of $0.06 + 0.08 + 0.3$, when writing the partial sums for $23.06 + 16.38$.

Language of Math

The term *decompose* is a verb. Ask students to think of some words or phrases that may be used in place of the term. Let students practice using the word correctly to describe their strategies for adding decimals.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students explore different ways to decompose decimal addends.

Materials: *Decimal Cards* Teaching Resource

Directions: Ask students to write an addition problem involving two 3-digit whole numbers and solve the addition using as many different strategies as they can. Invite students to share different strategies they used, focus attention on methods using decomposition, such as partial sums.

- Do you think these strategies will work to add decimals?

Provide copies of the *Decimal Cards* Teaching Resource. Have students select two decimals to write an addition expression. Students should find different ways to decompose the addends to find partial sums.

Support Productive Struggle

- How can you apply your method of decomposing whole numbers to decomposing decimals?
- Is your answer reasonable? How do you know?
- How is finding partial sums when adding decimals similar to finding partial sums when adding whole numbers?

Activity Debrief: Discuss with students that partial sums is one strategy they can use to add decimals. Using this strategy, they can use place value to decompose each addend, find the partial sums, and then add partial sums to calculate the sum of the decimals.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine the total cost of the helicopter and robot?

A PDF of the Teaching Resource is available in the Digital Teacher Center.

Student Cards	
3.86	9.14
2.7	8.01
5.65	7.3
9.43	9.6
6.7	2.23

Guided Exploration

Students extend their understanding of using partial sums to add whole numbers to using partial sums to add decimal numbers.

Facilitate Meaningful Mathematical Discussion

- How can you find an estimate for the sum? What is your estimate?
- **Think About It:** How did you use use partial sums when adding whole numbers?
- How does your understanding of place value and expanded form help you decompose decimal numbers?

Have students discuss different ways to find the partial sums. Ask:

- Which place would you start with? Why?
- Why do you get the same sum if you start with different places?
- How can you assess the reasonableness of the calculated answer?
- How would you decide which strategy to use to add decimals?



English Learner Scaffolds

Entering/Emerging Support students' understanding of cost. First, choose a classroom object, such as a book. Write a price on a sticker or piece of paper and put it on the object. Say *It's \$5.00. The cost is \$5.00.* Repeat the task with a different classroom object. Say *It's \$1.50.* Then prompt them to complete the following sentence saying the correct cost aloud: *The _____ is \$1.50.*

Developing/Expanding Support students' understanding of cost. Choose an object. Say *It's \$5.00. The cost is \$5.00.* Repeat the task with a new object. Say *It's \$1.50.* Prompt students to restate using cost. Finally, ask students to repeat the task, choosing a new object to put a price tag on, and stating its cost.

Bridging/Reaching Ensure comprehension of the meaning of *cost*. Then have students brainstorm other verbs associated with money such as *buy* and *sell*.

On My Own

Name _____

Write to the next like partial sums to solve.

1. $2.37 + 6.6$ 2. $0.9 + 3.33$
 $= 2 + 0.37 + 6 + 0.6$ $= 0 + 0.9 + 3 + 0.33$
 $= \mathbf{9.07}$ $= \mathbf{4.23}$

3. $39.11 + 54.31 = \mathbf{93.42}$ 4. $30.24 + 31.02 = \mathbf{61.26}$

5. $74.50 + 12 = \mathbf{86.50}$ 6. $44.36 + 2.9 = \mathbf{47.26}$

7. Math's team sold 200 raffle tickets. Last year they sold 150 in the ballpark. How many more tickets did they sell this year? **\$50.00**

8. John's suitcase weighs 25 pounds. Maria's suitcase weighs 21.82 pounds. What is the total weight of both suitcases? **46.82 lb**

9. Kim's goal was to run at least 20 miles this week to earn her team's captain title. She Tuesday she ran 3.87 miles and on Wednesday she ran 5.28 miles. Did she reach her goal? Explain. **Yes. Sample answer: She ran 9.15 miles.**

100 • Add and Subtract Decimals

10. 1704 Connection: If students explain the amounts of medication she requires over the course of 3 days, they may identify the medication each day wrong!

How many pills?

Day	Amount of Medication
Monday	32.5
Tuesday	48.25
Friday	21.7

$105.95 \text{ pills}; 32 + 46 + 26 + 7 + 0.6 + 0.2 + 0.1 + 0.05 = 105.95$

10. **Logic:** Sample answer: If you round each decimal to the nearest whole number, the sum is 105, which is greater than the actual sum because both estimations were rounded up.

11. **Area Model:** Use area to find $10 + 10.37$ using $10 + 10 + 4 + 0 + 0.3 + 0.07 + 0.02 + 0.07$.

Is both work correct? Why or why not?

Yes, his work is correct. Sample answer: Scott decomposed the addends by place value. He also decomposed 0.07 into the sum of 0.05 + 0.02 so that 0.07 could be added to 0.02 to make 0.1.

12. **Extend Your Thinking:** How can you use addition properties to subtract 0.04 from 0.12 ?

$0.12 + 0.9 = 1.02$

Sample answer: Rewrite the sum as $0.12 + 0.87 + 0.5$. Add the first two numbers: $0.12 + 0.87 = 1$. Then, add the third number: $1 + 0.5 = 1.5$.

Reflect

Describe one strategy to decompose decimals to find partial sums.

Answer: 1802 1877

Think It Over

How does your strategy for decomposing decimals differ from another's?

100 • Add and Subtract Decimals

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 3–6 Students may use place value incorrectly when decomposing decimals. For example, students may decompose 8.4 as $8 + 0.04$.

Item Analysis

Item	DOK	Rigor
1–6	2	Procedural Skill and Fluency
7–10	3	Application
11–13	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- Describe two ways to decompose decimals to find partial sums.
- Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you worked to recognize and respond to the emotions of others?

Students reflect on how they practiced social awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use strategies to add decimals.
- I can explain the strategy I use to add decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



Use It! Application Station

Cost of Living Depends on Where You Live

Students use equations to compare the cost of living in rural towns and urban cities. *The content of this card has concepts covered later in Lesson 4-8. You may want to assign this card to students ready to explore content covered later in this unit.*



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Student Practice Book, pp. 27–28

Write.

- At the mall, \$1.50 worth of underwear for \$2.00 and 2 pairs of socks for \$1.00 on Wednesday. How much more did you spend on Wednesday? **15.23 dollars**
- A pair grew 12 centimeters one month and 12.75 centimeters the next month. By how many centimeters did the total grow over the two months combined? **18.45 centimeters**
- Tim is a scientist. He grows 1.50 grams of cells every day and 1.55 grams the next day. How far did the group grow during the first two days of the week? **3.05 grams**
- Janita wants to save up \$70.00 for a bicycle. She earned \$12.27 last week by mowing lawns and selling aluminum cans. She earned \$12.08 this month. How many more hours must she mow to reach her goal? **Five. Sample answer: She has earned only \$24.35, which is less than \$70.**

Math in Motion Activity

Use the materials provided to create a story problem that requires you to add or subtract decimals. Write your problem on a separate sheet of paper. Exchange your problem with a partner and solve each other's problems. Be sure to explain your work and check your answers.

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28

Differentiation Resource Book, p. 28

Lesson 4-4 • Extend Thinking

Add Decimals

Write.

The Green Club and Coding Club are having a contest for their school's recycling program. They have saved the greatest number of pounds of old newspapers.

	Months of Use	30-Day Recycling	Ranking	Writing Ranking Name	Amount Saved (Pounds)
Green	24	2.50	1st	24.80	12.00
Coding	25	3.00	2nd	25.64	31

- How many hours did the Green Club members spend in all to win the contest?
75.75 hours. Sample answer: I used partial sums: 24 + 2 + 1 = 24 + 3 = 27; 0.5 + 0.25 + 0.5 = 0.75 + 0.64 = 2.35; 27 + 2.75 = 75.75.
- How many hours did the Coding Club members spend in all to win the contest?
77.07 hours. Sample answer: I used partial sums: 25 + 1 + 4 = 31 + 23 = 75; 0.42 + 0.18 + 0.22 + 0.24 = 2.07; 75 + 2.07 = 77.07.
- Which club won the contest? How do you know?
The Coding Club won. Sample answer: I compared their total number of hours that they volunteered and looked for the greater number. 77.07 > 75.75.

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Represent Subtraction of Decimals

Learning Targets

- I can represent subtraction of decimals less than 1 containing tenths.
- I can represent subtraction of decimals less than 1 containing hundredths.

Standards

Major Supporting Additional

Content

- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

- **MPP** Reason abstractly and quantitatively.
- **MPP** Model with mathematics.
- **MPP** Use appropriate tools strategically.

Vocabulary

Math Term

decimal grid

Academic Terms

assert
prove

Materials

The materials may be for any part of the lesson.

- *Blank Number Lines* Teaching Resource
- number cubes
- *Tenths and Hundredths* Teaching Resource

Focus

Content Objective

- Students use decimal grids to represent subtraction of decimals with the same number of decimal places.

Language Objectives

- Students explain how to use decimal grids to represent subtraction of decimals while answering *Wh-* and using *how much* as needed.
- Support optimizing output, MLR4: Info Gap.

SEL Objective

- Students collaborate with peers and contribute to group effort to achieve a collective mathematical goal.

Coherence

Previous

- Students fluently added and subtracted multi-digit whole numbers using the standard algorithm (Grade 4).
- Students used addition strategies to add decimals (Unit 4).

Now

- Students extend their understanding of decimals by representing subtraction of decimals.

Next

- Students use decimal grids to subtract (Unit 4).
- Students add, subtract, multiply, and divide decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students create and use representations to build their understanding of subtraction with decimals.

Procedural Skill & Fluency

- Students build proficiency with place-value skills and start to develop skills for subtracting decimals through hundredths.

Application

- Students use decimal grids to represent subtraction of decimals with the same number of decimal places.

Application is not a specific element of rigor for this standard.

Number Routine

Which Benchmark Is It Closest To?



5–7 min

Build Fluency

Students build fluency as they find the benchmark numbers nearest to a decimal.

These prompts encourage students to talk about their reasoning:

- What did you think about first when you observed one of the decimals?
- Once you know that a decimal is located between two benchmarks, how do you decide which benchmark it is closer to?
- Is there more than one possible benchmark for 0.5? Explain.
- How is this exercise similar to rounding? How is it different?

Purpose Students discuss real-world applications of showing decimals on a decimal grid.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may want to have students work in pairs as they brainstorm questions. This can help build a collaborative classroom culture. It also allows for greater participation among students as they share their thinking with their partners.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about representing subtraction of decimals and are based on possible comments and questions that students may make during the share out.

- How could you find how many more blue squares there are than orange squares?
- Explain when you have seen a grid like this before.
- What decimal could the yellow squares represent? Explain why.

Math is... Mindset

- How can you justify your thinking?

Relationship Skills: Teamwork

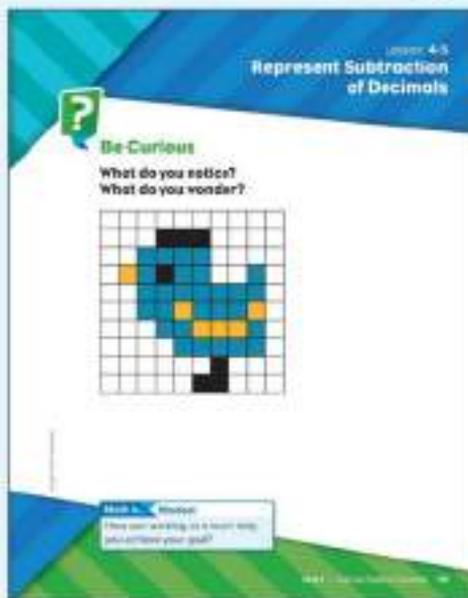
After students work through the Notice & Wonder routine independently, have them share their reasoning with a partner and advocate for their chosen representation. If students have used different representations to Notice & Wonder, or found different solutions, invite them to work together to understand one another's reasoning. Remind students that strong learners are willing to learn from not only their teachers but also their peers.

Transition to Explore & Develop

Ask questions that get students thinking about representing subtraction of decimals.

Establish Mathematics Goals to Focus Learning

- Let's talk about ways we can represent subtraction of decimals.



Lesson 4-5
Represent Subtraction of Decimals

Be Curious
What do you notice?
What do you wonder?

Math is... Mindset
How can you justify your thinking?



Be Curious
What do you notice?
What do you wonder?

GO ON

Learn

The table shows the amounts transported by different means to a local grid.

Mode	Amount
Train	0.4
Coach	0.8
Tractor	0.50
Plane	0.04

How can you determine how much more is shaded red than green? Yellow than purple?

Use a number line to find how much more is shaded red than green.

$0.8 - 0.4 = 0.4$

There is 0.4 more shaded red than green.

Use a decimal grid to find how much more is shaded yellow than purple.

$0.50 - 0.04 = 0.46$

There is 0.46 more shaded yellow than purple.

Use a number line on a decimal grid to solve a problem.

Work Together

How many grams heavier is an ostrich egg than a chicken egg? Explain. **0.50 kg.**

62 squares of a decimal grid are shaded. Then 6 of the shaded squares are marked with an X, leaving 56 shaded squares.

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1 Pose the Problem

LEP Pose Purposeful Questions

- What operation does this problem call for? Why do you think that?
- How do you think you might represent the information you have?

2 Develop the Math

Choose the option that best meets your instructional goals.

IGA Info Gap

Pair students. Provide Partner A with a problem like the one on the Learn page. Provide Partner B with the information to carry out the problem. Instruct Partner B to ask A what information they need, and for A to respond, explaining why they need it. Have students continue until the problem is completed.

3 Bring It Together

LEP Elicit and Use Evidence of Student Thinking

- What are some ways you can represent and solve decimal subtraction problems? Which way do you prefer? Why?
- How is using a representation to subtract decimals similar to using representations to add decimals? How is it different?

Key Takeaway

- Subtraction of decimals can be represented using concrete models or drawings, such as decimal grids.

Work Together

You may wish to provide copies of the *Tenths and Hundredths Teaching Resource* or *Blank Open Number Lines Teaching Resource* for students to use as they solve the Work Together problem.

CEP Common Error Students may get distracted by the 6s in different places in the two masses. Remind them to be careful to consider not just the digit, but the place a digit is in, and the value a digit represents.

LEP Language of Math

Students need multiple opportunities to use key terms so they become part of their active vocabulary. Ask students questions that require the use of *tenths*, *hundredths*, and *variable*.

Activity-Based Exploration

Students will write subtraction expressions and then use models to subtract the decimals.

Materials: number cube (labeled 1–6), *Blank Number Lines* Teaching Resource, *Tenths and Hundredths* Teaching Resource

Directions: Have students roll the number cube to create a decimal number to the tenths with a 0 in the ones place. Roll again to make another decimal number to the tenths. Students write a subtraction expression using the two decimal numbers. Students use decimal grids or number lines to find the difference. Repeat by rolling two number cubes and using the digits to make a decimal number to the hundredths.

Support Productive Struggle

- How did you determine which tool to use to represent the problem?
- Could you have used the hundredths grid to show subtraction of decimals in the tenths? Explain why or why not.
- Explain how you know what you found is the difference.
- How can you show that your calculated difference is reasonable?

Math is... Modeling

- How is each quantity shown on the decimal grid?

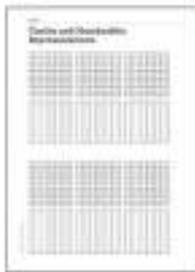
Students discuss how they use decimal grids to represent decimal numbers and decimal subtraction.

Activity Debrief: After students work through their solutions, encourage them to share their strategies and answers with others.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine how much more is shaded red than green? Yellow than purple?

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students use number lines or decimal grids to represent subtraction equations involving decimals to the tenths or hundredths.

Use and Connect Mathematical Representations

- **Think Aloud It:** What have you used to represent subtraction of whole numbers?

Provide copies of *Blank Number Lines* and *Tenths and Hundredths* to students. Ask:

- Which tool would you choose to solve the equation? Why?
- How could you use that tool?
- How will you label the number line? How do you know?
- Where will you place each known value on the number line?
- How can you find the difference between these two decimal numbers on the number line? Is there more than one way?

Discuss with students that there are two ways to show subtraction on a number line. One way is by plotting both known values and counting the difference between those points. Another way is starting at the greater known value and counting back the lesser known value. Ask:

- What are the similarities and differences of these methods?

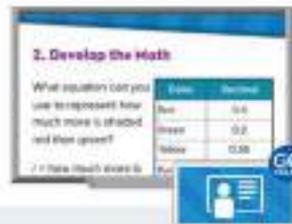
Have students use *Tenths and Hundredths* to solve $0.36 - 0.04$.

- Why did you use the hundredths decimal grid? Could you have used the tenths decimal grid?

Math is... Modeling

- How is each quantity shown on the decimal grid?

Students discuss how they use decimal grids to represent decimal numbers and decimal subtraction.



English Learner Scaffolds

Entering/Emerging Ensure understanding of *How much more...* Cut two pieces of string, different sizes. Give the longer piece to a student. Ask *How much more do you have?* Measure both pieces and say *You have [10 more inches]*. Repeat the task again and ask *How much more do you have?* Give two choices: the correct answer and a distractor that represents the full length of the longer piece.

Developing/Expanding Ensure understanding of *How much more...* Cut two pieces of yarn, different sizes. Give the longer piece to a student. Ask *How much more do you have?* Measure both strings and say *You have [10 more inches]*. Repeat the task again with two new pieces and ask *How much more do you have?* Expect a full sentence response.

Bridging/Reaching Ask students to say what method they like to use to determine how much more of something there is: a number line or decimal grid. Ask them to explain why. Allow students to interject and make corrections as needed. For example: *I don't agree. I prefer to use...because... or I don't think using... I think...*

On My Own

Name _____

What is the difference? Use the decimal grid to label.

Sample shading strategy

1. $0.7 - 0.4 = 0.3$



2. $0.09 - 0.03 = 0.06$



3. $0.64 - 0.38 = 0.26$



4. $0.25 - 0.08 = 0.17$



What is the difference? Use a number line to solve.

5. $0.7 - 0.2 = 0.5$

6. $0.6 - 0.4 = 0.2$

7. Malik has \$0.75. He bought a pencil for \$0.30. How much money left to buy a ruler for \$0.10? Explain.

Yes. Sample answer: Malik has \$0.25 left, so he can buy the ruler.

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3. 1104 Connected: An ocean engineer is comparing the weight of two different oceans. The first ocean weighs 3.8 grams. The second ocean weighs 0.25 grams. How much heavier is the second ocean? **0.07 g**



8. Connected: On Monday, Monday, the 100th anniversary of Tuesday. How much longer did it take to get to Monday than Tuesday? **0.14 km**

10. Money: A decimal that has a sum of 0.68. The first decimal has a sum of 0.24. How much less than the second decimal? What is the sum of the two decimals? **0.21 kg**

12. Money: A decimal that has a sum of 0.78. The first decimal has a sum of 0.25. How much less than the second decimal? **0.29 m**

13. Find Your Thinking: Explain how you solve for the $4.55 - 1.08$ to answer a long division for $4.55 \div 1.08$.

Sample answer: To model $4.55 - 1.08$, you shade the same number of squares and take away the same number of squares as when you model $4.55 \div 1.08$.

Reflect

How do decimal grids and number lines help you subtract decimals?

Assess with exit.

Math Talk: Explain how you solve for $4.55 \div 1.08$ using a number line.

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 8 Students may add instead of subtract because the word “more” is in the question. Remind students that “how much more than” indicates a subtraction problem.

Item Analysis

Item	DOK	Rigor
1–6	2	Procedural Skill and Fluency
7–11	3	Application
12	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How do decimal grids and number lines help you subtract decimals?
- Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you worked to understand your partner’s thinking?
- Students reflect on how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can represent subtraction of decimals less than 1 containing tenths.
- I can represent subtraction of decimals less than 1 containing hundredths.

To review today’s lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK Skill		Standard
1	2	Subtract decimals with the same number of decimal places using decimal grids	5.NBT.B.7
2	2	Subtract decimals with the same number of decimal places using decimal grids	5.NBT.B.7
3	3	Subtract decimals with the same number of decimal places using decimal grids	5.NBT.B.7
4	3	Subtract decimals with the same number of decimal places using decimal grids	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the U or E activities
3 of 4	<i>Take Another Look</i> or any of the U activities
2 or fewer of 4	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- U Build Proficiency
- E Extend Thinking



Lesson 4-5
Exit Ticket

Name: _____

1. Which equation does the number line represent?

A. $0.2 - 0.1 = 0.2$ B. $0.2 - 1 = 0.02$
 C. $0.2 - 1 = 0.2$ D. $0.2 - 0.1 = 0.02$

2. What is the difference? Use the decimal grid to help.

$0.24 - 0.09 = 0.15$

3. Andre bought 0.22 kilograms of almonds and 0.25 kilograms of almonds. How many more kilograms of almonds did Andre buy?

Andre bought 0.23 kilograms

4. Tyler walks 0.4 kilometers to school. He walks 0.2 kilometers home and they walk the remaining 0.4 kilometers to an ice cream shop. How far does Tyler walk to get to Tyler's house?

0.3 kilometers

Reflect On Your Learning

1
No confidence

2
Getting better

3
Confident

4
I can teach someone else.

Assess Answer Book 99

R Reinforce Understanding

SMALL GROUP

Roll It, Subtract It!

Work with students in pairs. One student rolls a number cube and writes the digit rolled as a decimal in tenths. Both students subtract the decimal from 0.7. Help students to use a decimal grid or a number line as needed. Repeat with another roll. Once students are comfortable working with tenths, have them roll twice to create a decimal in hundredths, then subtract from 0.7.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Represent Subtraction of Decimals
Task Cards

Students practice representing subtraction of decimals.



GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Model Subtracting Decimal Numbers



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 29

Lesson 4-5 Reinforce Understanding
Represent Subtraction with Decimals

Name: _____

Review
Use a simplified drawing to find the difference of decimal numbers.
Subtract $0.08 - 0.41$.

Subtract the decimals using a simplified drawing.

1. $0.62 - 0.47 = 0.15$ 2. $0.94 - 0.08 = 0.86$

3. $0.25 - 0.06 = 0.19$ 4. $0.30 - 0.21 = 0.09$

5. James is 2.35 inches taller than Leah. James is 5.26 inches tall. How tall is Leah? **0.79 inches tall**

6. Daniel had 0.75 kilometers on Monday. He ran 0.58 kilometers on Tuesday. How much farther did Daniel run on Monday than Tuesday? **0.05 kilometers**

Differentiation Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 29–30

Lesson 4-5
Additional Practice

Name: _____

Review
Use a simplified drawing to find the difference of decimal numbers.
Subtract $0.75 - 0.48$. How much more money does Will have than Jack?

Use a number line or a decimal grid to find the difference.

1. $0.28 - 0.14 = 0.14$

2. $0.08 - 0.02 = 0.06$

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



Use It! Application Station

Balancing a Checkbook Students research checking accounts and practice balancing a checkbook.

The content of this card has concepts covered later in Lesson 4-7. You may want to assign this card to students ready to explore content covered later in this unit.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Student Practice Book, pp. 29–30

Use a decimal grid to solve each equation.

1. $0.20 - 0.20 = 0.00$ 4. $0.2 - 0.4 = -0.2$

Label

- Janita had a length of string that is 0.8 meter long. She cuts off a piece that is 0.3 meter long. How long is the piece of string she is left with? **0.5 meter**
- She walks 0.42 kilometers to school. How much of the distance is left when she has walked 0.15 kilometers? **0.27 kilometers**
- On Friday, 0.2 meter of rain fell. On Saturday, the amount of rainfall fell only 0.1 meter less than the amount that fell on Friday. How much rain fell on Saturday? **0.1 meter**
- Quinten has 0.65 dollars of money left on his memory card. How much money did he use for the card if he started with 0.25 dollars? **0.40 dollars**

Math @ Home Activity

Use a decimal grid to solve each equation. Label each equation with the number of the problem. Use a decimal grid to solve each equation. Use a decimal grid to solve each equation. Use a decimal grid to solve each equation. Use a decimal grid to solve each equation.

Student Practice Book

Differentiation Resource Book, p. 30

Lesson 4-5 • Extend Thinking

Represent Subtraction with Decimals

Notes:

- Use a hundred grid to find the difference. Estimate the quotient (length of line Tangyria) and the maximum length of each of the other blades of each tower (line Lulu).

Blade of Tower	Maximum length (m)	Difference of
Line Tangyria	0.80	0.00
Line Lulu	0.00	0.00
Line Waver Lake	0.02	0.78
Line Tangyria	0.08	0.72
Line Lulu	0.02	0.78
Line Waver Lake	0.02	0.78

- The Wind-500 tower has a maximum height of 0.70 feet. How much taller is the 0.02 feet tower than the other 0.02 feet tower? How tall is the tower from the maximum of the other? Show your work. **0.02 feet**

Differentiation Resource Book

Represent Subtraction of Tenths and Hundredths

Learning Targets

- I can subtract tenths from hundredths.
- I can subtract hundredths from tenths.

Standards

Major Supporting Additional

Content

- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Model with mathematics.

Vocabulary

Math Term

decimal grid

Academic Terms

accurate

evaluate

Materials

The materials may be for any part of the lesson.

- *Decimal Grids* Teaching Resource

Focus

Content Objective

- Students use decimal grids to represent subtraction of decimals with different number of decimal places.

Language Objectives

- Students discuss using patterns to solve problems while answering *Wh-* questions and using *longer than* and *more*.
- Cultivate conversation, MLR3: Critique, Correct, and Clarify.

SEL Objective

- Students break down a situation to identify the problem at hand.

Coherence

Previous

- Students added and subtracted whole numbers using the standard algorithm (Grade 4).
- Students used representations to subtract decimals (Unit 4).

Now

- Students extend their understanding of subtraction of decimals by using decimal grids to subtract tenths and hundredths.

Next

- Students subtract decimals by decomposing the number being subtracted (Unit 4).
- Students add, subtract, multiply, and divide decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of subtraction of decimals by using decimal grids to represent subtraction.

Procedural Skill & Fluency

- Students build proficiency breaking down decimals into whole parts and decimal parts and writing equivalent names for decimals.

Application

- Students represent subtraction of decimals to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Which Benchmark Is It Closest To?



5–7 min

Build Fluency

Students build fluency as they decide which benchmark each decimal is closest to.

These prompts encourage students to talk about their reasoning:

- How did you determine the nearest benchmark number for each decimal?
- Why did you choose the strategy that you used?
- Is there more than one possible benchmark for 1.5? Explain.
- Once you know that a decimal is located between two benchmarks, how do you decide to which benchmark it is closer?



Purpose Students think about decimals used to represent the lengths of insects.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may want to have students work in pairs to discuss what they notice about the numbers.

1.E.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of using decimal grids to represent subtraction of tenths and hundredths and are based on possible comments and questions that students may make during the share out.

- How are these numbers similar? How are they different?
- How could you represent these numbers?
- How could you represent each of these numbers using the same type of decimal grid?

Math is... Mindset

- How can you identify the information needed to solve a problem?

1.E.1 Responsible Decision-Making: Identify Problems

Help students develop strong learning habits by providing them opportunities to practice responsible decision-making skills. As students consider the Notice & Wonder routine, invite them to share what information is most useful to identify the mathematical task at hand.

Transition to Explore & Develop

Ask questions that get students thinking about subtracting decimals with different number of decimal places. Ask them to think about ways to subtract, without using the standard algorithm. Guide students to think about the different strategies they can use to subtract decimals.

1.E.1 Establish Mathematics Goals to Focus Learning

- Let's think about how we can use decimal grids and other representations to represent subtraction of tenths and hundredths.

Lessons
The table shows different lengths of boards.

Board	Length (in)
Boards	0.7
Art	0.54
Building	0.43
Apex	0.3

How can you find how much longer the art is than the pyramid? The boards? How the building?

You can use subtraction to find the difference in lengths.

Find how much longer the art is than the pyramid.
 $0.54 - 0.24 = 0.30$

Find how much longer the building is than the pyramid.
 $0.43 - 0.13 = 0.30$

Find how much longer the art is than the building.
 $0.54 - 0.24 = 0.30$

Find how much longer the building is than the art.
 $0.43 - 0.13 = 0.30$

Subtracting one length from another gives the difference in lengths. Subtracting identical lengths always subtracts the same amount.

Work Together
Mason is using a string grid to solve $0.94 - 0.6$. How can he solve subtracting 0.01 faster your reasoning? He can draw an X on 60 of the stringed squares. Sample explanation: 0.6 is the same as 0.60.

1 Pose the Problem

Pose Purposeful Questions

- How did you represent subtraction of decimals in earlier problems?
- How is subtraction of these decimals different from decimal subtraction that you have performed in the past?

2 Develop the Math

Choose the option that best meets your instructional goals.

Critique, Correct, and Clarify

Make a false claim for students to critique. Write $0.04 - 0.01 = 0.03$. Point to the equation and say *This equation is correct. Yes or No?* Ask students to correct the statement. Revisit this routine throughout the lesson to provide reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How is the way you use decimal grids to subtract decimals having different numbers of decimal places similar to how you used them to subtract decimals having the same number of decimal places?
- How is it different?

Key Takeaway

- Subtraction of decimals with different number of decimal places can be represented using concrete models or drawings, such as decimal grids.

Work Together

You may wish to provide copies of the *Decimal Grids Teaching Resource* to have students represent the subtraction using a decimal grid.

Common Error Students may subtract 0.06 instead of 0.6. Have them pay close attention to decimal places and zeros.

Language of Math

The term *difference* is a noun. Ask students to think of real-world situations where this word is used. Have students compare this meaning to the mathematical meaning of the word. Let students practice using the word correctly when subtracting decimals, using decimal grids.

Activity-Based Exploration

Students explore using decimal grids to solve subtraction equations involving decimals with tenths and hundredths.

Materials: 10×10 Teaching Resource

Directions: Provide copies of the 10×10 Teaching Resource to each pair or small group. Have students solve the Pose the Problem.

Support Productive Struggle

- How did you determine how to represent 0.3 on a decimal grid showing hundredths?
- Will your strategy for subtracting tenths and hundredths on a decimal grid always work?
- Is there another way to solve the problem?

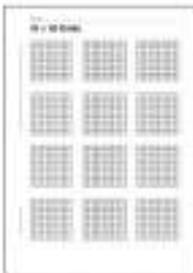
Math is... Perseverance

- How can you use addition to check that the answer is correct?

Students verify that their plans work by checking their answer using another method.

Activity Debrief: After groups work through their solutions, encourage them to share their decimal grids and answers with others. Facilitate a discussion to ensure students understand that when using representations to subtract tenths and hundredths, it is necessary to represent the tenths as an equivalent hundredths.

The PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students extend their understanding of representing subtraction of decimals with different number of decimal places.

Use and Connect Mathematical Representations

- Have the students create the equation.
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution.
 - Will you use rounding or compatible numbers to estimate the solution? Why?
 - How does using a decimal grid to model subtraction of decimals with different numbers of decimal places help you understand the problem?
 - **Think About It:** How can you use equivalent fractions to justify that $0.3 = 0.30$?

Math is... Perseverance

- How can you use addition to check that the answer is correct?

Students verify that their plans work by checking their answer using another method.



English Learner Scaffolds

Entering/Emerging Support students in understanding *lengths*. Put three pencils on the desk, different sizes. Say *Let's find the lengths of the pencils*. Measure each pencil and say *The length is (5 inches)* for each. Repeat with new objects. Finally, show students three more objects and ask them *What are the lengths?* Prompt students to measure each object and say the lengths aloud.

Developing/Expanding Support students in understanding *lengths*. Put three pencils on the desk, different sizes. Say *Let's find the lengths of the pencils*. Measure each pencil and say *The length is (5 inches)* for each. Repeat with new objects. Then ask students to choose three more objects and to tell you their lengths.

Bridging/Reaching Ask students to talk about the different measurements for length that they know. For example, *miles, kilometers, inches*, etc. Then have them sort them into two groups: metric and standard. Discuss with students the abbreviations we use for each. Validate or correct student vocabulary and grammar as needed.

On My Own

Name: _____

What is the difference? Use the decimal grids to solve.

1. $0.94 - 0.1 = 0.84$ 2. $0.9 - 0.00 = 0.90$

3. $1.01 - 0.5 = 0.51$

4. $1.20 - 0.7 = 0.50$

What is the difference? Use decimal grids to solve.

5. $2.3 - 2.17 = 0.13$ 6. $27 - 1.8 = 25.2$

7. $1.9 - 0.8 = 1.1$ 8. $2.25 - 1.2 = 1.05$

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3. 374K Concessions A concession stand has amounts of supplies listed in the table. How much more cash did the concession stand have at the beginning? **0.85 yen.**

Item	Amount
Whiskers	0.15 yen
Lettuce	0.82 yen
Onions	0.03 yen

4. Jim's Weight Jim weighed 100 pounds at the start of the year and 105 pounds at the end of the year. How much more weight did Jim gain? **5.00 lb.**

5. Order Analysis Write numbers 1 through 100 in order from the smallest to the largest. What is the difference between the numbers 1 and 100? **99.** The difference will be greater than 0.5. Sample answers: $0.2 - 0.2 = 0.0$ and $0.88 - 0.88 = 0.0$.

6. Express Your Thinking Use number disks to represent the sum of the expressions $0.9 - 0.5$ and $1.02 - 1.22$. **Sample answers: $0.9 - 0.5 = 0.4$ and $1.02 - 1.22 = -0.2$.**

Reflect

How did decimal grids help you subtract decimals with different numbers of decimal places?
Answers vary.

Math in... Mindset
How does the **Math in... Mindset** video help you practice?

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 1 Students may represent the 0.1 as one colored square in the grid instead of ten because they do not equate 0.1 with ten hundredths. Remind students that the first place after the decimal represents tenths. For some students, using grids to make and compare representations for one one-hundredth and one-tenth may be helpful.

Practice Item Analysis

Item	DOK	Rigor
1–8	2	Procedural Skill and Fluency
9–10	3	Application
11–12	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How did decimal grids help you subtract decimals with different numbers of decimal places?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you practice responsible decision making?

Students reflect on how they practiced responsible decision-making.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can subtract tenths from hundredths.
- I can subtract hundredths from tenths.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Subtract decimals with different number of decimal places using decimal grids	5.NBT.B.7
2	2	Subtract decimals with different number of decimal places using decimal grids	5.NBT.B.7
3	3	Subtract decimals with different number of decimal places using decimal grids	5.NBT.B.7
4	3	Subtract decimals with different number of decimal places using decimal grids	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the ✔ or ✔ activities
3 of 4	<i>Take Another Look</i> or any of the ✔ activities
2 or fewer of 4	Small Group Intervention or any of the ✔ activities

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 4-6
Exit Ticket

Name _____

- Which equation is showing the decimal grid?

$1.07 - 0.25 = 0.82$

A

$1.07 - 0.25 = 0.82$

B

C. $2 - 0.82 = 1.17$ D. $0.5 - 0.25 = 0.25$
- What is the difference? Use the decimal grids to solve.
 $1.07 - 0.25 =$ _____

A. 0.82

B. 0.82
- Mark says 1.8 pounds of bananas are more expensive than the grapes in a fruit basket. How many pounds of bananas does Mark have left?

117 pounds

Reflect On Your Learning

1.00 1.07 1.00 1.07

1.00 pounds 1.07 pounds 1.00 pounds 1.07 pounds

1.00 1.07 1.00 1.07

1.00 pounds 1.07 pounds 1.00 pounds 1.07 pounds

1.00 1.07 1.00 1.07

1.00 pounds 1.07 pounds 1.00 pounds 1.07 pounds

R Reinforce Understanding

SMALL GROUP

How Much More?

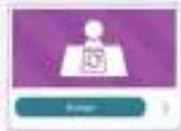
Have students use decimal grids to represent an amount of money between \$1.00 and \$2.00. Give them a price of an item that is less than \$1.00. Have students then use the decimal grids to determine how much more money they have than the cost of the item. Remind students to place the decimal point correctly in their answers. Repeat for different item prices.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Represent Adding and Subtracting (Tenths and Hundredths)



INDEPENDENT WORK

Differentiation Resource Book, p. 31

Lesson 4-6 Reinforce Understanding

Represent Subtraction of Tenths and Hundredths

Review

Use a simplified drawing to find the difference of decimal numbers.

Subtract $2.8 - 0.25$.

$2.8 - 0.25 = 2.55$

Subtract the decimals using a simplified drawing.

1. $2.8 - 0.25 = 2.55$

2. $3.75 - 4.2 = -0.45$

3. $5.8 - 1.8 = 4.0$

4. $3.36 - 0.27 = 3.09$

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Subtract Tens and Hundredths Race
 Students practice subtracting decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 31–32

Lesson 4-6

Additional Practice

Review

Use ten subtraction problems that have different place values.

Estimate, then subtract. Write the number and label the answer.

1. $2.8 - 0.25 = 2.55$

2. $3.75 - 4.2 = -0.45$

3. $5.8 - 1.8 = 4.0$

4. $3.36 - 0.27 = 3.09$

Use decimal grids to solve each equation.

1. $2.8 - 0.4 = 2.4$

2. $0.8 - 0.1 = 0.7$

3. $1.7 - 0.5 = 1.2$

4. $1.8 - 0.3 = 1.5$

Student Practice Book

Strategies to Subtract Decimals

Learning Targets

- I can use strategies to subtract decimals.
- I can explain the strategy I use to subtract decimals.

Standards

Major Supporting Additional

Content

- 5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Construct viable arguments and critique the reasoning of others.

MPP Use appropriate tools strategically.

Vocabulary

Math Term

decompose

Academic Terms

analyze

prove

Materials

The materials may be for any part of the lesson.

- Blank Open Number Lines* Teaching Resource
- Decimal Cards* Teaching Resource

Focus

Content Objective

- Students can use subtraction strategies they know, such as partial differences and the relationship between addition and subtraction, to subtract decimals.

Language Objectives

- Students discuss subtraction strategies while answering *Wh-* and *Yes/No* questions and using adjectives such as *efficient* and *easier*.
- Support optimizing output, MLR7: Compare and Connect.

SEL Objective

- Students recognize personal strengths through thoughtful self-reflection.

Coherence

Previous

- Students added and subtracted whole numbers using the standard algorithm (Grade 3).
- Students used representations to subtract tenths and hundredths (Unit 4).

Now

- Students subtract decimals by decomposing the number being subtracted.
- Students connect subtraction to addition by counting up on a number line to find the difference.

Next

- Students use adding and subtracting decimals to solve real-world problems (Unit 4).
- Students add, subtract, multiply, and divide decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of subtraction as they notice similarities between subtracting whole numbers and subtracting decimals.

Procedural Skill & Fluency

- Students build proficiency with subtraction facts and strategies for subtracting decimals.

Application

- Students use subtraction strategies, such as partial differences to subtract decimals.

Application is not a specific element of rigor for this standard.

Number Routine

Can You Make the Number?

5–7 min

Build Fluency Students build number sense and procedural fluency as they determine combinations of numbers using different operations to make the target number 10.

Remind students that each number can only be used once, but operations can be used as many times as they want.

Sample answers include $(4 \times 2 + 8 - 6) \div 1$, $(4 + 6 + 8) \div 2 + 1$, $(6 - 4) \div 2 + 1 + 8$, $6 \div (4 \div 2 + 1) + 8$, $4 - (6 \div 2) + 1 + 8$, and $(4 \div 2) \times 8 - (6 \times 1)$.

These prompts encourage students to talk about their reasoning:

- What is a different way to make the target number?
- How is order of operations used in making 10?
- How can we make the target number using all four operations?

Purpose Students look for connections among whole-number addition and subtraction equations.

Which Doesn't Belong?

- Which doesn't belong?

Teaching Tip You may want to have students write related addition and/or subtraction equations for each equation.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of what strategies could be used to subtract decimals and are based on possible comments and questions that students may make during the share out.

- How could you assess if the calculated sums and differences given are reasonable?
- Which of the equations are related? How do you know?
- What strategies would you have used to solve these addition and subtraction equations?

Math is... Mindset

- How can you stay focused on your math work?

Self-Awareness: Recognize Strengths

Before students begin the Which Doesn't Belong routine, invite them to think about their personal areas of strength in math. In addition to specific math skills, students may also acknowledge personal strengths that can help them with their learning, such as listening, staying focused, or explaining. As students work with strategies to subtract decimals throughout the lesson, model giving positive feedback to help them acknowledge their personal strengths. Encourage students to recognize and acknowledge the strengths of their peers.

Transition to Explore & Develop

Ask questions that get students thinking about the uses of estimates. Guide the discussion to have students think about how to subtract decimal numbers. If students bring up decomposing the number or representing the number with pictures organically, bring that into the discussion, but if students do not introduce the concept during this part of the lesson, they will be reminded of it in the Explore & Develop.

Establish Mathematics Goals to Focus Learning

- Let's think about strategies we can use to subtract decimals.



Lesson 4.7
Strategies to Subtract Decimals

Be Curious
Which doesn't belong?

$$400 - 240 = 160$$

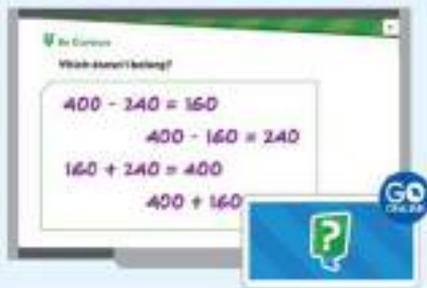
$$400 - 160 = 240$$

$$160 + 240 = 400$$

$$400 + 160 = 560$$

Math is... Mindset
How can you stay focused on your math work?

Self-Awareness: Recognize Strengths
How do you feel about your strengths in math?



Be Curious
Which doesn't belong?

$$400 - 240 = 160$$

$$400 - 160 = 240$$

$$160 + 240 = 400$$

$$400 + 160 = 560$$

GO ON!

Learn
How can you determine how much more gravitational energy Washington receives than Salem, Oregon?

How Way Decompose by place value to subtract.

$$\begin{array}{r} 24.97 - 19.23 = 6 \\ 24.97 - 19 = 5.97 \\ 5.97 - 19 = 4.97 \\ 4.97 - 19.23 = 4.74 \end{array}$$

Another Way Count on a number line to subtract.

$$19.23 + 6 = 25.23$$

Work Together
Find the difference and explain your strategy.
 $67 - 32.64$
24.38 Check students' strategies.

1 Pose the Problem

Pose Purposeful Questions

- What representations did you use to understand subtraction of whole numbers?
- What strategies did you use to subtract whole numbers?
- How did you choose what strategy you used to subtract whole numbers?

2 Develop the Math

Choose the option that best meets your instructional goals.

Compare and Connect

Pair students and give them an equation to solve similar to the one on the Learn page. Instruct one student to solve using partial differences and the other using counting. Then have them compare their strategies. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How would you explain how to decompose number to subtract decimals to a friend?
- How does a related equation help you subtract decimals?
- How are the strategies used to subtract decimals the same as the strategies used to subtract whole numbers? How are they different?

Key Takeaways

- One subtraction strategy is to decompose one decimal by place value and then subtract the decomposed parts from the total.
- Rewriting a subtraction equation as a related addition equation is another strategy for finding the difference.
- Strategies used to subtract decimals are the same as those used to subtract whole numbers.

Work Together

You may wish to provide copies of *Blank Open Number Lines* Teaching Resource for students to use as they solve the Work Together problem.

Common Misconception Students may want to decompose both the decimal numbers to subtract, which can result in a negative partial difference that students are not yet prepared to handle. Remind students that, during problem solving, they should ask themselves "Do I need to try a different way to solve this?" and persevere with another plan when they encounter something they are not yet prepared to handle.

Language of Math

Have students connect *related equations* to people who are *related* to them.

Activity-Based Exploration

Students explore different strategies to subtract decimal numbers.

Materials: *Blank Open Number Lines, Decimal Cards*

Directions: Ask students to write a subtraction problem involving two 3-digit whole numbers and solve the subtraction using as many strategies as they can. Invite students to share what they used.

- Do you think these strategies will work to subtract decimals?

Provide copies of *Decimal Cards* and *Blank Open Number Lines*. Have students select two decimals to write a subtraction expression. Students explore applying their strategies to subtract decimals.

Support Productive Struggle

- How can you apply your method of decomposing whole numbers to decomposing decimals?
- How is decomposing to subtract decimals similar to decomposing to subtract whole numbers? How is it different?
- How is counting on to subtract decimals similar to counting on to subtract whole numbers? How is it different?

Math is... Choosing Tools

- Is your calculated answer reasonable? How do you know?

Students detect possible errors by strategically using estimation and other mathematical knowledge.

Activity Debrief: Discuss with students that decomposing and counting on are strategies they can use to solve subtraction problems involving decimals.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine how much more precipitation Olympia, Washington receives than Salem, Oregon?

The PDF of the Teaching Resource is available in the Digital Teacher Center.

Problem Type		
	3.86	9.14
	2.7	8.01
	5.65	7.3
	9.13	9.6
	6.7	2.23

Guided Exploration

Students extend strategies they learned for subtracting whole numbers by decomposing the second number. They also connect subtraction to addition by counting up on a number line to find the difference between decimals.

Facilitate Meaningful Mathematical Discourse

- Have the students estimate the solution. Ask:
 - Will you use rounding or compatible numbers to estimate? Why?
- **Think About It:** What strategies do you know for subtracting whole numbers?
- **Think About It:** Will you get the same answer if you decompose 19.29 into 19 and 0.29? Explain.
- Have the students create the equation.
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution.
 - Will you use rounding or compatible numbers to estimate? Why?
- **Think About It:** How did you use counting on to find the difference of whole numbers?
- Does one of the strategies seem more efficient than the other? Why?
- Describe a situation where it would be easier to use one of the strategies than the other.

Math is... Choosing Tools

- Is your calculated answer reasonable? How do you know?

Students detect possible errors by strategically using estimation and other mathematical knowledge.



English Learner Scaffolds

Entering/Emerging Support students' understanding of the *difference*. Put 30 counters on the desk. Say *I have 30 counters*. Then say *I'm going to take away 17*. Remove 17. Say *I'm going to find the difference*. Count the 13 counters left. Say *The difference is 13*. Repeat twice, and after the third time, instead of providing the difference, say *Find the difference*. Correct as needed.

Developing/Expanding Support students' understanding of the *difference*. Put 30 counters on the desk. Say *I have 30 counters*. Then say, *I'm going to take away 17*. Remove 17. Say *I'm going to find the difference*. Count the 13 counters left. Say *The difference is 13*. Repeat twice, and then ask students to repeat the task themselves. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to discuss the different meanings and uses of *difference*. For example, the difference between two quantities, the difference in appearance or use between two objects, differences of opinion or meaning, etc. Validate and correct student vocabulary and grammar as needed and allow students to use a dictionary if desired.

R Reinforce Understanding

SMALL GROUP

Quality over Quantity

Give students a subtraction problem with decimals (decimal places to tenths). Encourage students to find the answer both quickly and correctly. Have students share the strategies they used to find the answer. If necessary, review how to find differences using number lines and partial differences.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Adding and Subtracting (Partial Sums and Differences)



INDEPENDENT WORK

Differentiation Resource Book, p. 33

Lesson 4.7 Reinforce Understanding
Strategies to Subtract Decimals

Name: _____

Review
Use partial differences to find the difference.

$35.2 - 4.36 = 7$	Decrease 4.36 to place value and subtract.
$35.2 - 4 = 31.2$	
$31.2 - 0.3 = 30.9$	
$30.9 - 0.36 = 30.54$	

Find the difference. Show your work.

1. $75.3 - 9.5 = 65.8$	2. $68.2 - 0.06 = 68.14$ The difference is 68.14.
3. $46.92 - 5 = 41.92$	4. $35.82 - 0.7 = 35.12$ The difference is 35.12.
5. A rectangular strip of dog food is 20.32 kg long. Its width was 8.24 kilograms. When the dog gets home for another checkup, it weighed 6.00 kilograms. How much weight did the dog gain? Show your work. 4.28 kilograms	

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Decimal Subtraction Tic Tac Toe
Students practice subtracting decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 33–34

Lesson 4.7
Additional Practice

Name: _____

Review
Use two strategies to subtract decimals.

Chris has \$11.76 and Dan has \$10.20. How much more money does Chris have than Dan?
The answer is \$1.56 = 15.6¢

Use partial differences. Decreasing 10.20 to place value and subtract. $10.20 - 10 = 0.20$ $0.20 - 0.20 = 0.00$	Use counting on. $10.20 + 1 = 11.20$ $11.20 + 0.4 = 11.60$ $11.60 + 0.20 = 11.80$
--	--

Chris has \$7.54 and Dan has \$6.00.

Find each difference. Show your work.

1. $4.24 - 1.8 = 2.44$	2. $6.8 - 0.07 = 6.73$
3. $41.92 - 5 = 36.92$	4. $35.82 - 0.7 = 35.12$

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Use It! Application Station

Balancing a Checkbook Students research checking accounts and practice balancing a checkbook.



Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



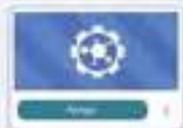
Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Student Practice Book, pp. 33–34

Find each difference. Explain your method.

- $34.92 - 0.75 = 34.17$
Sample answer:
 I decomposed 0.75: $34.92 - 0.75 = 34.17$
 $34.92 - 0.75 = 34.17$
- $1.05 - 0.28 = 0.77$
Sample answer:
 I counted up from 12.88: $12.88 + 0.12 = 13.00$
 $13.00 + 0.57 = 13.57$
 $13.57 - 0.80 = 12.77$

Spine

- A box of books weighs 22.38 pounds. After taking out some of the books, the box now weighs 20.75 pounds. How many pounds of books did you take out of the box? **16.63 pounds.**
- Heidi has read 1.32 kilometers more than her brother every week. The school is 12 kilometers from the city center. How many kilometers does Heidi have left to ride her bike to the school? **1.68 kilometers.**

Math @ Home Activity

Use a calculator to compare the two methods. Write your answer and show your work. Explain how you checked your answer. Write a word problem that uses the two methods. How many answers will you give your teacher?

Student Practice Book

Differentiation Resource Book, p. 34

Lesson 4.7 • Extend Thinking

Strategies to Subtract Decimals

Notes:

Read a story about money to buy a video game that costs \$22.50. How much less the total money you have than the cost of the game? How much more money do you need to buy the game?

Flowers	Week 1	Week 2	Week 3	Week 4
Cost	\$1.20	\$1.50	\$1.80	\$2.00
Revenue	\$1.17	\$1.48	\$1.78	\$1.98

- How much more money does Sarah need to buy a video game that costs \$22.50? Explain how you used a strategy to find the answer.
Sample answer: First, I added the amount of money she has saved. Sarah has saved \$42.50. Then I subtracted the total amount she has \$42.50. Sarah needs \$22.50 more to purchase the video game.
- Sarah plans to buy the video game in 4 more weeks. How much will she need to save each week to be able to buy the game? Explain how you used a strategy to find the answer.
Sample answer: Sarah has \$42.50 and will save \$8.50 next week. $\$42.50 + \$8.50 = \$51$. Subtract the amount from the cost: $\$22.47 - \$51.00 = \$28.53$. Sarah will have to save \$28.53 during each of the 4 weeks.
- April plans to save for 4 weeks to buy a video game. Her math journal data are shown below. Explain how you used a strategy to find the answer.
Sample answer: Sarah has \$62.80 and will save \$8.50 next week and \$8.50 the following week. $\$62.80 + \$8.50 + \$8.50 = \80.00 . Subtract the cost of the video game from this amount: $\$20.00 - \$80.47 = \$1.03$. Sarah will have \$1.03 left over.

Differentiation Resource Book

Explain Strategies to Add and Subtract Decimals

Learning Targets

- I can explain strategies for adding and subtracting decimals.
- I can add and subtract decimals to solve problems.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms

decomposition
partial sums

Academic Terms

evaluate
procedure

Materials

The materials may be for any part of the lesson.

- Explain and Show Your Strategies* Teaching Resource

Focus

Content Objective

- Students can explain their choice of strategy to solve.

Language Objectives

- Students talk about their choice of strategy to solve a problem while answering *Wh-* questions and using the adjective *efficient*.
- To support maximizing linguistic and cognitive meta-awareness, ELs participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing thoughtful and constructive feedback.

Coherence

Previous

- Students fluently added and subtracted multi-digit whole numbers using the standard algorithms (Grade 4).
- Students subtracted decimals by decomposing the number being subtracted (Unit 4).

Now

- Students extend their understanding of adding and subtracting decimals and solving real-world problems involving the sum and difference of decimals to explain the strategy used to solve.

Next

- Students fluently multiply multi-digit whole numbers (Unit 5).
- Students fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of adding and subtracting decimals as they use representations and models to explain the strategy used to find the sum or difference of decimals.

Procedural Skill & Fluency

- Students build proficiency with strategies for adding and subtracting decimals.

Application

- Students apply their understanding of addition and subtraction of decimals to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Can You Make the Number?

5–7 min

Build Fluency Students build number sense and procedural fluency as they determine combinations of the numbers using different operations to make the target number 16.

Remind students that there is more than one solution to the problem.

Remind students that each number can only be used once, but operations can be used as many times as they want.

Sample answers include
 $(8 - 6) \times (4 \times 2) \times 1$,
 $(6 + 8 + 4 - 2) \times 1$, and
 $((4 + 2) \div 6 + 1) \times 8$.

These prompts encourage students to talk about their reasoning:

- What is a different way to get the target number?
- How can we make the target number using all four operations?



Purpose Students think about a numberless word problem and the strategies they might use to solve it.

Numberless Word Problem

- What could you ask?
- What math do you use in this problem?

Teaching Tip You may want to have students work in pairs to discuss the numberless word problem.

1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about choosing and using strategies to add and subtract decimals and are based on possible comments and questions that students may make during the share out.

- What strategy would you use to solve this problem if it involved whole numbers only?
- How would your strategy change, if the problem involved decimals?

Math is... Mindset

- How can you show others you respect their ideas?

2.1 Social Awareness: Respect Other

As students work with partners to complete the Numberless Word Problem routine, remind them to show respect by listening attentively when others are sharing their ideas. Provide models of constructive and respectful feedback to guide students. As students share what they know and do not know about the problem, encourage classmates to provide thoughtful feedback to one another. Remind students that respecting others is an important part of being a member of the class community.

Transition to Explore & Develop

Ask questions that get students thinking about strategies and models used to add and subtract decimals. Guide students to think about how they can explain strategies used to solve real-world problems involving decimal sums and differences.

1.1 Establish Mathematics Goals to Focus Learning

- Let's think about choosing and using strategies to add and subtract decimals.

LESSON 4-8
Explain Strategies to Add and Subtract Decimals

Be Curious

Rose is participating in a bike-a-thon. She stops to eat at a rest stop after riding a certain distance. How much farther does Rose have to go?

Math is... Mindset
How can you show others you respect their ideas?

Be Curious

Rose is participating in a bike-a-thon. She stops to eat at a rest stop after riding a certain distance. How much farther does Rose have to go?

GO
4-8.2B

Learn

How is participating in a 50-kilometer triathlon like solving the steps to find all a cost that after 30.2 kilometers, how much more does Sam have to go?

You can use an bar diagram to represent the problem.

You can use a number line equation to represent the problem.

You can use different strategies to solve.

Decompose by place value. Count on by subtract.

Use the distributive property to solve.

Round the answer to the nearest hundredth.

Review the strategy that is most efficient based on the problem.

Work Together

Join distributed how much more Sam has to go. Use the bar diagram, number line, or equation to solve.

\$9.98: Check students' work.

1 Pose the Problem

Pose Purposeful Questions

- How do you know what operation is needed to solve the problem?
- In what ways can you represent this problem?
- What strategies have you learned? Which one would you use to solve this problem?

2 Develop the Math

Choose the option that best meets your instructional goals.

Co-Craft Questions and Problems

Pair students and have them co-create a problem similar to the one on the Learn page. Have them work together to solve their problem and then trade their problem with another pair. After each pair solves the other pair's problems, have them form a group of four to check solutions and correct any mistakes that may have been made. Revisit the routine throughout the lesson for reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How do you choose which strategy you use when solving a problem involving the addition or subtraction of decimals?

Key Takeaway

- Any of the addition or subtraction strategies can be used to determine a sum or difference.

Work Together

You may wish to provide copies of the *Show and Explain Your Strategies* Teaching Resource for students to use to solve the Work Together problem.

Common Misconception Students may assume the only strategies they can use are ones explicitly discussed in the lessons. Students could use the adjusting numbers strategy, by seeing that the cost of each game is \$0.01 less than \$5. So, the sum must be \$0.02 less than \$10.

Language of Math

The term *representation* is a noun. Ask students to think of real-world situations where this word is used. Have students relate this meaning to a mathematical representation. Let students practice using the word correctly when explaining how to represent and solve problems involving decimal sums and differences.

Activity-Based Exploration

Students explore different strategies to solve real-world problems involving decimals.

Materials: *Explain and Show Your Strategies* Teaching Resource

Directions: Provide copies of the *Explain and Show Your Strategies* Teaching Resource. Have students solve the Pose the Problem using two different strategies.

Support Productive Struggle

- Which strategy did you use first? Why did you decide to start with that strategy?
- Was there a strategy that didn't work? Why do you think it didn't work?
- What is the same about your two strategies? What is different?

Math is... Choosing Tools

- Explain why you find one strategy more efficient than another.

Students make decisions about when tools might be helpful, recognizing both the knowledge to be gained and their limitations.

Activity Debrief: Discuss with students that problems can be solved using any known strategy. Some addition and subtraction strategies may be more efficient than others due to the quantities within the problem.

The PDF of the Teaching Resource is available in the Digital Teacher Center.

Guided Exploration

Students extend their understanding of adding and subtracting decimals by using various strategies.

Use and Connect Mathematical Representations

- How does the bar diagram represent the problem?

Have students create the equations.

- How should the numbers appear in the equations? Why?
- How should the unknown appear in the equations? Why?

Offer different eTools that the students may use to aid and assist them in finding the solution. Have students work with a partner to discuss strategies for solving. Ask:

- Which tool would you use? Explain why.
- **Think About It:** Which strategies would not be efficient for solving $50 - 30.2 = d$?

Math is... Choosing Tools

- Explain why you find one strategy more efficient than another.

Students make decisions about when tools might be helpful, recognizing both the knowledge to be gained and their limitations.



English Learner Scaffolds

Entering/Emerging Support students' understanding of *farther*. Place two objects such as two chairs across from your desk, with one chair being farther away than the other. Point to the chair that's farther away from you and say, *That chair is farther*. Repeat with two more pairs of objects. Then, choose two more pairs of objects, and ask students, *Which [book] is farther?*

Developing/Expanding Support students' understanding of *farther*. Place two objects across from your desk, with one being farther away than the other. Point to the object that's farther away and say *That (chair) is farther*. Repeat with two more pairs of objects. Then prompt students to choose two objects to compare and tell you which one is farther away from where they're standing.

Bridging/Reaching Have students compare and contrast the words *far* and *farther* and *close* and *closer*, and how they relate to distance. Allow students to intersect, agreeing or disagreeing. For example, *Are you sure farther means... or I'm not sure about that. I think that if something is closer...*

On My Own

Name _____

What is the sum of differences? Explain how you decomposed whole strategy to use. **Check students' explanations.**

1. $20 + 30 = 50$ 2. $50 - 30 = 20$

3. $100 + 0.05 = 100$ 4. $502 - 14 = 472$

5. $15 - 10 = 5$ 6. $319 + 20 = 339$

7. **Can't tell** (students might think 1000 grams is 1000 pounds, which is not true). **Check students' explanations.**

8. **Any three** (e.g., 100 miles on Monday and 100 miles on Tuesday, 100 miles on Wednesday and 100 miles on Thursday). **Check students' explanations.**

9. **34.88** to check students' explanations. 10. **2.16** to check students' explanations.

1104 • Unit 4 • Add and Subtract Decimals 126

8. 1104 Connection

As a mathematician, explain to your friend how to solve this problem. How much more does one gram weigh than one kilogram? **0.999** kg

City of origin	London's Total
London	1000 km
Tokyo	1021 km
Washington	1049 km

10. A challenging problem In a classroom measuring 120 ft, students are lined up and 3 ft apart. How far apart are the centers of the centers? **45.5 ft**

11. Shared Your Thinking How would you find the sum of 75 and 225? Explain how to use a similar strategy for the fraction of 1/6 + 1/3.

Sample answer: You can add 75 + 25 to make 100, then add 100 + 100 + 100 to find a sum of 300. You can add 0.75 + 0.25 to make 1, then add 1 + 1 + 1 to find a sum of 3.

12. The answer did not check Explain to your friend why they spent 325 ft of their legs (12 1/4 ft) on a mountain bike. They did have 8 ft left. How much is their leg left? **315 ft**

8. Reflect

How did you solve this problem? What strategy did you use? **Answers will vary.**

8.1104 Connection Explain to your friend how to solve this problem. How much more does one gram weigh than one kilogram?

1104 • Unit 4 • Add and Subtract Decimals 126

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 7–10 Students may use the wrong operation to solve. For example, for Exercise 8, students may solve $13.4 + 11.25$. Students may also incorrectly decompose a decimal. In Exercise 7, students may incorrectly break apart 15.6 as the sum of $15 + 0.06$.

Practice Item Analysis

Item	DOK	Rigor
1–6	2	Procedural Skill and Fluency
7–10	3	Application
11	4	Conceptual Understanding
12	3	Application

Reflect

Students complete the Reflect question.

- How did you think like a mathematician when selecting which strategy to use?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you shown others you respect their ideas?

Students reflect on how they practiced social awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain strategies for adding and subtracting decimals.
- I can add and subtract decimals to solve problems.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	3	Explain strategy to add decimals	5.NBT.B.7
2	3	Explain strategy to add decimals	5.NBT.B.7
3	3	Explain strategy to add decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the P or F activities
2 of 3	<i>Take Another Look</i> or any of the G activities
1 or fewer of 3	Small Group Intervention or any of the I activities

Key for Differentiation

- P Reinforce Understanding
- G Build Proficiency
- F Extend Thinking



Lesson 4-8
Exit Ticket

Name _____

What is the sum or difference? Use a strategy to solve.

- Ali's garden was 0.06 meters long. She made it 1.50 meters longer. What is the length of Ali's garden now?
1.56 meters
- Tyler's class does a science experiment. They use 0.22 liter of extra solution and 0.07 liter of water. How much solution is there after mixing the two solutions?
0.29 liter
- Kevin weighs 44 kilograms and is going to add 10 for his brother. His brother weighs 2.25 kilograms of water after the accident. How many kilograms of fabric will weigh in the accident?
3.25 kilograms

Reflect On Your Learning

1. Yes () No ()

2. Yes () No ()

3. Yes () No ()

4. Yes () No ()

5. Yes () No ()

R Reinforce Understanding

SMALL GROUP

Raise the Bar

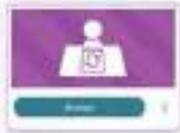
Provide students with a bar diagram that represents a decimal sum or difference such as $4.2 + 11.5$ or $15.1 - 3.7$. Each student writes the addition or subtraction expression that goes with the bar diagram and a real-world problem that may be represented by the model. If students have difficulty getting started, ask them what numbers are involved and whether they are combining the numbers (adding) or separating the numbers (subtracting). Have students share their expression and problem with the group. Have the group discuss strategies to use to solve each problem.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Represent Adding and Subtracting (Tenths and Hundredths)
- Adding and Subtracting (Partial Sums and Differences)



INDEPENDENT WORK

Differentiation Resource Book, p. 35

Lesson 4.8 Reinforce Understanding
Explain Strategies to Add and Subtract Decimals

Name: _____

Review
 You can use partial differences to subtract decimal numbers.

$17.24 - 5.47$

Decompose by 5.47 (one whole and tenths).

$17.24 - 5 = 11.77$
 $11.77 - 0.4 = 11.37$
 $11.37 - 0.07 = 11.30$

Solve each equation. Show your work.

1. $91 - 2.25$ 4. $11 + 7.08$
 $91 - 2 = 89$ $11 + 7 = 18$
 $89 - 0.05 = 88.95$ $18 + 0.08 = 18.08$

2. $41.03 + 3.02$ 3. $10.49 - 7.03$
 $41.03 + 3 = 44.03$ $10.49 - 7 = 3.49$
 $44.03 + 0.02 = 44.05$ $3.49 - 0.03 = 3.46$

3. $6.4 - 3.45$ 4. $5 + 0.08$
 $6.4 - 3 = 3.4$ $5 + 0.08 = 5.08$
 $3.4 - 0.05 = 3.35$ $5.3 + 0.05 = 5.35$

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Add or Subtract Decimal Word Problem Race
 Students practice adding and subtracting decimals to solve word problems.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 35–36

Lesson 4.8
Additional Practice

Name: _____

Review
 You can use any method to add or subtract decimals.

Estimate each sum or difference. Use a number line to check the decimal by 0.15 (tenths each day). What strategy will Federico use to solve the problem?

You can represent this problem with a bar diagram. The bar diagram shows that you have 4 boxes. The equation is $4.4 + 0.35 = 4.75$.

How many boxes does the store have in all?
 $3.4 + 3.4 + 3.4 + 0.35 = 14.55$
 $3 + 0 = 3$ $0.4 + 0.7 = 1.1$ $0.05 + 0.05 = 0.10$
 Add the partial sums: $3 + 1.1 + 0.10 = 4.20$

Estimate each sum or difference. Show your work.

More math equations. Explain how you determined which strategy to use. Check students' explanations.

1. $3.02 + 2.0 = 5.02$ 2. $24 - 0.01 = 23.99$

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Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with adding and subtracting decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 35–36

Write a division strategy used to solve.
Check students' explanations.

- 8 bags of rice, 2.375 lbs of rice each bag. How much rice is there in all? **3.9375 lbs.**
- The length of one extension cord is 10 feet. The original 4 security cameras is 5.47 kilometers. How much longer is the first extension cord than the other cameras?
1.23 kilometers
- 8 problems earned 10.28 kilograms of gravel for a project. The contractor had to take an additional 10 kilograms of gravel to complete the project. How much gravel was needed?
20.28 kilograms
- Twelve bags, 31.7 meters of fabric for a table. The table is only 20.5 meters of the fabric. How much fabric is left over?
5.2 meters

Math in Motion Activity

Use your math skills to determine how much more or less you would need to buy to make a whole number. Write your answer in the space provided. Show your work.

Subtracting Decimals

E

Extend Thinking

Use It! Application Station

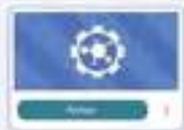
Let's Get Organized! Students use decimals to measure and create organizers.



WORKSTATIONS

WebSketch Exploration

Assign a websketch exploration to apply skills and extend thinking



GO ONLINE

Differentiation Resource Book, p. 36

Lesson 4.8 • Extend Thinking

Explain Strategies to Add and Subtract Decimals

Name: _____

Solve each problem. Explain your answer and why you used each strategy.

- Jason has 11.04 grams of gold and granite. The granite weighs 27.01 grams. How much does the gold weigh?
Sample answer: I used the like differences because the decimal amounts were the same. $72.04 - 27 = 50.04$; $50.04 - 0.04 = 50$. The gold weighs 50 grams.
- Sammy spent \$100 on video games and \$11.32 on books. He had to pay \$20. How much change did he get?
Sample answer: I used decomposition because I saw $0.88 + 0.32$ is a whole number. $100 - 7 = 93$; $0.6 + 0.3 = 0.9$; $0.08 + 0.02 = 0.10$. $93 + 0.9 + 0.1 = 94$. Next subtract to find the change. $20 - 10 = 10$. Sammy will receive \$2 in change.
- Leo paid for his favorite smoothie and \$2.11 for the year his favorite smoothie cost \$2.41. What was the increase in price?
Sample answer: I rounded up because both amounts were very close in value. $38, 39, 40, 41, 42, 43$. The increase in price is \$0.09.
- Chris has 7 gallons of tomatoes. Seven tenths of the tomatoes he has. The rest is tomatoes in 50-gallon containers. How many containers will he need?
Sample answer: Subtract the water from the gallons of tomatoes to find the answer. $7 - 0.7 = 6.3$. The amount of tomatoes is 6.3 gallons.

Differentiation Resource Book

INDEPENDENT WORK

Unit Review Name _____

Vocabulary Review

Choose the correct word(s) to complete each sentence.

1. A number that has a digit in the tenths place, hundredths place, and thousandths place is called a(n) **decimal**.

2. To **decompose** a number means to break the number into parts by using ones to fit other numbers and operations.

3. A number can be used to represent points and lengths in order to **illustrate** a problem.

4. Add the parts of decomposed numbers to find **partial sums**.

5. A number that is an equivalent is called a(n) **equivalent**.

Review

1. Why do you need to decompose when you add $0.23 + 0.18$ when the tenths digits don't add up to 10? Explain how you would use the base ten blocks to solve $0.23 + 0.18 = 0.41$.

2. Use the base ten blocks to solve $0.23 + 0.18 = 0.41$. Complete the addition equation that is represented by the base ten blocks.

3. Use partial sums to add these two numbers.

Sample answer:
 $4 \div 1 = 5$; $0.23 + 0.18 = 0.41$
Total Sum: 5.41

4. Use the base ten blocks to solve $0.23 + 0.18 = 0.41$. Complete the addition equation that is represented by the base ten blocks.

Sample answer:
 $0.23 + 0.18 = 0.41$

Students can complete the **Unit Review** to prepare for the **Unit Assessment**. Students may complete the Review in their Interactive eBook in the Digital Student Center.

Vocabulary Review

Item Analysis

Item	Lesson
1	4-1
2	4-4
3	4-2
4	4-4
5	4-1

Review

Item Analysis

Item	DOK	Lesson	Standard
6	2	4-1	5.NBT.B.7
7	2	4-3	5.NBT.B.7
8	2	4-4	5.NBT.B.7
9	2	4-3	5.NBT.B.7
10	3	4-5	5.NBT.B.7

To review the lessons in this unit, have students watch the Math Replay video in their Digital Student Center.

Assign the Unit Review practice to students from the Digital Teacher Center.



Item Analysis (continued)

Item	DOK	Lesson	Standard
11	2	4-6	5.NBT.B.7
12	2	4-5	5.NBT.B.7
13	2	4-7	5.NBT.B.7
14	2	4-8	5.NBT.B.7
15	2	4-8	5.NBT.B.7

Performance Task

Standard: 5.NBT.B.7

Rubric (4 points)

Part A – 2 points

2 POINTS Student's work reflects a proficiency in using a bar diagram to represent a word problem. The student can complete a bar diagram and use a variable to represent the unknown.

1 POINT Student's work reflects developing proficiency in using a bar diagram to represent a word problem. The student partially completes the bar diagram.

0 POINTS Student's work reflects a weak understanding of using a bar diagram to represent a word problem. The student cannot use a variable to represent the unknown.

Part B – 2 points

2 POINTS Student's work reflects a proficiency in using strategies to subtract decimals. The student's solution is accurate and the student is able to explain the strategy.

1 POINTS Student's work reflects developing proficiency in using strategies to subtract decimals. The student's solution may be accurate, but they may not be able to explain the strategy.

0 POINTS Student's work reflects a weak understanding of using strategies to subtract decimals. The student's solution is inaccurate, and they are not able to explain the strategy.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

11. Benji used a number grid to solve $12 - 3.7$.

Which operation can he be using to solve the problem? Explain.

A. He should start with a number less than 12.

B. He should subtract 3.7 from 12.

C. He should start with a number greater than 12.

D. He should subtract 3.7 from 12.

12. Use a number grid to subtract.

$0.02 - 0.08 = 0.02$

Sample answer shown

13. Decrease by each minute a dollar. How much work?

$5.02 - 2.08 = 2.94$

**Sample answer: $5.02 - 2 = 3.02$
 $3.02 - 0.08 = 2.94$**

14. What weight has a mass? The first weight is 2.85 kilograms. The second weight is 2.20 kilograms. How much heavier is the second weight? Explain how you determine which strategy to use.

0.23 kg. Check student's explanation.

15. What is the difference? Explain the strategy you use to solve.

$12 - 3.80 = 8.20$

Check student's explanation.

Grade 5 • Unit 1 • Lesson 10 • 101

Performance Task

A contractor needs a plan to remove equal odd corners. She removes 1.48 yards of bottom gravel and 0.78 yard of middle gravel. How much bottom gravel does she need to remove? Explain your work.

Part A: Complete the bar diagram to represent the problem.

Sample answer shown

Part B: Solve the problem. Show your work and explain how you determine which strategy to use to solve.

Check student's explanation. Sample answer: $0.78 \text{ in } 1.48 - 0.70 = 0.78 - 0.78 = 0.02 = 0.78$

Reflect

Describe two strategies for adding or subtracting decimal numbers. Which strategy do you prefer to use?

Answers may vary.

Grade 5 • Unit 1 • Lesson 10 • 102

Unit 4
Fluency Practice

Name: _____

Fluency Strategy

You learned an algorithm to subtract. Subtract the numbers in the same place value.

Subtract the ones first, then the tens.

$18.75 - 12.42 = 6.33$

$2.00 - 0.00 = 2.00$

Use a strategy to subtract.

Fluency Flash

What is the difference?

1.

Tenths	Hundredths	Tens	Ones
5	4	7	9
4	1	6	5
2	3	2	3

2.

Tenths	Hundredths	Tens	Ones
9	7	2	9
2	5	4	1
1	3	3	3

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Fluency Check

What is the sum or difference?

A. $3,007 - 2,804 =$ **203**

B. $2,010 + 5,007 =$ **7,017**

C. $430 + 40 =$ **470**

D. $12,567 - 1244 =$ **11,323**

E. $125 - 103 =$ **22**

F. $5,070 - 2,000 =$ **3,070**

G. $45,971 + 31,000 =$ **76,971**

H. $9,000 - 67,000 =$ **-58,000**

I. $4,0000 + 4,300 =$ **44,700**

J. $24 + 10 =$ **34**

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Fluency Talk

Subtract a 4-digit from a 5-digit. Explain to a partner why you need to regroup when subtracting. Write an algorithm.

Explanation may vary.

How do you regrouping to subtract a different from using an algorithm to subtract?

Explanation may vary.

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Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students practice using an algorithm to subtract.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Performance Task

Cell Phone Shopping

Student draw on their understanding of using strategies to add and subtract decimals. Use the rubric shown to evaluate students' work.

Standard: 5.NBT.B.7

Rubric (8 points)

Part A (DOK 3) – 2 points

- 2 POINTS** Student's explanation reflects a proficiency with estimating with decimals in context.
- 1 POINTS** Student's explanation reflects developing proficiency with estimating with decimals in context.
- 0 POINTS** Student's explanation reflects a poor understanding with estimating with decimals in context.

Part B (DOK 2) – 2 points

- 2 POINTS** Student's work reflects a proficiency with decimal addition and subtraction. Student's work reflects a proficiency with estimation.
- 1 POINTS** Student's work either reflects a developing proficiency with decimal addition and subtraction or a developing proficiency with estimation.
- 0 POINTS** Student's work shows a weak proficiency with decimal addition and subtraction. Student's work shows a weak proficiency with estimation.

Part C (DOK 3) – 2 points

- 2 POINTS** Student's work reflects a proficiency with decimal addition and subtraction. Student's conclusion is reasonable.
- 1 POINTS** Student's work either shows developing proficiency with decimal addition and subtraction or has a reasonable conclusion.
- 0 POINTS** Student's work shows weak proficiency with decimal addition and subtraction. The student's conclusion is not reasonable.

Part D (DOK 2) – 2 points

- 2 POINTS** Student's work reflects 2 reasonable strategies to find the correct answer.
- 1 POINTS** Student's work reflects 1 reasonable strategy to find the correct answer.
- 0 POINTS** Student's work reflects weak proficiency with decimal operations.

Unit 4
Performance Task

Name: _____

Cell Phone Shopping

Sam is shopping for a new cell phone plan. She wants to make the best decision for her budget when choosing the phone plan, so she wants to know around the area by Cell City, so she has some:

Part A

The first plan Sam is looking at is the \$100 plan. She has \$17.00 budgeted per month for her phone bill. Sam found that it would cost \$4.00 monthly service fee. She can get the better data plan for \$24.00 per month. Do you agree? Explain.

Sample answer: No, Sam should round to the nearest greater dollar. She actually does not have enough money for this plan.

$$\begin{aligned} \$1.00 &= \$2.00 \\ + 14.99 &= 15.00 \\ \hline 17.00 &= 16.99 \end{aligned}$$

Part B

Sam is trying to find a new phone in Cell City.

Cell City Phone Plans			SR Data Plans		
Phone	Plan	Price	1 GB	2 GB	3 GB
100-100	100-100	\$19.99	\$19.99	\$19.99	\$19.99

If Sam buys within her phone budget of \$17.00, what is the highest number of GB of data she can afford to buy, then would she still get the phone, too, and how much for each data plan (payment is for 1 GB). Show your work.

$$\begin{aligned} 19 - 20 - 11 &= 0 = 29.1 \text{ GB} \text{ Sam can afford 2 GB of data.} \\ 16.99 - 29.99 &= 49.97 \\ 49.97 - 19.99 &= 29.97 \\ 29.97 - 4.22 &= 25.75 \end{aligned}$$

Sam can only afford to buy 2 GB of data for \$16.99.

Answer Key: 100-100

Part C

Sam is trying to find a new phone in Cell City. She has some:

Super Cell Phone Plans			SR Data Plans		
Phone	Plan	Price	1 GB	2 GB	3 GB
100-100	100-100	\$19.99	\$19.99	\$19.99	\$19.99

She has a budget of \$17.00. She can get the better data plan for \$24.00 per month. Do you agree? Explain.

Sample answer: Super Cell is better than SR Data. She can afford to buy 2 GB of data for \$16.99.

Super Cell: $\$39.99 + \$20.00 + \$8.99 + \$7.94 = \$76.91$

Compare the total cost with the Cell City plan from Part B. If Sam has \$68 of data, which is the better cell phone plan for Sam? Explain. Show your work.

Cell City: $\$29.99 + \$19.99 + \$4.94 + \$6.22 = \$61.14$
Super Cell: $\$39.99 + \$20.00 + \$8.99 + \$7.94 = \$76.91$
Super Cell is the better plan, but both plans are greater than her budget.

Part D

Sam is trying to find a new phone in Cell City. She has some:

She is looking at the phone. She wants to make the best decision for her budget when choosing the phone plan, so she wants to know around the area by Cell City, so she has some:

Strategy 1: $19 - 4.00 = 15.00$
Strategy 2: $6.00 + 0.22 + 9.99 = 16.21$
 $16 - 16.21 = 0.21$
 Sam will have 0.21 GB free after the lookup.

Answer Key: 100-100

Unit Assessments

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

 **Data** When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support Intervention Lesson	Standard
1	2	4-1	Estimate Sums and Differences of Decimals	5.NBT.B.7
2	2	4-5	Model Subtracting Decimal Numbers	5.NBT.B.7
3	2	4-3	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7
4	1	4-2	Model Adding Decimals	5.NBT.B.7
5	2	4-6	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7
6	2	4-4	Adding and Subtracting (Partial Sums and Differences)	5.NBT.B.7
7	2	4-3	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7
8	2	4-5	Model Subtracting Decimal Numbers	5.NBT.B.7
9	2	4-1	Estimate Sums and Differences of Decimals	5.NBT.B.7
10	2	4-1	Estimate Sums and Differences of Decimals	5.NBT.B.7
11	2	4-7	Adding and Subtracting (Partial Sums and Differences)	5.NBT.B.7
12	3	4-4, 4-7	Adding and Subtracting (Partial Sums and Differences)	5.NBT.B.7
13	3	4-8	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7
14	3	4-8	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7
15	3	4-8	Represent Adding and Subtracting (Tenths and Hundredths)	5.NBT.B.7

Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 4 Unit Assessment, Form A

1. Where Robert lives, the average high temperature in July is 82°F. The average low temperature in July is 64°F. Which assessment best estimates the difference between the average high and low temperatures in July?

- A. $87 - 61 = 26$
- B. $88 - 64 = 24$
- C. $88 - 62 = 26$
- D. $87 - 64 = 23$

3. What operation is shown by the decimal grid?



- A. $1 - 0.25 = 0.75$
- B. $0.60 + 0.40 = 1.00$
- C. $0.25 + 0.25 = 0.50$
- D. $0.25 + 0.25 = 0.50$

4. What operation is shown by the decimal grid?



$1.00 + 0.70 = 1.70$

Answer Form A-10

4. What is the sum? Use the decimal grid to solve.



- A. 0.0
- B. 0.1
- C. 1.1
- D. 0.2

5. What is the difference? Use the decimal grid to solve.



- A. 0.0
- B. 0.7
- C. 0.3
- D. 0.2

6. Which of the following is a correct way to find $26.34 + 13.02$? Choose what you want.

- A. $26 + 13 = 39$ and $0.34 + 0.02 = 0.36$
- B. $26 + 13 = 39$ and $0.34 + 0.02 = 0.36$
- C. $20 + 10 = 30$ and $6 + 3 = 9$ and $0.34 + 0.02 = 0.36$
- D. $26 + 13 = 39$ and $0.34 + 0.02 = 0.36$

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Unit 4

Unit Assessment, Form A (continued)

Name _____

8. The number of people that live in the city of New York is 20,000,000. How many times as large is the population of New York as the population of the state of New York?
- A. 20 times
B. 10 times
C. 5 times
D. 100 times
9. At the grocery store, there are 20 bags of 2 pounds. The second bag was 5.5 pounds. How much longer was the 5th bag?
- A. 0.5 pounds
B. 0.1 pounds
C. 1.2 pounds
D. 1.5 pounds
10. The great wall is 2.2 million kilometers. The second wall is 1.5 million kilometers. How many times as long is the second wall as the first?
- about 3 times
11. A line contains 2000 customers long. A person had had been using a line 1200 customers long. How many times longer is the line now?
- about 10 customers
12. The number 2.25 is 2.25 times as large as the number 1. How many times as large is the number 2.25 as the number 1?
- 2.25 times

Assessment Form A (cont.)

13. The number of people that live in the city of New York is 20,000,000. How many times as large is the population of New York as the population of the state of New York?
- 20 times
14. The number of people that live in the city of New York is 20,000,000. How many times as large is the population of New York as the population of the state of New York?
- \$20.34. Sample answer: I used the count on to subtract strategy. I started at 12.95 and counted up by 0.01 to 13.00. Then I added 0.32 to get 13.32. Then I added 25 to get 41.32. Then I added 0.01 + 0.32 + 28 = 25.34.
15. A number is 2.25 times as large as the number 1. How many times as large is the number 2.25 as the number 1? What strategy did you use to solve?
- 2.25 times. Sample answer: I decomposed both numbers and added the like place values: $10 + 10 = 20$; $0.2 + 0.2 = 0.4$; $0.05 + 0.05 = 0.1$; $0.05 + 0.05 = 0.1$. Then I added the partial sums: $20 + 10 + 0.4 + 0.1 + 0.1 = 25.34$.
16. A number is 2.25 times as large as the number 1. How many times as large is the number 2.25 as the number 1? What strategy did you use to solve?
- 2.25 times. Sample answer: I used the count on to subtract strategy. I counted up 0.05 from 20.00 to get 20.05. Then I added 0.5 to get 20.5. Then I added 0.7 to get 40.5. So the answer is $0.05 + 0.5 + 0.7 = 20.5$.

Assessment Form A (cont.)

Unit 4

Unit Assessment, Form B

Name _____

1. Which number is the largest? Circle the largest number.
- A. 10 + 10 + 10
B. 10 + 10 + 10
C. 10 + 10 + 10
D. 10 + 10 + 10
2. Write the number of people that live in the city of New York.
- 
- A. 100
B. 1000
C. 10000
D. 100000
3. Write the number of people that live in the city of New York.
- 
- 100 + 100 = 200

Assessment Form B (cont.)

Unit 4

Unit Assessment, Form B

Name _____

4. Write the number of people that live in the city of New York.
- 
- A. 100
B. 1000
C. 10000
D. 100000
5. Write the number of people that live in the city of New York.
- 
- 100 + 100 = 200
6. Write the number of people that live in the city of New York.
- 
- 100 + 100 = 200

Assessment Form B (cont.)

100 + 100 = 200
100 + 100 = 200
100 + 100 = 200

7. Write the number of people that live in the city of New York.
- 100 + 100 = 200
100 + 100 = 200
100 + 100 = 200
8. Write the number of people that live in the city of New York.
- 100 + 100 = 200
100 + 100 = 200
100 + 100 = 200

Assessment Form B (cont.)

Benchmark Assessment 1

The Benchmark Assessment 1 is available in both print and digital.

Data When students complete the Benchmark Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Skill	Standard
1	2	Subtract decimals	5.NBT.B.7
2	3	Understand volume	5.MD.C.3
3	2	Add decimals	5.NBT.B.7
4	2	Round decimals	5.NBT.A.4
5	2	Add decimals	5.NBT.B.7
6	1	Understand decimal place value	5.NBT.A.1
7	3	Describe how to find volume	5.MD.C.5
8	2	Compare decimals	5.NBT.A.3.b
9	2	Determine the volume of composite figures	5.MD.C.5
10	2	Compare decimals	5.NBT.A.3.b
11	3	Represent decimals in different ways	5.NBT.A.3.a
12	2	Determine the volume of composite figures	5.MD.C.5
13	1	Relate addition and subtraction of decimals	5.NBT.B.7
14	2	Count unit cubes to determine volume	5.MD.C.3, 5.MD.C.4
15	2	Understand decimal place value	5.NBT.A.1
16	2	Solve volume word problems	5.MD.C.5
17	1	Read and write decimals	5.NBT.A.3.a
18	2	Represent subtraction of decimals	5.NBT.B.7
19	2	Estimate sums and differences of decimals	5.NBT.B.7
20	1	Understand volume	5.MD.C.3
21	2	Represent subtraction of decimals	5.NBT.B.7

Assign the digital Benchmark Assessment to students or download and print PDFs from the Digital Teacher Center.



Grade 5
Benchmark Assessment 1

Name: _____

1. Look at the expression.
 $96.6 - 0.18$
What is the value of the expression?
96.42

2. A student is asked to find the volume of the rectangular prism.
Write the number that the student is being asked to fill in the blank prism.
12
A. Find the number of unit cubes it takes to fill the prism.
B. Find the number of unit cubes it takes to fill the entire rectangular prism.
C. Find the number of unit cubes it takes to equal the length of the rectangular prism.
D. Find the number of unit cubes it takes to equal the bottom of the rectangular prism.

3. Replace each letter with the missing number to complete the equation.
 $1 + 2 = 3$
 $0.6 + 0.3 = 0.9$
 $0.66 + \underline{0.02} = \underline{0.08}$
 $0.750 + \underline{0.05} = \underline{0.25}$

4. Which is 0.01 less than the number 0.01?
A. 0.01
B. 0.02
C. 0
D. 0.01

Answer Key: 1. 96.42, 2. 12, 3. C, 4. C

5. What is the sum?
 $0.66 + 0.02 + 0.03 + 0.01 = \underline{0.72}$

6. What is the volume of the prism?
A. 120
B. 12
C. 14
D. 40

7. Which of these is not a correct method for finding the volume of a box?
A. Multiply the length by the width by the height of the box.
B. Multiply the length by the width and add this to the height of the box.
C. Fill the box completely with unit cubes and count the number of unit cubes it takes to fill the box.
D. Fill the bottom of the box with unit cubes and then multiply the number of unit cubes by the height of the box.

8. How far did the car travel?
 $0.0007 - 0.0000000 = \underline{0.0007}$

9. A company designs a desk for homes. The desk and the handle are shown. The desk is 12 inches long, 3 inches wide, and 3 inches high. The handle is 3 inches long, 1 inch wide, and 1 inch high.

What is the total volume of the desk and handle?
A. 27 cubic inches
B. 33 cubic inches
C. 21 cubic inches
D. 30 cubic inches

Answer Key: 5. 0.72, 6. B, 7. B, 8. C, 9. B

Grade 6

Benchmark Assessment 1 (continued)

Name _____

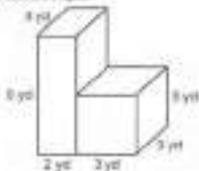
13. Which symbol makes the comparison true?

A. $50,425 > \square$ B. $50,425 < \square$
 C. $50,425 = \square$ D. $50,425 \leq \square$

14. Read a number line that has only one tick mark every 100 units.
- $100 + 10 = \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \dots$
- Which expressions give the lengths shown on the line? Check all that apply.

A. $100 + 10 + \frac{100}{100}$ D. $100 + 1 + \frac{1}{10} + \frac{1}{100}$
 C. $100 + 1 + \frac{10}{100} + \frac{100}{100}$ E. $100 + \frac{10}{100} + \frac{100}{100}$
 B. $100 + \frac{1}{10} + \frac{10}{100} + \frac{100}{100}$ F. $100 + 20 + 1 + \frac{1}{10} + \frac{10}{100} + \frac{100}{100}$

15. Look at the figure.



What is the volume in cubic units of the figure?

- A. 20 cubic units B. 45 cubic units
 C. 63 cubic units D. 90 cubic units

Answer Key: 63 14

Grade 6

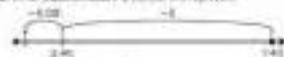
Benchmark Assessment 1 (continued)

Name _____

16. Which of these is 8% less and forty three thousandths?

A. 32,430
 B. 32,403
 C. 32,443
 D. 32,243

17. Which equation does the number line represent?



Write the missing numbers.

$$1.45 - 0.28 = 1.17$$

18. Luke made three grades in school. His average grade in History is 80 percent, in Language is 50 percent, and in Science is 78 percent. Which equation could give the arithmetic mean of the different classes? Luke's average grades in History and Science?

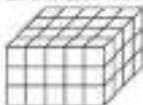
A. $80 + 78 = 158$
 B. $80 + 78 = 158$
 C. $80 + 78 = 158$
 D. $80 + 78 = 158$

Answer Key: 80 17

19. Which equation has the same solution as
- $22.50 + \square = 28.57$
- ?

A. $\square + 28.57 = 22.50$
 B. $28.57 - \square = 22.50$
 C. $22.50 - 28.57 = \square$
 D. $28.57 - 22.50 = \square$

20. Look at the figure, which is 100 cubic centimeters long.



What is the volume of the figure above?

100 cubic centimeters

21. Two eggs, a collector bought a row of 40 eggs. The value of the collection is \$20, which is 10 times their length when you multiply the collector by the cost?

A. 50
 B. 520
 C. 5200
 D. 52,000

22. Consider a box that is 40 centimeters 2 centimeters and 5 centimeters.

What is the volume of the box? (Volume = length)

400 cubic centimeters

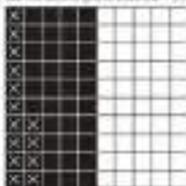
Answer Key: 400 22

23. Study each figure to see how many units it is 100 units.

What is the volume of the number line? Study, looking for the

A. length
 B. perimeter
 C. area
 D. volume

24. Use the figure to solve
- $55 - 37 = 18$
- .

What is the value of 18 ?

18

Answer Key: 18 24

Multiply Multi-Digit Whole Numbers

PACING: 12 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  Mile-High Pennies	Review estimation and multiplication skills using stacks of pennies.		
5-1 Understand Powers and Exponents	Students write a power of 10 as a multiplication expression with factors of 10. Students write a power of 10 using a base of 10 and exponents.	Students explain the steps to take to write a power of 10 as a multiplication expression while using the passive voice.	Students demonstrate self-awareness of personal strengths and areas of challenge in mathematics.
5-2 Patterns When Multiplying a Whole Number by Powers of 10	Students use patterns to determine products when multiplying whole numbers by powers of 10. Students explain patterns in the products when multiplying whole numbers by powers of 10.	Students talk about the patterns they see in products while answering <i>Wh-</i> questions.	Students employ techniques that can be used to help maintain focus and manage reactions to potentially frustrating situations.
5-3 Estimate Products of Multi-Digit Factors	Students estimate products of multi-digit factors using the same strategies used to estimate products of lesser factors. Students use estimated products to make predictions about a calculated solution. Students use estimated product to assess the reasonableness of a calculated solution.	Students discuss estimating products while answering <i>Wh-</i> questions.	Students determine the strategies and analyses necessary to make informed decisions when engaging in mathematical practices.
5-4 Use Area Models to Multiply Multi-Digit Factors	Students use an area model to determine partial products and add partial products to calculate the product.	Students explain how to use an area model to multiply while answering <i>Wh-</i> questions.	Students explore taking different perspectives on approaches to problem solving.
5-5 Use Partial Products to Multiply Multi-Digit Factors	Students determine partial products by decomposing the factors and add partial products to calculate the product.	Students discuss how to solve multiplication equations using partial products while answering <i>Wh-</i> and <i>Yes/No</i> questions.	Students practice strategies for persisting at a mathematical task, such as setting a small goal or setting timers for remaining focused.
5-6 Relate Partial Products to an Algorithm	Students use an algorithm to multiply multi-digit factors by a one-digit factor. Students understand and explain a multiplication algorithm.	Students discuss strategies to multiply while using <i>as...as</i> .	Students collaborate with peers to complete a mathematical task and offer constructive feedback to the mathematical ideas posed by others.
Math Probe Multiplication of 2-Digit Numbers	Determine if a given strategy is a correct approach to find the product of two 2-digit numbers.		
5-7 Multiply Multi-Digit Factors Fluently	Students use an algorithm to multiply two multi-digit factors.	Students explain how to use an algorithm to multiply while answering <i>Wh-</i> and <i>Yes/No</i> questions.	Students identify and discuss the emotions experienced during math learning.
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION:
How can I multiply
multi-digit numbers?

LESSON	KEY VOCABULARY		MATERIALS TO GATHER	RIGOR FOCUS	STANDARD
5-1	Math Terms	Academic Terms	• number cubes	Conceptual Understanding Procedural Skill & Fluency	5.NBT.A.2
	base exponent exponential form power of 10	accurate prove			
5-2	base exponent factor power of 10	cite establish	• calculators • index cards	Conceptual Understanding Procedural Skill & Fluency	5.NBT.A.2
5-3	estimate round	accurate relevant	• calculators • index cards • number cubes	Procedural Skill & Fluency	5.NBT.B.5
5-4	area model decompose partial products	debate speculate	• none	Procedural Skill & Fluency	5.NBT.B.5
5-5	area model partial products	analyze suggest	• number cubes	Procedural Skill & Fluency	5.NBT.B.5
5-6	algorithm partial products regroup	procedure prove	• base-ten blocks • number cubes	Procedural Skill & Fluency	5.NBT.B.5
5-7	algorithm	analyze note transition	• <i>Multiplication Algorithm</i> Teaching Resource • number cubes	Procedural Skill & Fluency	5.NBT.B.5
			• spinners		

Unit Overview

Focus

Multiply Multi-Digit Whole Numbers

In this unit, students are guided gradually from their previous understanding of place-value relationships to a concrete understanding of multi-digit multiplication. They begin by writing powers of 10 in exponential form and then work to identify patterns when multiplying by powers of 10.

Students then begin to estimate products, using compatible numbers and rounding. Estimation gives students a way to think about computation with larger numbers. For example, the magnitude of the product $5,136 \times 13$ may not be as easy for students to comprehend as $5,000 \times 10$. That may be because students may lose sense of the magnitude of the product when they work through the steps of finding $5,136 \times 13$. After they estimate products, students begin finding exact products by using area models and partial products.

Students then relate their understanding of partial products to an algorithm. Multiplying multi-digit numbers using an algorithm can be an abstract process. Even when students multiply the digits in the correct order and regroup accurately, they may not be fully aware of the actual quantities with which they are working.

Coherence

What Students Have Learned

- Students multiplied up to 4-digit whole numbers by 1-digit whole numbers using place value and properties of operations.
- Students multiplied two 2-digit whole numbers using place value and properties of operations.
- Students understood the relationship between values of digits within the base-ten system.

What Students Are Learning

- Students use whole-number exponents to denote powers of 10.
- Students explain patterns when multiplying a number by powers of 10.
- Students use patterns to multiply a number by powers of 10.
- Students use area models to determine partial products and relate the partial products to the standard algorithm.
- Students multiply multi-digit whole numbers using an algorithm.

What Students Will Learn

- Students extend the algorithm for multiplication to multiply decimals.

Rigor

Conceptual Understanding

Students develop understanding of:

- exponential form of powers of 10.
- patterns when multiplying whole numbers by powers of 10.

Procedural Skill and Fluency

Students build proficiency with:

- solving and evaluating expressions with powers of 10.
- multiplying by a power of 10.
- estimating the product of multi-digit factors.
- using area models to multiply multi-digit factors.
- using partial products and an algorithm to multiply multi-digit numbers.

Application

Students apply their knowledge of:

- estimating products to solve real-world applications involving the products of multi-digit numbers.
- area models and partial products to solve real-world applications involving the products of multi-digit numbers.

Application is not a targeted element of rigor for the standards in this unit.

Effective Teaching Practices

Use and Connect Mathematical Representations

Throughout this unit, students use a variety of representations as they develop skills with multi-digit multiplication.

- They use partial products represented both numerically and with area models. This reinforces place value and also provides a visual means for understanding why the partial products are added to determine the final product.
- Students write equations using variables to represent the products, and they write the steps for multiplying with the algorithm.

Each connection that students make among these representations helps them visualize the math.

Encourage students to use more than one representation and to articulate the connections among them.

For example, as students make the transition from partial products to the algorithm, ask them to explain how each partial product is represented in the steps of the algorithm. Have students pay special attention to what the regrouped digits represent and how they are composed with subsequent products.

Ask open-ended questions that encourage students to discuss which representations they find most meaningful and effective.

Guide students to maintain fluency with varied tools and strategies.

When students get stuck using one strategy, guide them to try another one with which they might be more comfortable.

For example, as students progress to using the algorithm to multiply factors with greater numbers of digits, remind them of how they have used partial products and how they related the two strategies.

Math Practices and Processes

Look for and Express Regularity in Repeated Reasoning

This unit's progression of multiplication strategies and size of factors provides consistent opportunities for students to look for and express regularity.

- When students identify patterns when multiplying by powers of 10, they should describe ways to use the pattern to find other products.
- When students estimate a product, use partial products to calculate the product, and then compare the estimate with the calculation, they should observe and describe the connections they see.
- When students progress from multiplying a multi-digit number by a 1-digit number to multiplying multi-digit numbers by a 2-digit number, the reasoning that they have applied in one instance should guide their understanding of the next.

Provide frequent opportunities for students to articulate their strategies and reasoning.

Some suggestions include:

- Students are given different multiplication problems. Each student shows the same problem using partial products and the algorithm. Then, students share their work with partners. Pairs describe to each other how the partial products and algorithm steps show the same multiplication, including regrouping.
- Students are given the same multiplication problem and are asked to find different ways to represent it. Each student then describes how he or she chose the representation and how each step or element is part of finding the product.
- Students are given a multiplication problem and are asked to estimate the product using both compatible numbers and rounding, find the actual product using a calculator, and then explain the differences among the two estimates and the calculated product.

Social and Emotional Learning

What Skills Will We Develop?

- **Self-Awareness – Accurate Self-Perception** (Lesson 5-1): Having accurate self-perception allows students to determine areas of strength as well as areas in which they need to focus and practice.
- **Self-Management – Control Impulses** (Lesson 5-2): Students who can regulate their impulses and reactions are better able to navigate and solve problems.
- **Responsible Decision Making – Analyze Situations** (Lesson 5-3): Students make sense through analysis, which helps them make informed decisions.
- **Social Awareness – Develop Perspective** (Lesson 5-4): Developing perspective can help students understand different ways of thinking.

- **Self-Management – Self-Discipline** (Lesson 5-5): Self-disciplined students can manage their impulses to focus on a mathematical task.
- **Relationship Skills – Social Engagement** (Lesson 5-6): Engaging with others allows students to develop relationships and establish a sense of security and belonging in the classroom community.
- **Self-Awareness – Identify Emotions** (Lesson 5-7): Students who can identify and understand their own feelings and emotions can better manage the reactions to those feelings and emotions.

Unit Overview

Language of Math

Vocabulary

Students will be using these key terms in this unit:

- **algorithm** (Lesson 5-6, 5-7) Students may have been introduced to this term in Grade 3 when using the addition and subtraction algorithm. Now this term will be applied to multi-digit multiplication.
- **base*** (Lesson 5-1, Lesson 5-2) The base is the number that is repeatedly multiplied when written in exponential form.
- **estimate** (Lesson 5-3) Students were introduced to estimating in Grade 3. Have students discuss estimation techniques such as rounding as a way of determining the magnitude of a solution or checking the reasonableness of a calculated solution.
- **exponent*** (Lesson 5-1, 5-2) The exponent is the superscript after the number and notes the number of times the number is multiplied times itself.

- **exponential form*** (Lesson 5-1) Exponential form involves a number, called the base, and an exponent. Exponential form is a way of simplifying the notation for repeated multiplication.
- **partial products** (Lesson 5-4, 5-5, 5-6, 5-7) Students were introduced to partial products in Grade 3. Relate this term to the area models used to find products as well as the Distributive property.
- **power of 10*** (Lesson 5-1, 5-2) A power of ten is the exponential form using a base of 10. The exponent is also called the power.
- **round** (Lesson 5-3) Students were introduced to rounding in Grade 2. Have students review when to round up and when to round down. Discuss the importance of place value when rounding.

*This is a new term.

Math Language Development

A Focus on Speaking

When students learn a new language, speaking that language is of paramount importance.

Learning the grammar and vocabulary will not be enough for the language student to build fluency; instead, a certain reading and writing fluency may be gained while the student is never comfortable enough with the rhythm and sound of the language to understand or participate in its spoken form.

The language of mathematics is a subset of the language of where it is being taught and discussed. In the United States, it is part of English, in Germany, it is part of German, and so on. As such, the linguistic aspects of math may not receive pedagogical focus.

But the specific vocabulary, usage, and phrasing of math is its own subset of the language, one that can be difficult to learn for students who are learning it in their first languages but even more so for second-language students.

And just like students of new languages, students of math will not gain real fluency in its language without speaking the words and sentences that make up, describe and explain it.

For this reason, give students ample opportunities to speak about the math that they are learning. As they learn about multi-digit multiplication, model precise oral usage of correct vocabulary and guide students to integrate it into their own speech.

Students should hear the words *base*, *exponent*, *factor*, *product*, *estimate*, *partial product*, and *algorithm* in your discourse and then become fluent with these terms in their own explanations.

Help students analyze terminology, breaking down words' meanings to make them more accessible. For example, discuss that when we use partial products, each product is a part of the whole product.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to multiplying multi-digit whole numbers. Because many of the words (*distance*, *feet (ft.)*, *vertical*), phrases (*as...as*, *make money*), and grammar structures (*can be...*, *to + verb*) used in this unit could prove challenging to ELs, they are supported in understanding and using them so that the instruction is more accessible.

Lesson 5-1 – *can be (connected)*

Lesson 5-2 – *distance*

Lesson 5-3 – *to + verb* to say why

Lesson 5-4 – abbreviation ft.

Lesson 5-5 – *vertical*

Lesson 5-6 – *as...as...* to compare

Lesson 5-7 – *make money*

Unit Routines

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

About How Much?

Purpose: Build estimating skills.

Overview: Students estimate the value of expressions (with operations) shown, explaining their strategies and thinking. The teacher records students' estimates, then reveals the value of the expression. Students analyze the estimates and discuss which are closest to the actual value of the expression.

Find the Pattern, Make a Pattern

Purpose: Build efficiency with recognizing and building patterns.

Overview: Students determine the rule(s) for a given pattern, then use the rule(s) to create a new pattern. The teacher records students' new patterns and facilitates a discussion to validate the pattern and its rules.

Greater Than or Less Than

Purpose: Build proficiency with number and place value sense; estimating and comparing skills.

Overview: Students use mental math to estimate or evaluate the value of given expressions and then compare the value of the expressions to a target benchmark number. Students share their solutions and thinking.

What's Another Way to Write It?

Purpose: Build flexibility with number sense and mental math operations.

Overview: Given a number, students generate expressions using operations that, when evaluated, have the same value as the number. The teacher records expressions as students share. Students then look for relationships amongst the expressions.

Sense-Making Routines

- **Which Doesn't Belong?** (Lesson 5-1) Students analyze four multiplication expressions, looking for similarities and differences that get them to think about multiplication with the repeated factors.
- **Notice & Wonder: How are they the same? How are they different?** (Lesson 5-2, 5-7) Students consider the similarities and differences between different representations involving multiplication by powers of 10. In lesson 7, students compare two ways to solve a multiplication problem.
- **Notice & Wonder: What do you notice? What do you wonder?** (Lesson 5-3, 5-5, 5-6) In Lesson 5-3, students prepare to think about how an estimate compares to a calculated solution. In the following lessons, students think about how a multiplication equation relates to an area model and then how a multiplication equation with partial products relates to the standard algorithm.
- **Notice & Wonder: What do you see?** (Lesson 5-4) In lesson 5-4, students consider an image where the area is decomposed into smaller rectangles and how they add to the total.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable, format for amplifying and developing students' social and academic language. For more information on the Math Language Routines, see the Appendix.

- Lesson 5-1 – Students participate in MLR6: Three Reads.
- Lesson 5-2 – Students participate in MLR1: Stronger and Clearer Each Time.
- Lesson 5-3 – Students participate in MLR7: Compare and Connect.
- Lesson 5-4 – Students participate in MLR4: Information Gap.
- Lesson 5-5 – Students participate in MLR8: Discussion Supports and MLR3: Critique, Correct, and Clarify.
- Lesson 5-6 – Students participate in MLR1: Stronger and Clearer Each Time.
- Lesson 5-7 – Students participate in MLR5: Co-Craft Questions and Problems.

LEVEL 3
How Ready Am I?

Name: _____

1. Which place has the smallest part of \$27?

A. $3 + 3 + 3$
 B. $30 + 30 + 30$
 C. $300 + 30 + 3$
 D. $3000 + 200 + 10$

2. What is the number 491,532 rounded to the nearest thousand?

A. 500,000
 B. 490,000
 C. 492,000
 D. 487,500

3. Which coin is equivalent to 10¢ in 3 different pennies?

A. 4¢
 B. 10¢
 C. 50¢
 D. 100¢

4. What is the product of 30 × 40?

A. 70
 B. 700
 C. 1,200
 D. 1,400

5. What is the product of 20 × 40?

A. 60
 B. 80
 C. 800
 D. 8000

Answer Key: 1. C, 2. C, 3. B, 4. C, 5. C

6. What is the correct sum?

$3,284$
 $+ 457$
 A. 3,741
 B. 3,737
 C. 3,641
 D. 3,741

7. What is the correct sum?

$5,189$
 $+ 5,882$
 A. 11,071
 B. 11,070
 C. 11,072
 D. 11,073

8. Which number meets the equation?

$33 = 11 \times 300 \div 7 \times 30 \div 3$

A. 70
 B. 30
 C. 300
 D. 350

9. A rectangular flower bed is 40 feet long and 40 feet wide. About how much is the area of the flower bed?

A. 2,000 square feet
 B. 2,400 square feet
 C. 2,000 square feet
 D. 3,000 square feet

10. A penny is 0.01 units for 1 cent. How much did the coin cost from the sale of the penny?

A. 300
 B. 3000
 C. 30000
 D. 300000

Answer Key: 6. A, 7. A, 8. B, 9. C, 10. D

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

Use Guided Support intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill		Guided Support Intervention Lesson	Standard
1	1	Identify expanded form of a number	Expanded Form through 999,999	4.NBT.A.2
2	2	Round to the nearest thousand	Round to Nearest 10, 100, or 1,000	4.NBT.A.3
3	2	Use partial products to multiply	Multiply 2- by 1-Digit Numbers	4.NBT.B.5
4	2	Multiply two 2-digit numbers	Partial Products (2- by 2-Digit Numbers)	4.NBT.B.5
5	2	Multiply two 2-digit numbers	Partial Products (2- by 2-Digit Numbers)	4.NBT.B.5
6	2	Add multi-digit numbers	Add Multi-Digit Numbers	4.NBT.B.4
7	2	Add multi-digit numbers	Add Multi-Digit Numbers	4.NBT.B.4
8	1	Identify partial products	Partial Products (2- by 2-Digit Numbers)	4.NBT.B.5
9	1	Estimate multiplying two 2-digit numbers	Estimate Products (Whole Number Factors)	4.NBT.B.5
10	2	Multiply a whole number by a power of 10	Multiply 2-Digit Multiples of 10	4.NBT.B.5

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.

Unit Opener

Focus Question

Introduce the Focus Question: *How can I multiply multi-digit numbers?*

Ask students to think about what they know about multiplying multi-digit numbers.

- What does multi-digit mean? What are whole numbers?
- What do you know about multiplying multi-digit numbers?
- What do you think you will be doing in the unit?

Remind students that at the end of the unit, they will reflect back on what they learned in this unit.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.



STEM in Action

Videos

Students can watch the two STEM videos.

STEM Career: Entomologist: Owen discusses his aspirations to be an entomologist.

Counting Ladybugs: Owen and entomologists use multi-digit multiplication to help them do their work, including estimating a population.

STEM Project Card

Students can complete the STEM Project Card during their workstation time.



Ignite!

Name: _____

Mile-High Pennies

Use the stacks of pennies below to answer the questions.

Answers will vary. Sample answers are given.

- How many pennies are in a 1-inch stack? 17
How many pennies are in a 2-inch stack? 34
- How many pennies would be in a 1-foot stack? 200
- How is going 1 mile is equal to 5,280 feet how many pennies do you think would be needed to make a stack that is 1 mile tall?
100,000,000
Write a number that is definitely too large for a reasonable estimate: 100,000,000,000
Write a number that is definitely too small for a reasonable estimate: 100
- What is your estimated answer for the number of pennies in a stack that is 1 mile tall? About 1,000,000

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Ignite!

Mile-High Pennies

Students review estimation and multiplication skills in preparation for work in Unit 5.

- Direct attention to the stacks of pennies.
 - What do you notice about the stacks of pennies?
 - Which stack appears to be about 1 inch tall? How many pennies are in that stack?
 - Which stack appears to be about 2 inches tall? How many pennies are in that stack?
- Provide students with a ruler to confirm the above results. Have them record the results with Question 1.
- Have students think about a stack of pennies that is 1 foot tall.
 - About how many pennies do you think would be in that stack? Explain.

Have students record their estimated number of pennies in a 1-foot stack with Question 2

- Now have students think about a stack of pennies that is 1 mile tall.
 - How many pennies do you think would be needed to make a stack that is 1 mile tall? Write your guess with Question 3.
 - Also write a number of pennies that you think is definitely too large for a reasonable estimate. Then write a number of pennies that you think is definitely too small.
- Challenge students to use the above results, along with the images of the pennies and a ruler, to make a calculated estimate of the number of pennies needed to reach a height of 1 mile. You may want to provide the following conversions as needed:

$$12 \text{ inches} = 1 \text{ foot} \qquad 3 \text{ feet} = 1 \text{ yard}$$

$$5,280 \text{ feet} = 1 \text{ mile} \qquad 1,760 \text{ yards} = 1 \text{ mile}$$
- Have students record their calculated estimate with Question 4. Discuss the various strategies that emerge.
 - How did you solve the problem?
 - How does your estimate compare with the guess you made with Question 3?

Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson
Game Station	Game Station 	Students build proficiency with multiplying multi-digit whole numbers. <ul style="list-style-type: none"> • Powers of 10 Concentration 5-1 • Multiplying by 10 Tic Tac Toe 5-2 • Estimating Products Bingo 5-3 • Area Model Task Cards 5-4 • Partial Products Concentration 5-5 • Multiplication Standard Algorithm Task Cards 5-6 • Multiplication Showdown 5-7 	
	Digital Game 	Dino Dig Student multiply with area models.	5-1
Have students complete at least one of the Use It! activities for this unit.			
Application Station	STEM Project Card 	Make a Pulley System Students use measurements 5-7 to create a pulley system.	
	Connection Card 	Washington Color School Movement—Color Field Painting Students create art to represent a base number with an exponent.	5-1
	Real World Card 	Let's Celebrate Students use charts to create a budget for a graduation celebration.	5-3

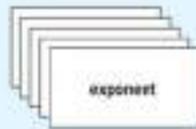
Additional Resources

Use the resources below to provide additional support for this unit.



Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the new terms on the front side of the card.



Foldables

Use the unit foldables with Lessons 5-5 and 5-6.

	10 ⁰	10 ¹	10 ²	10 ³
10 ⁰	1	10	100	1,000
10 ¹	10	100	1,000	10,000
10 ²	100	1,000	10,000	100,000
10 ³	1,000	10,000	100,000	1,000,000

Spiral Review

Students can complete the Spiral Review at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
5-1	5.MD.C.3
5-2	5.NBT.A.1
5-3	5.MD.C.5
5-4	5.NBT.A.3
5-5	5.NBT.A.2
5-6	5.NBT.A.4
5-7	5.NBT.B.5

Understand Powers and Exponents

Learning Targets

- I can write a power of 10 as a multiplication expression with factors of 10.
- I can write a power of 10 using a base of 10 and exponents.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.A** Understand the place value system.
- ◆ **5.NBT.A.2** Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

Math Practices and Processes

MPP Look for and make use of structure.

Focus

Content Objectives

- Students write a power of 10 as a multiplication expression with factors of 10.
- Students write a power of 10 using a base of 10 and exponents.

Language Objectives

- Students explain the steps to take to write a power of 10 as a multiplication expression while using the passive voice.
- To support maximizing linguistic and cognitive meta-awareness, ELs participate in MLR6: Three Reads.

SEL Objective

- Students demonstrate self-awareness of personal strengths and areas of challenge in mathematics.

Coherence

Previous

- Students recognized that a digit represents 10 times as much as it represents in the place to its right and $\frac{1}{10}$ of what it represents in the place to its left (Unit 3).

Now

- Students extend their understanding of place value to write powers of 10 using exponents.

Next

- Students examine patterns based on place value when a whole number is multiplied by a power of 10 (Unit 5).
- Students write and evaluate numerical expressions involving whole-number exponents (Grade 6).

Rigor

Conceptual Understanding

- Students develop conceptual understanding by connecting the ideas of powers and exponents.

Procedural Skill & Fluency

- Students solve and evaluate expressions with powers of 10.

Application

- Students apply their understanding of powers and exponents to solve problems based on real-world contexts.

Application is not a targeted element of rigor for this standard.

Vocabulary

Math Terms

base
exponent
exponential form
power of 10

Academic Terms

accurate
prove

Materials

The materials may be for any part of the lesson.

- number cubes

Number Routine

Find the Pattern, Make the Pattern

5–7 min

Build Fluency Students build number sense as they determine a pattern in a sequence of numbers and find the missing terms. Then they create a new sequence with the same pattern but different numbers.

These prompts encourage students to talk about their reasoning:

- How did you determine the pattern in the sequence of numbers?
- How can you explain to someone what steps to take to find a pattern?
- How did you determine the missing numbers?
- How did you determine the starting point of your sequence?

Purpose Students analyze four multiplication expressions and identify any similarities and/or differences.

Which Doesn't Belong?

- Which doesn't belong?

Teaching Tip You may wish to have students work in small groups to discuss what they notice about the multiplication problems. Invite them to share what they are wondering and how they decide how to compare and contrast the expressions. Remind students that there are multiple ways to answer the question and stress the importance of their justification using correct mathematical terminology.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' awareness of multiplication expressions whose factors are the same number and are based on possible comments and questions that students may make during the share out.

- What do you notice about the factors in each expression?
- What do you notice about the product of each expression?

Math is... Mindset

- What do you want your classmates to know about your math story?

Self-Awareness: Accurate Self-Perception

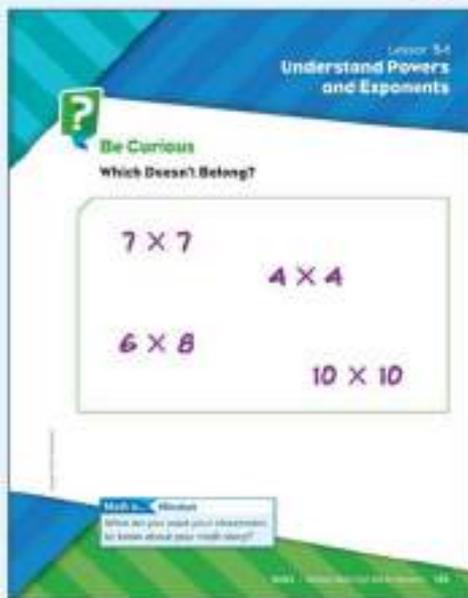
As students begin to think about identifying similarities and differences in the Which Doesn't Belong routine, encourage them to make connections to strategies/concepts they are more familiar or comfortable with, such as the similarities and differences in each factor. They can also use more familiar strategies to check their answers. As students continue to understand powers and exponents, differentiate instruction to provide opportunities for students to experience success and gratification as well encounter appropriate amounts of productive struggle.

Transition to Explore & Develop

Ask questions that get students thinking about multiplication expressions whose factors are the same number.

Establish Mathematics Goals to Focus Learning

- Let's think about multiplication expressions whose factors are the same number and other ways to write those types of expressions.



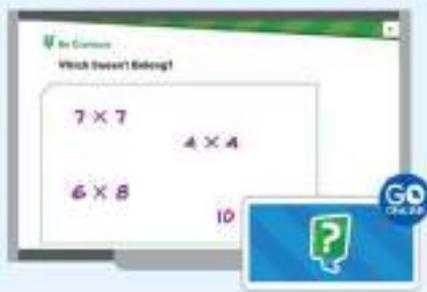
Lesson 5-4
Understand Powers and Exponents

Be Curious
Which Doesn't Belong?

7×7 4×4

6×8 10×10

Math is... Mindset
What do you want your classmates to know about your math story?



Be Curious
Which Doesn't Belong?

7×7 4×4

6×8 10

GO ON!

Learn

At Bank 1, Drew had 10 pennies half a year ago. She increased the number of pennies by 10 times the previous year.

During each year, Drew had 1,000,000 pennies.

You can organize the information in a table to help understand the situation.

Year	Number of Pennies (Previous Year)	Number of Pennies (This Year)
1	10	10
2	10×10	100
3	$10 \times 10 \times 10$	1,000
4	$10 \times 10 \times 10 \times 10$	10,000
5	$10 \times 10 \times 10 \times 10 \times 10$	100,000
6	$10 \times 10 \times 10 \times 10 \times 10 \times 10$	1,000,000

Drew will have 1,000,000 pennies in Year 6.

You can write a power to tell us a multiplication expression with factors of 10. The last zero in a power of 10 is **exponent**. **How many 10s are there in a power of 10?**

Work Together

Why not use a multiplication problem? Here's one to try:

$$10 \times 10 = 100,000,000$$

1 Pose the Problem

1.1 Collect and Display

As students discuss the questions, make a list of key words and phrases you hear, such as *power of 10*, *exponential form*, *base*, and *exponent*. Display the list and use these expressions to help students connect words they already know and math vocabulary.

1.2 Pose Purposeful Questions

- How can you describe the problem in your own words?
- How could you organize the information in the problem?

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Three Reads

1st Read: Have students underline the key numbers that will be used to solve the problem.

2nd Read: Have students write the meaning of each number in context.

3rd Read: Have students work in pairs to create mathematical expressions until they get to 1,000,000 pennies.

3 Bring It Together

3.1 Elicit and Use Evidence of Student Thinking

- How can you write a product where all the factors are 10 using exponential form?

Key Takeaways

- A power of 10 is the product of 10 multiplied by itself a number of times.
- A power of 10 can be written in exponential form.

Work Together

Students write a power of 10 as a multiplication problem and then as a product.

Common Error Students may often write the product as 10 followed by 8 zeros. Make sure they understand the pattern that 10 followed by 8 zeros.

3.2 Language of Math

An *exponent* is also a person who believes strongly in an idea, as in, “She is an exponent of the teachings of Euclid,” or a person who is highly skilled, as in “He is the world’s leading exponent of classical trombone.”

Activity-Based Exploration

Students represent powers of 10 using small objects and compare what 10, 100, and 1,000 of the objects look like. They use these findings to predict what 1,000,000 objects will look like.

Materials: small objects, such as centimeter blocks, paper clips, cereal, beans, and toothpicks

Directions: Partners choose an object and determine what 10, 100, 1,000 of the object looks like. They use these findings to describe and predict what 1,000,000 objects would look like. Have students determine a way to represent their findings for others to see.

Implement Tasks That Promote Reasoning and Problem Solving

- About how big will 1,000 of your objects be?
- How will 1,000 of your objects compare to 1,000 of a smaller object?
- What did you discover when representing 10, 100, and 1,000?
- How did you use multiplication to help you think about what 1,000,000 objects would look like?
- How did your estimate compare with your findings?
- How did the size of your object affect what the values looked like?

Activity Debrief: Have students share their representations of 10, 100, and 1,000 and their prediction of what 1,000,000 looks like. Tell students that these numbers are called *powers of 10* and that they are created by starting with 1 and repeatedly multiplying by 10. Explain that powers of 10 can be written in *exponential form*, using a *base* and an *exponent*. Have students add to their representations to show each number written in exponential form.

Math is... Patterns

- What patterns do you notice when representing powers of 10?

Students look for and use mathematical patterns to understand and solve the problem.

Have students revisit the Pose the Problem question and discuss answers.

- During which week will Dean add 1,000,000 pennies?

English Learner Scaffolds

Entering/Emerging Support students in understanding the passive by demonstrating. Show students two tens rods. Connect the two tens rods. Say *These tens rods can be connected*. Repeat the task twice with new objects, using the passive with *can*. Finally, put a group of chips on the table, and demonstrate counting them. Say *Complete the sentence: These chips can [be counted]*.

Developing/Expanding Support students in understanding the passive *can* by demonstrating. Show students two tens rods then connect them. Say *These tens rods can be connected*. Next, put a group of chips on the table, and demonstrate counting them. Say *Complete the sentence: These chips can [be counted]*. Finally, ask students to make their own sentence using the passive with *can*.

Bridging/Reaching Ask students to explain how a power of 10 can be written in exponential form. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, it can't be written.... or No, that's incorrect because....*

Guided Exploration

Students use the relationship between repeated multiplication and the product to develop an understanding of powers and exponents.

Facilitate Meaningful Mathematical Discourse

- **Think About It:** How can the table help you understand the problem?
- How can you use place value to help you determine $10 \times 10 \times 10$?
- Have the students fill in the row for Week 4 on their own. Ask:
 - What multiplication expression can you use to represent the number of pennies in Week 4?
 - How can you use place value to help you determine $10 \times 10 \times 10 \times 10$?
- Have the students write the exponential forms for each row. Ask:
 - What is the base for each exponential form? How do you know?
 - What is the exponent for each exponential form? How do you know?
 - How is writing 1,000 in exponential form the same as writing $10 \times 10 \times 10$? How is it different?
 - What happens to the value of the digit 1 for each power of 10?
 - **Think About It:** How can you use place value to justify the pattern in the number of zeros?

Math is... Patterns

- What patterns do you notice in the table?

Students look for and use mathematical patterns to understand and solve the problem.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Understand powers of 10	5.NBT.A.2
2	2	Understand powers of 10	5.NBT.A.2
3	2	Understand powers of 10	5.NBT.A.2

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

3 of 3	Additional Practice or any of the U or T activities
2 of 3	<i>Take Another Look</i> or any of the U activities
1 or fewer of 3	Small Group Intervention or any of the H activities

Key for Differentiation

- U** Reinforce Understanding
- T** Build Proficiency
- H** Extend Thinking



Lesson 5.1
Exit Ticket

Name: _____

- Which operation from numbers each power of 10? (circle the appropriate base on the axis.)

10,000	10 ⁴
1,000	10 ³
100,000	10 ⁵
- Which is equivalent to 10⁴? (circle all that apply.)
 - A. 10 × 10
 - B. 10 × 10 × 10 × 10
 - C. 10 × 10 × 10 × 10 × 10
 - D. 1,000
 - E. 10,000
 - F. 100,000
- Which is equivalent to 1,000,000? (circle all that apply.)
 - A. 10 × 10
 - B. 10 × 10 × 10 × 10 × 10
 - C. 10 × 10 × 10 × 10 × 10 × 10
 - D. 10 × 10 × 10 × 10 × 10 × 10 × 10
 - E. 10⁶
 - F. 10⁷

Reflect On Your Learning

On _____ (circle) One day _____ (circle) Understanding _____ (circle) I got help _____ (circle)

Assessment Resource Book 19

R Reinforce Understanding

SMALL GROUP

Roll It and Write It!

Work with students in small groups. Provide students with a number cube. Have students write a base of 10 and then roll the number cube to obtain an exponent. Students write the expression using an exponent and as a multiplication expression and find the product. Make sure students recognize how the expressions are related.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Introduction to Powers of 10
- Powers of 10 (Exponents)



INDEPENDENT WORK

Differentiation Resource Book, p. 37

Lesson 5.2 • Reinforce Understanding

Understand Powers and Exponents

Name _____

Review

The product of multiplying 10 by itself a number of times is called a power of 10.

$$10^2 = \underbrace{10 \times 10}_{\text{2 times}}$$

= 10,000

10^3 would be a 10 with 3 zeros after the one.

Write each power of 10 as a product of 10s.

- $10^2 = 10 \times 10$
- $10^3 = 10 \times 10 \times 10$
- $10^4 = 10 \times 10 \times 10 \times 10$
- $10^5 = 10 \times 10 \times 10 \times 10 \times 10$

Write as a product of 10s and as the exponential form.

- $100 = 10 \times 10 = 10^2$
- $10 = 10 = 10^1$
- $1,000,000 = 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 = 10^7$
- $100,000 = 10 \times 10 \times 10 \times 10 \times 10 = 10^5$
- $10,000,000 = 10 \times 10 = 10^7$

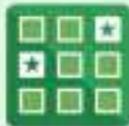
Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Powers of 10 Concentration
Students practice powers of 10 in standard form, as expressions, and with exponents.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 37–38

Lesson 5.2

Additional Practice

Name _____

Review

You can use a base and an exponent to find and represent powers of 10.

For 10²:

in the expression 10², 10 is the base and 2 is the exponent; 10² represents the product, 10 multiplied by 10 to a total of 100.

$$10^2 = 10 \times 10 = 10 \times 10 = 100$$

Represent 10 to the 3rd power in exponential form, using a base and an exponent.

Since 10 is the repeated factor and it is being used as a factor 3 times, 10 will be the base and 3 will be the exponent. Write the expression in exponential form.

$$10 \times 10 \times 10 = 10^3$$

Write each power of 10 as a product of 10s.

- $10^2 = 10 \times 10$
- $10^3 = 10 \times 10 \times 10$
- $10^4 = 10 \times 10 \times 10 \times 10$
- $10^5 = 10 \times 10 \times 10 \times 10 \times 10$

Write the exponential form.

- $10 \times 10 \times 10 = 10^3$
- $10 \times 10 \times 10 \times 10 = 10^4$
- $10 \times 10 \times 10 \times 10 \times 10 = 10^5$
- $10 \times 10 \times 10 \times 10 \times 10 \times 10 = 10^6$

Student Practice Book



Extend Thinking

Use it! Application Station
Washington Color School Movement—
Color Field Painting Students create
 art to represent a base number with
 an exponent.



Own It! Digital Station

Build Fluency Games

Assign the digital game to develop
 fluency with multiplication using
 area models.



WORKSTATIONS

Spiral Review

Assign the digital Spiral Review
 Practice to students or
 download and print PDFs of
 the Spiral Review from the
 Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to
 apply skills and extend thinking.



GO ONLINE

Student Practice Book, pp. 37–38

Write the exponential form of each power of 10.

31. $10 = 10^1$ 32. $10,000 = 10^4$

33. $100 = 10^2$ 34. $10,000,000 = 10^7$

35. A company has a total of 10⁵ employees. How many employees does the company have?
 The company has **100,000** employees.

36. A city has 10⁶ photos on her computer. How many photos does she have?
 She has **1,000,000** photos.

37. A number is 10⁴ more each day. What is this number as a product of 10? What is this number in exponential form?
 $10 = 10 \cdot 10^1$

38. Each day, there is 100 people in each of 10,000 people. What is this number as a product of 10? What is this number in exponential form?
 $10^7 = 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10$

Math
Homework
Activity

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INDEPENDENT WORK

Differentiation Resource Book, p. 38

Lesson 5.4 • Extend Thinking

Understand Powers and Exponents

Given:

1. Complete the missing cells in the table.

Number	Power of 10	Product of 10s
10	10^1	10
100	10^2	10×10
1,000	10^3	$10 \times 10 \times 10$
10,000	10^4	$10 \times 10 \times 10 \times 10$
100,000	10^5	$10 \times 10 \times 10 \times 10 \times 10$
1,000,000	10^6	$10 \times 10 \times 10 \times 10 \times 10 \times 10$
10,000,000	10^7	$10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10$
1 with 8 zeros	10^8	$10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10$

2. Complete the table in this section. Each entry you have in each section, the last one is worth for you.

Number	Power of 10	Product of 10s
100 is written as 10	$10^2 \times 10$ $(10 \times 10) \times 10$	\$1,000
100 are hundred dollars	$1,000 \times 100$ $10^3 \times 10^2 \times 10^2 \times 10^2 \times 10^2$	\$100,000
\$1 are thousand dollar bills	$10 \times 1,000$ $10 \times 10^3 \times 10^3 \times 10^3$	\$10,000
10,000 ten-thousandths	$10,000 \times 10$ $10^4 \times 10^1 \times 10^1 \times 10^1 \times 10^1$	\$100,000

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Patterns When Multiplying a Whole Number by Powers of 10

Learning Targets

- I can determine the products of numbers multiplied by powers of 10 written with exponents.
- I can describe the pattern for multiplying by powers of 10.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.A** Understand the place value system.
- ◆ **5.NBT.A.2** Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

Math Practices and Processes

MPP Construct viable arguments and critique the reasoning of others.

Vocabulary

Math Terms

base
exponent
factor
power of 10

Academic Terms

cite
establish

Materials

The materials may be for any part of the lesson.

- calculators
- index cards

Focus

Content Objectives

- Students use patterns to determine products when multiplying whole numbers by powers of 10.
- Students explain patterns in the products when multiplying whole numbers by powers of 10.

Language Objectives

- Students talk about the patterns they see in products while answering *Wh-* questions.
- To support optimizing output, ELs participate in MLRT: Stronger and Clearer Each Time.

SEL Objective

- Students employ techniques that can be used to help maintain focus and manage reactions to potentially frustrating situations.

Coherence

Previous

- Students recognized that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (Grade 4).
- Students extended their understanding of place value to write powers of 10 using exponents (Unit 5).

Now

- Students examine patterns based on place value when a whole number is multiplied by a power of 10.

Next

- Students estimate products of multi-digit factors to determine if calculations are reasonable (Unit 5).
- Students write and evaluate numerical expressions involving whole-number exponents. (Grade 6).

Rigor

Conceptual Understanding

- Students develop conceptual understanding by multiplying by powers of 10 and looking for patterns and understand the effect multiplying by a power of 10 has on a number.

Procedural Skill & Fluency

- Students build upon the conceptual foundation for the effect of multiplying by a power of 10, which gives students some early experience developing proficiency.

Application

- Students apply their understanding of powers and exponents to solve problems based on real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

Find the Pattern, Make a Pattern

5–7 min

Build Fluency Students build number sense as they determine the pattern and find the missing terms, and then create a new sequence with the same pattern but different numbers.

These prompts encourage students to talk about their reasoning:

- What strategy did you use to determine the pattern and missing numbers?
- How can you tell if your sequence follows the same rule?

Purpose Students think about differences and similarities between four representations of the same number using powers of 10.

Notice & Wonder

- How are they the same?
- How are they different?

Teaching Tip You may wish to divide the class in half and assign one question to each half of the class. Ask students to independently analyze the expressions and answer their question. Then invite students to share their findings and discuss any points of interest that the different perspectives may provide.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of patterns that arise when multiplying a number by powers of 10 and are based on possible comments and questions that students may make during the share out.

- What do you notice about the factors in the expressions?
- What do you notice about the exponents in the expressions?
- What do you notice about the zeros in the expressions?

Math is... Mindset

- What do you do to avoid getting distracted?

Self-Management: Control Impulses

Invite students to set a class Focus Goal for the Notice & Wonder routine by agreeing on a set time that they will independently focus on noticing and wondering. As students work through this time, remind them to be mindful of their collective goal. Model constructive strategies and language for helping others stay on task, as well as for maintaining one's own focus. If students lose focus, allow them to take independent breaks to help them regain their focus.

Transition to Explore & Develop

Guide the discussion to have students analyze the similarities and differences in terms of powers of 10. Ask questions to get students thinking about ways to determine how to relate how the digits of the whole number shift based on the exponent on the power of 10.

Establish Mathematics Goals to Focus Learning

- Let's think about how we can use patterns to multiply a number by powers of 10.

Lesson 5-2
Patterns When Multiplying a Whole Number by Powers of 10

Be Curious
How are they the same?
How are they different?

$15 \times 10,000$
 $15 \times 10 \times 10 \times 10 \times 10$
 15×10^4 $150,000$

Think & Wonder
What do you do to avoid getting distracted?

Be Curious
How are they the same?
How are they different?

$15 \times 10,000$
 $15 \times 10 \times 10 \times 10 \times 10$
 15×10^4 $150,000$

GO ON!

Learn

The distance from Mercury to the Sun is about 36 million miles. Write the distance from Mercury to the Sun in powers of 10.

How can you determine the value of these expressions?

36 × 10⁷ = 36 × 10 × 10 × 10 × 10 × 10 × 10 × 10 × 10
 = 36 × 10,000,000
 = 360,000,000

The distance from Mercury to the Sun is about **36,000,000 miles**.

How can you determine the value of the distance from Mercury to the Sun?

3 × 10⁷ × 1 × 1,000,000
 = 30,000,000

The distance from Mercury to the Sun is about **3,000,000,000 miles**.

When multiplying by powers of 10, there is a pattern to the number of zeros in the product in relationship to the exponent.

Work Together

Find the value of each expression. Explain how you used patterns to find the value.

31×10^3 , $3,200 \times 10^2$, $32,000 \times 10^1$, $320,000$

Student answer: I moved the digits to the left the same number of places as the exponent.

1 Pose the Problem

Pose Purposeful Questions

- What do you notice about the multiplication expressions?
- What is the problem asking you to do?

2 Develop the Math

Choose the option that best meets your instructional goals.

Stronger and Clearer Each Time

Pair students and have them work together to find the values of two expressions. Have them individually write sentences explaining the patterns they used. Then have them share their writing with their partner and, if needed, refine their writing. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How could you explain to a friend how to use place-value patterns to multiply a number by a power of 10?

Key Takeaways

- Multiplying a whole number by a power of 10 results in a discernible pattern – the number of zeros following the whole number is the same as the power.
- The exponent of a power of 10 indicates the number of times 10 is multiplied by itself and is represented by the number of zeros after the whole number.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of how to use patterns to simplify expressions involving a whole number times a power of 10. Have students work on the activity in pairs before asking them to explain how they found their answers.

Common Misconception Students may see and use the “adding zeros” pattern and feel it is incorrect. It is not, but remind them that the digits in a number shifting when it is multiplied by a power of 10 is what establishes that pattern, and they should always understand how and why a shortcut works.

Language of Math

Make sure that students understand the difference between a *multiple* of 10 and a *power* of 10. Encourage students to cite numbers that are powers of 10, then others that are multiples of 10.

Activity-Based Exploration

Students explore place-value patterns when multiplying by powers of 10 and use their patterns to multiply whole numbers by powers of 10.

Materials: calculator

Directions: Students enter any 2-digit whole number on the calculator (e.g. 57), then multiply their number by 10. Have them predict the product before they press the equal key. Students continue to multiply by 10 mentally, challenging themselves to predict the product before they press the equal key.

Depending on the calculator being used, students may notice that they reach a point that an “E” is shown followed by some digits. Ask students to use their patterns to make a conjecture about what the “E” represents.

Implement Tasks That Support Reasoning and Problem Solving

- How did you use mental math to predict the product?
- What happens to the digits each time the number is multiplied by 10?
- What are some ways to record your work to look for patterns?
- How could you summarize the results to predict how multiplying a number by a power of 10 affects the values of the digits?

Math is... Structure

- How can you use place value to explain why the place of the digits in a number shift each time you multiply by 10?

Students use structure to connect place value and multiplying by powers of 10.

Activity Debrief: Have students share their findings when repeatedly multiplying by 10. Encourage students to write their multiplication expressions by writing the powers of 10 in exponential form. Discuss the relationship between the exponent and the number of places the digits shifted.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine the value of these expressions?

English Learner Scaffolds

Entering/Emerging Support students in understanding the term *distance* by demonstrating. Measure the distance between two objects in your classroom; for example, a desk and the door. Say *The [desk] is [three feet] away from the door.* Pause and then say *The distance is [three feet]. Repeat twice with new objects.* Finally, ask students to measure distance, and complete the following sentence, saying it aloud: *The distance is _____.*

Developing/Expanding Support students in understanding the term *distance* by demonstrating. Measure the distance between two objects in your classroom; for example, a desk and the door. Say *The [desk] is [three feet] away from the door.* Pause and then say *The distance is [three feet]. Repeat twice with new objects.* Finally, ask students to measure the distance between two objects, and say it aloud in a sentence using *distance*.

Guided Exploration

Students examine the patterns that arise when multiplying a whole number by a power of 10.

Use and Connect Mathematical Representations

Have the students write the expression 36×10^8 as a product without exponents on their own. Ask:

- What is the base of 10^8 ?
- What is the exponent of 10^8 ?
- How can you write 10^8 as a product? How do you know?
- How do you know that $10 \times 10 \times 10 \times 10 \times 10$ equals 1,000,000?
- How do you know that $36 \times 1,000,000$ equals 36,000,000?

Have the students find the other representations of 3×10^8 on their own. Ask:

- What is the exponent of 10^8 ?
- How many zeros should be in the product? How do you know?

Math is... Structure

- How can you use place value to explain why the place of the digits in a number shift each time you multiply by 10?

Students use structure to connect place value and multiplying by powers of 10.



Bridging/Reaching Ask students to discuss how they can find the distance between two objects in the classroom. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, I disagree because... or No, that isn't the distance...*

On My Own

Name _____

What is the product? Use patterns to solve.

1. $33 \times 10 = 330$ 2. $34 \times 10,000 = 340,000$
 $33 \times 100 = 3,300$ 34 $\times 10,000 = 340,000$
 $33 \times 1,000 = 33,000$ 34 $\times 100,000 = 3,400,000$

3. $33 \times 10^2 = 3,300$ 4. $37 \times 10^3 = 370,000$
 $33 \times 10^3 = 33,000$ 37 $\times 10^4 = 370,000$
 $33 \times 10^4 = 330,000$ 37 $\times 10^5 = 3,700,000$

What is the product?

5. $23 \times 70 = 23,000$ 6. $181 \times 10 = 18,100$
 $3 \times 10 = 30$ 7. $12 \times 10 = 12,000$

What is the unknown factor?

8. $171 \times 80 = 13,680$ 9. $43 \times 100,000 = 4,300,000$
 $6 \times 4 = 24$ 10. $18 \times 10 = 18,000 = 18,000,000$

11. How do you describe the relationship between the equations above?
 Sample answer: Each time the exponent increases by 2, the digits in the first factor shift 2 more places to the left.

12. Which equations are true? Circle or check each.
 A. $8 \times 100 = 8$ B. $8 \times 10 = 80$
 C. $10,000 \times 4 = 40 \times 10 = 400 \times 10 = 4,000$
 D. $16 \times 10^2 = 1,600$
 E. $30 \times 10 = 30 = 300$

13. **Behind Your Backings** Find the unknown factor that is a whole number. Explain your thinking.
 $5 \times 10^4 = 50,000,000$
 $333 \times 10^3 = 33,300,000$. Sample answer: Because multiplying by powers of ten shifts the digits of the factor to the left, you can work backwards and move the digits of the product to the right the same number of places as the power of ten.

Reflect

What patterns did you notice when multiplying by powers of 10?
 Answers vary, vary.

Math is... Mindset
 How have you practiced using strategies?

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 7 Some students may develop a habit of adding the same number of zeros as the power to the first digit of a multiple of 10 or 100, resulting in an error. Make sure they remember to add zeros to the number being multiplied.

Item Analysis

Item	DOK	Rigor
1–12	1	Procedural Skill and Fluency
13–16	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- What patterns did you notice when multiplying by powers of 10?
- Ask students to share their reflections with their classmates.

Math is... Mindset

- What steps did you take to maintain your focus today?
- Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can determine the products of numbers multiplied by powers of 10 written with exponents.
- I can describe the pattern for multiplying by powers of 10.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	3	Multiply whole numbers by powers of 10 patterns	5.NBT.A.2
2	2	Multiply whole numbers by powers of 10 patterns	5.NBT.A.2
3	2	Multiply whole numbers by powers of 10 patterns	5.NBT.A.2
4	2	Multiply whole numbers by powers of 10 patterns	5.NBT.A.2
5	2	Multiply whole numbers by powers of 10 patterns	5.NBT.A.2

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do	
5 of 5	Additional Practice or any of the D or E activities
4 of 5	<i>Take Another Look</i> or any of the D activities
3 or fewer of 5	Small Group Intervention or any of the H activities

Key for Differentiation

- H Reinforce Understanding
- D Build Proficiency
- E Extend Thinking



Lesson 5-2
Exit Ticket

Name _____

- What is the product of the equation? Use a unit tile to find the value.
 $30 \times 10 = 300$
 $30 \times 100 = 3,000$
 $30 \times 1,000 = 30,000$
- Which equation is 3.2×10^3 ?
 A. 320
 B. 3,200
 C. 320,000
 D. 3,200,000
- Which is equivalent to $10^6 \times 10^3$?
 A. 10
 B. 1,000
 C. 1,000,000
 D. 1,000,000,000
- Which power of 10 completes the equation?
 $42 \times \underline{10^2} = 4,200$
- Which exponential form completes the equation?
 $27 \times \underline{10^3} = 2,700,000$

Reflect On Your Learning

100% mastered 75% mastered 50% mastered 25% mastered

○ ○ ○ ○

100% mastered 75% mastered 50% mastered 25% mastered

○ ○ ○ ○

R Reinforce Understanding

SMALL GROUP

Place Value Slide

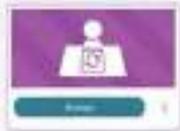
Work with students in small groups. Give each student index cards for the digits 1–9, and three cards with 0. Have each student create a number using three cards. Announce an operation and power of 10, such as “multiply by 100” or “divide by 1,000.” Students shift their cards with respect to the decimal point to display the results, inserting 0s as needed. Have students explain how the operation affects where the decimal point is.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Introduction to Powers of 10
- Multiply by Powers of 10 (Decimal Point)



B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Multiplying by 10 Tic Tac Toe
Students practice multiplying whole numbers and decimals by 10 and 100.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 39

Lesson 5.3 • Reinforce Understanding
Patterns When Multiplying a Whole Number by Powers of 10

Name: _____

Review
Use the pattern in the number of zero digits product when multiplying a whole number by a power of 10.

$38 \times 10 =$	$38 \times 10 = 380$
$38 \times 100 =$	$38 \times 100 = 3,800$
$38 \times 1,000 =$	$38 \times 1,000 = 38,000$

So 38×10^3 is equivalent to 38 with two 0s = 38,000.

Complete the equations.

- $227 \times 100 = 22,700$
- $52 \times 1,000 = 52,000$
- $8 \times 10,000 = 80,000$
- $100 \times 10 = 1,000$

Find the value of each expression.

$45 \times 10^2 = 4,500$	$31 \times 10^3 = 310,000$
$70 \times 10^4 = 7,000$	$8 \times 10^5 = 800,000$
$9 \times 10^6 = 900,000$	$60 \times 10^7 = 600,000$

Differentiation Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 39–40

Lesson 5.3
Additional Practice

Name: _____

Review
You can use a pattern to multiply whole numbers by powers of 10.

It's time to go to the grocery store. There are 50 items in stock, and the grocery purchases 1,000 packs. How many packs does the company purchase?

When multiplying numbers by a power of 10, the product increases 10 times greater for each power of 10.

$50 \times 10^1 = 500$	$50 \times 10^2 = 5,000$
$50 \times 10^3 = 500,000$	$50 \times 10^4 = 500,000,000$

The company purchases 5,000 packs.

Use patterns to find each product.

$1 \times 10 = 10$	$70 \times 1,000 = 70,000$
$20 \times 100 = 2,000$	$70 \times 10,000 = 700,000$
$25 \times 1,000 = 25,000$	$70 \times 50,000 = 3,500,000$

$8 \times 10^2 = 800$	$4 \times 10^3 = 4,000$
$44 \times 10^4 = 440,000$	$8 \times 10^5 = 800,000$
$44 \times 10^6 = 440,000,000$	$8 \times 10^7 = 80,000,000$

Student Practice Book

Estimate Products of Multi-Digit Factors

Learning Targets

- I can explain how to estimate products of multi-digit factors.
- I can estimate products of multi-digit factors to determine if calculations are reasonable.
- I can use an estimated product to make predictions about a calculated solution.

Standards

Major Supporting Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.5** Fluently multiply multi-digit whole numbers using the standard algorithm.

Math Practices and Processes

MPP Use appropriate tools strategically.

Vocabulary

Math Term

estimate
round

Academic Terms

accurate
relevant

Materials

The materials may be for any part of the lesson.

- calculators
- index cards
- number cubes

Focus

Content Objectives

- Students estimate products of multi-digit factors using the same strategies used to estimate products of lesser factors.
- Students use estimated products to make predictions about a calculated solution.
- Students use estimated products to assess the reasonableness of a calculated solution.

Language Objectives

- Students discuss estimating products while answering *Wh-* questions.
- To maximize linguistic and cognitive meta-awareness, ELs participate in **MLR7: Compare and Connect**.

SEL Objective

- Students determine the strategies and analyses necessary to make informed decisions when engaging in mathematical practices.

Coherence

Previous

- Students multiplied two two-digit numbers, using strategies based on place value and the properties of operations (Grade 4).
- Students examined place-value patterns when a whole number was multiplied by a power of 10 (Unit 5).

Now

- Students estimate products of multi-digit factors to determine if calculations are reasonable.

Next

- Students will find products of two- and three-digit factors using area models and partial products (Unit 5).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build their understanding of multiplying multi-digit numbers by estimating products.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students build proficiency estimating the product of multiplying multi-digit numbers.

Application

- Students estimate and find products to solve problems based on real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine About How Much?



5–7 min

Build Fluency Students build number sense as they estimate the sum of two decimals. Remind students that they should use mental math strategies to estimate the sums and that they should not be computing exact answers.

These prompts encourage students to talk about their reasoning:

- What strategy did you use to estimate each sum?
- How can you tell when a calculated sum is not reasonable?
- What is another way to find an estimate?

Purpose Students think about how changing a factor (like what is done when estimating a product) changes a product.

Notice & Wonder

- What do you notice? What do you wonder?

Teaching Tip It may help students understand the Notice & Wonder situation better by thinking of the area on the left as something being covered by the blue rectangles, like a table and tablecloths, or a window and curtains, or pieces of paper.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' noticings and wonderings about how changing a factor in a multiplication equation impacts the product and are based on possible comments and questions that students may make during the share out.

- What factors were changed in the expression 15×12 ?
- Which one is closest in area to 15×12 ?
- Which one is farthest away in area from 15×12 ?

Math is... Mindset

- What helps you make sense of a situation?

Responsible Decision-Making: Analyze Situations

As students work through the Notice & Wonder routine, have them think about alternative ways to consider the factors and products. Encourage students to use a different strategy to check their answer. Remind them that thinking flexibly can help them work through challenging problems/mathematical tasks.

Transition to Explore & Develop

Ask questions that get students thinking about how estimating products can be useful. Guide the discussion to encourage students to think about multi-digit factors that they cannot easily multiply mentally. Encourage students to think about how they can use products of numbers they already know to find estimates.

Establish Mathematics Goals to Focus Learning

- Let's think about how we can find an estimate for a product and how we can use those estimates we find.

Learn

The following 422 people go to the theater. How much money does the theater collect on Tuesday?



You can use strategies you learned to estimate reasonably.

One Way: Compatible numbers	Another Way: Round/Estimate
$422 \approx 400$ $400 \times 12 = 4 \times 100 \times 12 = 4 \times 1,200 = 4,800$ The theater collects about \$4,800.	$422 \approx 400$ $400 \times 12 = 4 \times 100 \times 12 = 4 \times 1,200 = 4,800$ The theater collects about \$4,800.

Multiple-Choice Question
 What amount is an estimated product of 422 and 12?
 A. \$4,800
 B. \$4,200
 C. \$4,000
 D. \$4,000

Work Together

Estimate the product of 475 and 26. **\$12,550**
 Which strategy did you use? Explain why.
Sample answer: 36,500; Check students' responses.

180 Grade 4 • Math • Student Resource Book

1 Pose the Problem

1.1 Pose Purposeful Questions

- What operation will you use to solve the problem?
- Do you need to find an exact answer? Why or why not?

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Compare and Connect

Pair students. Provide students with a problem similar to the one on the Learn page. Instruct each student to solve it individually, and then have the students compare and contrast the strategies they used. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

3.1 Elicit and Use Evidence of Student Thinking

- How are using compatible numbers and rounding to estimate products similar? How are they different?
- How can estimating a product help you determine whether a calculated product is reasonable?

Key Takeaways

- Estimating products can help make predictions about a calculated solution.
- Estimating products helps assess the reasonableness of a calculated solution.
- Strategies used to estimate products of lesser factors, such as rounding and compatible numbers, can also be used to estimate products of multi-digit factors.

Work Together

As students share out their responses, ask them to explain the differences in the strategies used and their estimates. Encourage students to make predictions about the calculated product based on their estimates.

Common Misconception Remind students that there are no real “rules” for creating compatible numbers or rounded numbers to use in their estimates. The goal is to find two numbers that are easy for them to multiply mentally and quickly.

3.1.1 Language of Math

Looking at 6 jelly beans and knowing there are 6 of them without counting is called *subitizing*. Looking at a jar full of jelly beans saying there are “about 100 of them” is *estimating*. Students practiced subitizing when they were younger and just learning numbers.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students estimate products of multi-digit factors using various strategies. They will compare their estimates.

Materials: number cubes

Directions: Students play a game where the greater estimate wins. Have students discuss estimation strategies they have used in the past, and how they can apply those strategies to multiplication. Students roll the number cubes to create two 2-digit factors. Each student estimates the product of a multiplication equation using a strategy of their choosing. The student with the higher estimate wins that round.

After students have compared their estimates, students work together to predict whether each estimate is greater than or less than the actual product.

Support Productive Struggle

- How can you make an estimate that you know is greater than the calculated product?
- How can you make an estimate that you know is less than the calculated product?
- Which strategy do you think helps you find a more accurate estimate?

Math is... Choosing Tools

- What can and can't an estimated product tell you?

Students detect possible errors using estimation, recognizing both the insight to be gained from, and limitations of, estimation.

Activity Debrief: Have students share their strategies for determining a greater estimate and their prediction of how their estimate compares to the calculated product. For each multiplication expression shared, provide students with a calculated product. Facilitate a class discussion to use their estimate to assess the reasonableness of the calculated product.

Have students revisit the Pose the Problem question and discuss answers.

- About how much money does the theater collect on Saturday?

English Learner Scaffolds

Entering/Emerging Support students' understanding of using the infinitive to express purpose. Go to your classroom door. Say *I can turn the knob to open the door*. Then pick up a [crayon]. Say, *I can use this [crayon] to [color a picture]*. Finally, ask students to complete the sentence, saying the answer aloud: *I can use a pencil _____ (to write) my name*.

Developing/Expanding Support students' understanding of using the infinitive to express purpose. Go to your classroom door. Say *I can turn the knob to open the door*. Then pick up a [crayon]. Say, *I can use this [crayon] to [color a picture]*. Finally, ask students to say something that they can do, using the same sentence pattern. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to explain how they can use compatible numbers or rounded numbers to find an estimate. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, I disagree because... or No, can use compatible numbers to find an estimate by...*

Guided Exploration

Students use two different strategies to estimate products of multi-digit factors. They will then compare their estimates to the calculated product and use their estimates to assess if the calculated product is reasonable.

Facilitate Meaningful Mathematical Discourse

Have the students mentally find the product of 400 and 15. Make sure they share their strategies and ask useful questions to improve each others' strategies: Ask:

- What strategy did you use? Why?
- Can you understand someone else's strategy?
- How would you find the exact solution to this problem?

- **Think About It:** What other compatible numbers could you use?
- How can you use place value to explain why $43010 = 4,300?$

Have the students compare the calculated and estimated products. Ask:

- Is the calculated result reasonable? Why or why not?
- Why is the estimate using compatible numbers greater than the calculated product?
- Will compatible numbers always result in an estimate greater than the calculated product? Why or why not?
- Why is the estimate using rounded numbers less than the calculated product?
- Will rounded numbers always result in an estimate greater than the calculated product? Why or why not?

Math is... Choosing Tools

- What can and can't an estimated product tell you?

Students detect possible errors using estimation, recognizing both the insight to be gained from, and the limitations of, estimation.



On My Own

Estimate the products. *Strategic decisions are shown.*

1. 612×30 325×43
 $600 \times 30 = 18,000$ $300 \times 70 = 21,000$

2. 432×27 812×49
 $400 \times 30 = 12,000$ $800 \times 50 = 35,000$

3. On a shopping, 24 students went to a museum. Together they paid \$24. About how much did all students spend on tickets?
Sample answer: $80 \times 30 = \$2,400$

4. The local library has 45 shelves. Each shelf holds 36 books. About how many books does the library have?
Sample answer: $500 \times 40 = 20,000$

5. A teacher at a fair is selling her pastries for \$22 each. Over the course of the fair, 100 people purchase her pastries. About how much did she receive over the course of the fair?
Sample answer: $300 \times 20 = \$6,000$

6. The 4th grade sold 150 school pencils at the fair. Each pencil costs \$20. How much did the 4th grade raise?
Sample answer: $40 \times 400 = \$4,000$

7. **Ben's Answer:** His estimate for the product of 492 and 22 was 1,200. How do you disagree with him?
Sample answer: I do not agree with him. Using compatible numbers, 500×20 gives an estimate of 10,000.



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10. Which equation represents a reasonable estimate for 802×19 ?
 Reason: **Check students' explanations.**

A. $80 \times 10 = 8,000$
 B. $800 \times 20 = 16,000$
 C. $800 \times 21 = 16,800$

11. If you estimate the product of 298×38 , will the product be greater using rounded numbers or compatible numbers? Why?
Compatible; the factors using compatible numbers would be $300 \times 40 = 12,000$, and rounded numbers would be $200 \times 40 = 8,000$.

12. **Extend Your Thinking:** If predicting that there are about 4,000 books before each of the 25 students in the class collected 22 books a day for 5 days. About how many books did they collect at the end of the day? Do they meet their goal?
Sample answer: The club collected about 16,000 books, so they likely met their goal.

Exit Ticket

Why can you use estimates to determine whether a calculated result is reasonable?
Answers may vary.

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercise 9 If students front-end estimate to 400 and 30, they may see that $4 \times 3 = 12$ and forget the correct place value, so about 1,200 would seem like an estimate of the product. Remind students to make sure they are using the correct place value when estimating using rounded numbers.

Item Analysis

Item	DOK	Rigor
1–4	1	Procedural Skill and Fluency
5–8	2	Application
9–12	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you use estimates to determine if a calculated product is reasonable?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did flexible thinking help you with your work today?

Students reflect on how they practiced responsible decision-making.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain how to estimate products of multi-digit factors.
- I can estimate products of multi-digit factors to determine if calculations are reasonable.
- I can use an estimated product to make predictions about a calculated solution.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Estimate products of multi-digit numbers	5.NBT.B.5
2	2	Estimate products of multi-digit numbers	5.NBT.B.5
3	2	Estimate products of multi-digit numbers	5.NBT.B.5
4	2	Estimate products of multi-digit numbers	5.NBT.B.5
5	3	Estimate products of multi-digit numbers	5.NBT.B.5

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
5 of 5	Additional Practice or any of the R or E activities
4 of 5	<i>Take Another Look</i> or any of the R activities
3 or fewer of 5	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- R Build Proficiency
- E Extend Thinking



Lesson 5-3
Exit Ticket

Name: _____

- Which tile represents the product for 38×327 ?
 - A. 12×300
 - B. 60×400
 - C. 300×400
 - D. 600×300
- Which tile represents the product for 27×89 ?
 - A. 30×90
 - B. 30×90
 - C. 40×90
 - D. 40×90
- Estimate the product 102×37 .
Sample answer: $100 \times 30 = 3,000$
- A movie theater seats 120. During one day, a theater sold 478 tickets. About how many more did the theater receive that day?
 - A. 600
 - B. $6,000$
 - C. $60,000$
 - D. $600,000$
- A rectangular field measures 700 feet long and 90 feet wide. About how much is the area of the field?
Sample answer: $800 \times 90 = 72,000$ square feet

Reflect On Your Learning

On a scale of 1 to 4, how confident are you about your understanding of the lesson concepts?

1 2 3 4

Assessment Resource Book 146

R Reinforce Understanding

SMALL GROUP

Is the Product Reasonable?

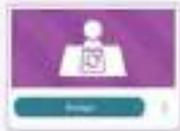
Prepare a set of index cards with expressions describing the product of one 2-digit number and one 3-digit number. Provide some cards showing the correct product and some showing a clearly incorrect product. Work with students to use estimation strategies to determine which products are reasonable and which are incorrect.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Estimate Products (Whole Number Factors)



INDEPENDENT WORK

Differentiation Resource Book, p. 41

Lesson 5.3 • Reinforce Understanding
Estimate Products of Multi-Digit Factors

Name: _____

Review
 You can multiply with models of 10 to help when estimating products of multi-digit factors.

Estimate the product 52×308 .

$$\begin{aligned} 50 \times 300 &= 5 \times 10 \times 3 \times 100 \\ &= 5 \times 3 \times 10^3 \\ &= 15 \times 10^2 \\ &= 1,500 \end{aligned}$$

Estimate the product using number names or multiples of 10. Check students' answers. Sample answers given.

1. 123×52 $700 \times 80 = 56,000$	4. 200×40 $800 \times 60 = 48,000$
2. 189×22 $950 \times 58 = 30,000$	5. 300×27 $300 \times 30 = 9,000$
3. 200×11 $200 \times 10 = 2,000$	6. 140×90 $700 \times 90 = 63,000$

Estimate the product presented in the word problems.

1. The classroom library has 12 shelves. Each shelf holds 52 books. About how many books does the classroom library have in all? Show your work. $12 \times 50 = 600$

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Estimating Products Bingo Students practice finding estimated products.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 41–42

Lesson 5.3
Additional Practice

Name: _____

Review
 You can use rounding or compatible numbers to estimate a product.

Flyer and 200 students bring in school. Each student donates 5 pennies worth. About how many pennies does the classroom have?

$$\begin{array}{r} 200 \times 5 = 1,000 \\ \downarrow \quad \downarrow \\ 200 \text{ rounds to } 200 \\ 5 \text{ rounds to } 5 \\ \hline 200 \times 5 = 1,000 \end{array}$$

A compatible number is that the estimated product is 2,000 when you round.

Estimate each product. Use 1–35. Sample answers shown.

1. $21 \times 17 =$ <u>400</u>	20. $20 =$ <u>8,000</u>
2. $30 \times 23 =$ <u>700</u>	21. $20 =$ <u>9,000</u>
3. $12 \times 187 =$ <u>80</u>	22. $700 =$ <u>86,000</u>
4. $37 \times 300 =$ <u>60</u>	23. $300 =$ <u>30,000</u>
5. $700 \times 4 =$ <u>700</u>	24. $80 =$ <u>8,000</u>
6. $400 \times 2 =$ <u>300</u>	25. $50 =$ <u>20,000</u>
7. $70 \times 100 =$ <u>80</u>	26. $500 =$ <u>60,000</u>
8. $24 \times 700 =$ <u>20</u>	27. $700 =$ <u>14,000</u>

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication using area models.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 41–42

9. One window of a certain type costs 32 dollars. How much do 25 windows of this type cost? Round your answer to the nearest dollar. Show your work and label your units.
- Sample answer:** $32 \times 25 = 2,500$; about 2,500 dollars.
10. One student reads 120 pages each day. How many pages does she read in 30 days? Round your answer to the nearest hundred pages. Show your work.
- Sample answer:** $120 \times 30 = 3,600$; about 3,600 pages.
- Decide whether the calculation is reasonable. Explain why or why not.
11. Find the product. 70 by 500. Use a strategy to estimate the product. **Yes.** Sample answer: The exact estimate is $70 \times 50 = 3,500$. This estimate is close to the calculation, which shows that the calculation is reasonable.
12. Find each product. Round to the nearest hundred dollars. **Yes.** Sample answer: The exact estimate is $220 \times 70 = 15,400$. This estimate is far from the calculation, which shows that the calculation is not reasonable.



Use the Student Practice Book to help students practice estimating the product using the area model. Use the Student Practice Book to help students practice estimating the product using the area model. Use the Student Practice Book to help students practice estimating the product using the area model.

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M

Extend Thinking

Use It! Application Station

Let's Celebrate Students use charts to create a budget for a graduation celebration.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Differentiation Resource Book, p. 42

Lesson 5-3 • Extend Thinking Estimate Products of Multi-Digit Factors

Name:

Estimate the following products by determining which product is greater. The first one to do so for you.

Problem	Product A	Product B	Product C
1.	15×243 30×200 1,800	22×298 20×300 6,000	
2.	50×788 60×293 $= 17,580$	50×800 60×100 $= 6,000$	
3.	80×18 200×80 $= 16,000$	100×70 150×90 $= 13,500$	
4.	500×87 600×70 $= 42,000$	400×60 $= 24,000$	
5.	800×20 800×30 $= 24,000$	700×30 800×20 $= 16,000$	
6.	70×643 80×600 $= 48,000$	50×500 60×580 $= 34,800$	

1. $30 \times 243 = 7,290$ dollars and $22 \times 298 = 6,556$ dollars. $7,290$ is greater than $6,556$, so 30×243 is greater than 22×298 .
2. $50 \times 788 = 39,400$ dollars and $60 \times 293 = 17,580$ dollars. $39,400$ is greater than $17,580$, so 50×788 is greater than 60×293 .
3. $80 \times 18 = 1,440$ dollars and $200 \times 80 = 16,000$ dollars. $16,000$ is greater than $1,440$, so 200×80 is greater than 80×18 .
4. $500 \times 87 = 43,500$ dollars and $600 \times 70 = 42,000$ dollars. $43,500$ is greater than $42,000$, so 500×87 is greater than 600×70 .
5. $800 \times 20 = 16,000$ dollars and $800 \times 30 = 24,000$ dollars. $24,000$ is greater than $16,000$, so 800×30 is greater than 800×20 .
6. $70 \times 643 = 45,010$ dollars and $80 \times 600 = 48,000$ dollars. $48,000$ is greater than $45,010$, so 80×600 is greater than 70×643 .

Use Area Models to Multiply Multi-Digit Factors

Learning Target

- I can use an area model and partial products to multiply multi-digit whole numbers.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.5** Fluently multiply multi-digit whole numbers using the standard algorithm.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Look for and make use of structure.

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

area model
decompose
partial products

Academic Terms

debate
speculate

Materials

The materials may be for any part of the lesson.

- none

Focus

Content Objective

- Students use an area model to determine partial products and add partial products to calculate the product.

Language Objectives

- Students explain how to use an area model to multiply while answering *Wh-* questions.
- To support optimizing output, ELs participate in MLR4: Info Gap.

SEL Objective

- Students explore taking different perspectives on approaches to problem solving.

Coherence

Previous

- Students multiplied two 2-digit numbers, using strategies based on place value and the properties of operations (Grade 4).
- Students estimated products of multi-digit factors to determine if calculations are reasonable (Unit 5).

Now

- Students find products of two- and three-digit factors using area models and partial products.

Next

- Students use the partial products strategy to multiply a multi-digit number by a multi-digit number (Unit 5).
- Students add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students connect multi-digit multiplication with area models and partial products to make use of students' conceptual understanding of place value.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students use the conceptual framework provided by the Distributive Property to organize their work and gain skill and fluency in multiplying single-digit numbers by multi-digit numbers.

Application

- Students use the Distributive Property to solve problems based on real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

Greater Than or Less Than

5–7 min

Build Fluency

Students build number sense as they determine whether the sum of two decimals is greater than 100 or less than 100.

Remind students that they should use mental-math strategies to form their comparisons and that they should not be computing exact sums.

These prompts encourage students to talk about their reasoning:

- How did you estimate to determine if the sum is greater than 100 or less than 100?
- How can you use place value to help you answer the question?
- Which digit in each number has the greatest impact on the sum? Which digit is next most important? Explain.

Purpose Students use area models to multiply multi-digit numbers.

Notice & Wonder

- What do you see?

Teaching Tip You may want to have students copy the area model on their own piece of paper. This can help them become familiar with drawing area models later in the lesson.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of how multiplication relates to area models and are based on possible comments and questions that students may make during the share out.

- How could you find the area of the box?
- How does the area of the whole box compare to the area of the boxes inside it?
- If you knew the area of all the smaller boxes, how could you find the area of the box they are inside?

Math is... **Mindset**

- How can you show that you understand your partner's point of view?

Social Awareness: Develop Perspective

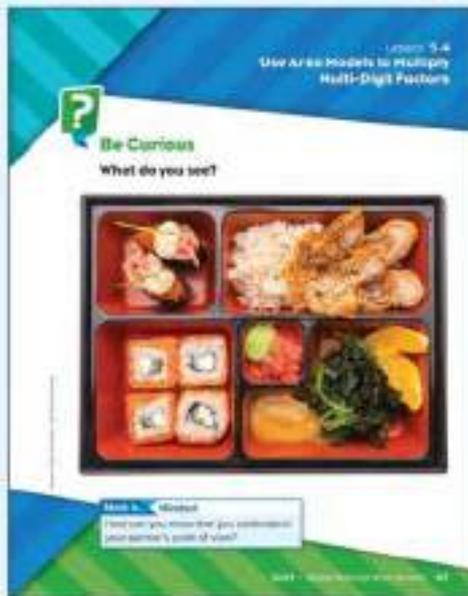
Encourage students to think about different ways to consider the Notice & Wonder routine. With a partner, have them share different tools, strategies, representations, or methods they can use to explain what they see. Invite students to consider and build off their partners' ideas.

Transition to Explore & Develop

Ask questions that get students thinking about how the area of a rectangle can be found by adding the areas of rectangles it is composed of.

Establish Mathematics Goals to Focus Learning

- Let's think about how we can use area models to understand multi-digit multiplication and to calculate products.




Learn
How can you determine the area of the youth soccer field?

You can use an area model to solve 22×74 m².



Decompose the factors by place value.

20	2	0	0
70	0	0	0
0	0	0	0
0	0	0	0

Determine partial products.

20	2	0	0
70	0	0	0
0	0	0	0
0	0	0	0

Math **Meaning**
How does the grid model help you understand multiplication?

Apply the partial products to determine the product.

$$2000 + 330 + 280 + 220 + 20 + 4 = 3,054$$

The area of the soccer field is 3,054 square feet.

You can estimate products to help you check your answer.

Work Together

Use an area model and partial products to determine the product of 304×48 . **28,672**

1 Pose the Problem

Pose Purposeful Questions

- What operation can you use to determine area?
- What strategies do you know for multiplying?

2 Develop the Math

Choose the option that best meets your instructional goals.

Info Gap

Pair students. Provide Partner A with a problem like the one on the Learn page. Provide Partner B with the information to solve the problem. Instruct Partner B to ask A what information they need, and for A to respond, explaining why they need it. Have students continue until the problem is completed.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How do you decompose each factor when you use an area model?
- How do you determine the partial products when you use an area model?
- How do you determine the product when you use an area model?

Key Takeaway

- One multiplication strategy uses an area model to determine partial products, which are then added together to arrive at the product.

Work Together

Before students begin calculating the product, have them first make an estimate using compatible numbers and rounded numbers. After students have calculated the product using an area model and partial products, have them use their estimate to check that the product is reasonable.

Common Misconception Students may be confused about how to decompose 304 since there are no tens in it. Point out that it can be decomposed as $300 + 0 + 4$, or just $300 + 4$.

Language of Math

Tell students that *decompose* means “to break down into simpler elements.” We decompose a number by breaking it down by place value. Similarly, you can decompose words by breaking them down to their base word and prefix or suffix (*unhappy* decomposes into *un-* and *happy* or “not happy”). Either way, decomposing can make things easier to understand.

Activity-Based Exploration

Students explore area models to determine different ways to decompose them to form partial products.

Directions: Ask students to write a multiplication problem using one 3-digit factor and one 1-digit factor and draw an area model to represent the product. Have students record as many ways as possible to decompose the area model. Invite students to share ways they decomposed the area model and focus attention on similar methods of decomposing, such as decomposing by place value.

- Do you think these methods of decomposing will work for multiplying two multi-digit numbers?

Have students explore different ways to decompose an area model that represents the product of 114×72 and find the product.

Support Productive Struggle

- How can you apply your method of using an area model to multiply a 3-digit factor by a 1-digit factor to multiplying a 3-digit factor by a 2-digit factor?
- Is your answer reasonable? How do you know?
- How is your area model the same as or different from another student's method?

Math is... Modeling

- How does an area model help you understand multiplication?

Students map the quantities in a practical situation using a model, and assess if the model has served its purpose.

Activity Debrief: Discuss with students that an area model is one method they can use to multiply multi-digit numbers. Using this method, they can decompose by place value, find partial products, and add partial products to calculate the product of two multi-digit whole numbers.

English Learner Scaffolds

Entering/Emerging Support students' understanding of the abbreviation for *feet (ft)* by showing students other common abbreviations they may know. Write the name of a male that students know well on the board. (Mister [Smith]/ Mr. [Smith]) Say, *Mister [Smith]*. Point to *Mister*. Say *Mister* again and point to *Mr*. Say *This is short for mister*. Point to the *M* and *r* in *Mister* for emphasis on the letters used in the abbreviation. Repeat the task with other abbreviations.

Developing/Expanding Support students' understanding of the abbreviation for *feet (ft)* by showing students other common abbreviations they may know. Ask students to look at the Learn page. Ask *Can you find an abbreviation?* Once they find *ft*, ask them to search the page for the full word.

Bridging/Reaching Ask students to explain what *ft* is short for and explain how they know/figured it out. Have students work together to brainstorm other math abbreviations they may know and to sort them into categories, such as people, measurement, etc.

Guided Exploration

Students expand their knowledge of multiplying with multi-digit factors by breaking down factors by place value, creating an area model, finding partial products, and adding partial products to find the product.

Use and Connect Mathematical Representations

- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - Will you use compatible numbers or rounded numbers to estimate the solution? Why?
- Have the students draw their own area models and fill them out as they work through the problem as a class.
 - How can you decompose each factor?
 - How can you determine the multiplication expression that represents the area of each region of the area model?
 - How can you determine the partial product for each region?
- **Think About It:** Is the calculated result reasonable? Why or why not?

Math is... Modeling

- How does an area model help you understand multiplication?

Students map the quantities in a practical situation using a model, and assess if the model has served its purpose.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Use area models to multiply multi-digit factors	5.NBT.B.5
2	2	Use area models to multiply multi-digit factors	5.NBT.B.5
3	3	Use area models to multiply multi-digit factors	5.NBT.B.5

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the or activities
2 of 3	<i>Take Another Look</i> or any of the activities
1 or fewer of 3	Small Group Intervention or any of the activities

Key for Differentiation

- Reinforce Understanding
- Build Proficiency
- Extend Thinking



Lesson 5-4
Exit Ticket

Name: _____

1. What product is shown by the area model?

	300	+ 40	+ 9
40	12,000	1,600	360
300	3,600	1,200	270

A. $50 \times 300 = 15,000$
 B. $50 \times 349 = 17,450$
 C. $57 \times 349 = 19,983$
 D. $57 \times 348 = 19,836$

2. What is the product 23×407 ? Complete the area model.

	200	+ 30	+ 7
40	8,000	2,400	280
200	8,000	700	140

$40 \times 407 = \underline{16,280}$.

3. Every person spends \$27 on a last-day event. At the last game, there were 156 people. How much money was spent at the sporting event?

\$13,902

Reflect On Your Learning

How confident are you about your learning today?

Not confident
 Fairly confident
 Confident
 Extremely confident

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R Reinforce Understanding

SMALL GROUP

Multiplication Challenge

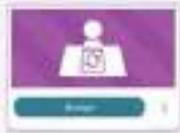
Work with students in groups of 3. The first student writes a single-digit multiplication fact, such as $6 \times 7 = 42$. The second student inserts a digit to the left of the second factor and writes a new equation (for example, $6 \times 57 = 342$). The third student inserts a digit to the left of the 2-digit factor and writes a new equation. Help students understand how to relate the products shown using an area model to the products previously obtained.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Multiply 2-Digit Numbers (Area Models)



INDEPENDENT WORK

Differentiation Resource Book, p. 43

Lesson 5.4 • Reinforce Understanding
Use Area Models to Multiply Multi-Digit Factors

Review

Draw a rectangle for each problem and label its length and width. Multiply to find the area. Add to find the product.

$17 \times 35 = 21 \times 7 + 207 + 67 + 35$

in	300	20	5
10	$10 \times 300 = 3,000$	$10 \times 20 = 200$	$10 \times 5 = 50$
7	$7 \times 300 = 2,100$	$7 \times 20 = 140$	$7 \times 5 = 35$
	5,100	340	85

$17 \times 35 = 3,000 + 2,100 + 200 + 140 + 50 + 35 = 5,525$

Use area models to find the area of the rectangles.

- 670
- 1,790
- 33,470
- 9,860

Use area models to solve these equations.

- $30 \times 20 = 9,288$
- $30 \times 40 = 9,920$
- $30 \times 14 = 7,270$
- $30 \times 16 = 9,258$

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Area Model Task Cards
 Students use area models to multiply.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 43–44

Lesson 5.4
Additional Practice

Review

You can use area models and partial products to determine factors and find products.

A parking lot is 240 feet long and 50 feet wide. What is the area of the parking lot?

To find the area, draw a rectangle and label its length and width.

in	200	40	0
10	$10 \times 200 = 2,000$	$10 \times 40 = 400$	
4	$4 \times 200 = 800$	$4 \times 40 = 160$	
	2,800	560	

Use the area model to find the product.

$2,800 + 560 = 3,360 + 0 = 3,360$

The area of the parking lot is 3,360 square feet.

Use the area model and partial products to solve. Show solutions, model drawings, and number combinations shown.

1. John's lawn has 2 rectangles that are attached. What is the area of the lawn?

in	100	0	0
10	$10 \times 100 = 1,000$		
1	$1 \times 100 = 100$		
	1,100		

The area of the lawn is 1,100 square feet.

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication using area models.



Use It! Application Station
Washington Color School Movement—Color Field Painting Students create art to represent a base number with an exponent.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Student Practice Book, pp. 43–44

Use area models and partial products to solve.

2. $30 \times 40 = 1,200$ $8 \times 30 = 240$

	70	+ 4			200	+ 20	+ 1
40	2,800	160		10	2,000	200	10
5	350	20		8	5,600	160	8

4. $31 \times 734 = 22,754$ $32 \times 603 = 19,296$

	400	+ 20	+ 8		800	+ 3	+ 3
80	32,000	1,600	240	30	24,000	900	90
3	3,000	180	24	2	5,200	6	6

6. What is the area of the computer desk?

	100	+ 40	+ 8
30	3,000	1,200	240
2	200	100	16

The area of the desk is **5,376** square feet.

7. A quarterly goods inventory report had 627 boxes of baseball bats and 1 box of equipment of baseballs, one shipped from 20 shops. The company paid out **18,825** dollars of baseballs.

Health
or
Home
Activity

Read the facts and write a story that uses each fact. Use your own words to describe a number line. An example is provided. An area model is also shown. Use the facts to create a story that uses the facts. Use the facts to create a story that uses the facts. Use the facts to create a story that uses the facts.

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Differentiation Resource Book, p. 44

Lesson 5-4 • Extend Thinking

Use Area Models to Multiply Multi-Digit Factors

Use the missing part of the area models below. Then fill in the blanks for the factors and the product.

1.

	200	60	8
25	4,000	1,200	160
5	1,000	300	40

The product of **245** \times **28** is equal to **6,860**.

2.

	100	80	5
38	38,000	3,200	190
2	2,000	160	10

The product of **40** \times **32** is equal to **12,800**.

3.

	100	0	8
90	9,000	0	720
2	2,000	0	160

The product of **908** \times **18** is equal to **16,344**.

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Use Partial Products to Multiply Multi-Digit Factors

Learning Targets

- I can use partial products to help me multiply multi-digit factors.
- I can explain how to use partial products to multiply.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- ◆ **5.NBT.B.5** Fluently multiply multi-digit whole numbers using the standard algorithm.

Math Practices and Processes

- MPP** Use appropriate tools strategically.
MPP Look for and make use of structure.

Focus

Content Objective

- Students determine partial products by decomposing the factors and adding partial products to calculate the product.

Language Objectives

- Students discuss how to solve multiplication equations using partial products while answering *Wh-* and *Yes/No* questions.
- To support sense-making and cultivating conversation, ELs participate in MLR8: Discussion Supports and MLR3: Critique, Correct, and Clarify.

SEL Objective

- Students practice strategies for persisting at a mathematical task, such as setting a small goal or setting timers for remaining focused.

Coherence

Previous

- Students multiplied two two-digit numbers, using place value and the properties of operations (Grade 4).
- Students found products of two- and three-digit factors (Unit 5).

Now

- Students use the partial products strategy to multiply a multi-digit number by a multi-digit number.

Next

- Students connect the partial products strategy to an algorithm (Unit 5).
- Students add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build their understanding of multiplication by using partial products to multiply multi-digit factors.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students gain skill and fluency in evaluating partial products when multiplying multi-digit factors.

Application

- Students apply their understanding of partial products to solve problems with real-world contexts.

Application is not a targeted element of rigor for this standard.

Vocabulary

Math Terms

area model
partial products suggest

Academic Terms

analyze

Materials

The materials may be for any part of the lesson.

- number cubes

Number Routine

Greater Than or Less Than



5–7 min

Build Fluency

Students build number sense as they determine whether sums and a product are greater than 800 or less than 800. Remind students that they should use mental math strategies to form their comparisons and that they should not be computing exact results.

These prompts encourage students to talk about their reasoning:

- What was your strategy for estimating the value of each expression?
- How did you determine if each expression was greater than 800 or less than 800?
- How do you know that your estimates are reasonable?



Purpose Students explore how an area model relates to a multiplication equation stepped out with partial products.

Notice & Wonder

- What do you notice? What do you wonder?

Teaching Tip Have students work in pairs as they notice and wonder. Encourage students to work together to determine where the factors come from (for example, 40 is from the tens place in 43 and 300 is from the hundreds place in 374).

1.EP Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help students connect an area model to the partial products strategy and are based on possible comments and questions that students may make during the share out.

- How do the strategies appear to be related to one another?

Math is... Mindset

- What steps can you take to focus on your work today?

5.EP Self-Management: Self-Discipline

Help students develop strong learning habits by providing them opportunities to practice self-regulation. Before beginning the Notice & Wonder routine, discuss ways that students will manage distractions and stay focused on their work noticing and wondering.

Transition to Explore & Develop

Ask questions that get students thinking about how they can use partial products to solve a multiplication equation without using an area model. Students should begin to understand multiplication in a more abstract sense.

1.EP Establish Mathematics Goals to Focus Learning

- Let's think about how a strategy using partial products can help us solve multiplication equations.

Lesson 5-5
Use Partial Products to Multiply Multi-Digit Factors

Be Curious
What do you notice?
What do you wonder?

43	374	16072
40	300	12000
3	74	222
43	74	3182
40	70	2800
3	4	12

16072 = 12000 + 222 + 3182 = 12000 + 2800 + 12 = 14812

Math is... Mindset
When working on your table or book, try your notice-wonder!

Be Curious
What do you notice?
What do you wonder?

43	374	16072
40	300	12000
3	74	222
43	74	3182
40	70	2800
3	4	12

16072 = 12000 + 222 + 3182 = 12000 + 2800 + 12 = 14812

GO
5.4.2B

Activity-Based Exploration

Students explore ways to record their work when using partial products to multiply.

Directions: Ask students to write a multiplication problem using one 3-digit factor and one 1-digit factor. Have students determine the product in as many different ways as they can. Invite students to share their different methods, focusing attention on similar methods that involve finding partial products.

Implement Tasks That Promote Reasoning and Problem Solving

- What steps did you take to determine the product?
- What patterns do you notice as you calculate each partial product?
- Is your calculated product reasonable? How do you know?

Activity Debrief: Display a multiplication problem using the vertical format. Work with students to record the steps for finding each partial product, then adding to determine the product.

Math is... Generalizations

- How does the area model help you understand how this strategy works?

Students look for both general methods and shortcuts.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine how many seats are in the stadium?

English Learner Scaffolds

Entering/Emerging Support students in understanding the word *vertical* using manipulatives or drawings and say *This is vertical*. Be sure to motion up-down to emphasize what makes the object/drawing vertical. Then choose two more objects or use two more drawings, one being vertical, and one being horizontal. Show each item, and ask *Is this vertical?*

Developing/Expanding Support students in understanding the word *vertical* using manipulatives or drawings and say *This is vertical*. Be sure to motion up-down to emphasize what makes the object/drawing vertical. Then choose two more objects or use two more drawings, one being vertical, and one being horizontal. Ask students to tell you which item is vertical, and to explain how they know. Provide sentence frames for students who need more guidance.

Guided Exploration

Students use partial products to multiply using multi-digit factors, while following along with an area model.

Use and Connect Mathematical Representations

- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - Will you use compatible numbers or rounded numbers to estimate the solution? Why?
- Have the students draw their own area models and fill them out as they work through the problem as a class. Ask:
 - How can you decompose each factor?
 - How can you determine the multiplication expression that represents the area of each region of the area model?
 - How can you determine the partial product for each region?
- **Think About It:** What patterns do you see in how the place values of the factors are used to find the partial products in this strategy?
- Have the students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Generalizations

- How does the area model help you understand how this strategy works?

Students look for both general methods and shortcuts.



On My Own

Name _____

Use the unknown partial products. Show find the product.

1. 325×33

$$\begin{array}{r} 325 \\ \times 33 \\ \hline 975 \\ 9750 \\ \hline 10725 \end{array}$$

2. 134×17

$$\begin{array}{r} 134 \\ \times 17 \\ \hline 938 \\ 1340 \\ \hline 2278 \end{array}$$

3. What is the product? Use partial products to explain.

3. 85×17

$$\begin{array}{r} 85 \\ \times 17 \\ \hline 595 \\ 850 \\ \hline 1445 \end{array}$$

4. 27×34

$$\begin{array}{r} 27 \\ \times 34 \\ \hline 108 \\ 810 \\ \hline 918 \end{array}$$

5. 26×133

$$\begin{array}{r} 26 \\ \times 133 \\ \hline 78 \\ 780 \\ 2600 \\ \hline 3458 \end{array}$$

6. 223×58

$$\begin{array}{r} 223 \\ \times 58 \\ \hline 1784 \\ 11180 \\ \hline 12934 \end{array}$$

7. A clothing store sold 24 mountain bikes and 24 mountain bikes. How much money did they make selling bikes? **\$5,376**



8. The store you own 12 mountain bikes and 24 mountain bikes. Each for \$251 how much money do they make? **\$4,404**

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9. At a school fundraiser, 507 books for \$21 each. How much money does the school make? **\$10,647**

10. A store has 20 boxes of 100 pens. 12 pens in each box. How many pens are there in all? **2,000 pens**

11. **Self-Analysis** Have your class students check the amount of 00 or 00 instead of 00 or 00. How many? **100 or 100**

12. **Extend Your Thinking** Write and explain your solution. Check students' explanations.

13. **Reflect**

How can you use partial products to find the product of multi-digit numbers?

Answers may vary.

Math in a Minute

What strategy can you use to find the product of 200 and 300?

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Misconception: Exercise 11 Students certainly may include partial products for the ones place in 60. While 0×100 , 0×50 , and 0×2 all yield partial products of 0, including those partial products as "placeholders" can help students better understand how to use the strategy.

Item Analysis

Item	DOK	Rigor
1–6	1	Procedural Skill and Fluency
7–11	2	Application
12–13	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you use partial products to find the product of multi-digit factors?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What steps did you take to focus on your work today?

Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use partial products to help me multiply multi-digit factors.
- I can explain how to use partial products to multiply.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Use partial products to multiply multi-digit factors	5.NBT.B.5
2	2	Use partial products to multiply multi-digit factors	5.NBT.B.5
3	3	Use partial products to multiply multi-digit factors	5.NBT.B.5

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the R or E activities
2 of 3	<i>Take Another Look</i> or any of the R activities
1 or fewer of 3	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- R Build Proficiency
- E Extend Thinking



Lesson 5-5
Exit Ticket

Name: _____

1. Which sum shows how to combine 28 × 73 using partial products?

A.	700	B.	2,030	C.	21,013
	20		30		300
	4		21		140
	50		400		4,200
	4		28		112
	274		5,012		28,014

2. A store set the goal to raise bank and change amounts to \$100. They set 27 percent of that goal. Use partial products to find how much money the store company received.

R A. \$27
E B. \$270
R C. \$497
E D. \$90

3. A rectangular prism measures 240 inches long and 84 inches tall. Use partial products to find the area of the surface.

25,920 square inches

Reflect On Your Learning

How confident? How well knowing? I understand I got help

1 2 3 4

Assessment Resource Book

R Reinforce Understanding

SMALL GROUP

Distribute the Factors

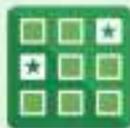
Have students roll number cubes to create two 2-digit numbers. Students then write a multiplication equation and estimate the product. They write the equation using partial products and find the product. Then, they compare their work for accuracy. Help students recognize how the partial products relate to an area model.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Partial Products Concentration
Students use partial products to multiply.

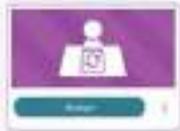


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Multiply 2-Digit Numbers (Area Models)



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 45

Lesson 5.6 • Reinforce Understanding
Use Partial Products to Multiply Multi-Digit Factors

Name: _____

Review
Decompose the factors by place value. Use this to help set up your partial products.

$$\begin{array}{r} 17 \times 32 = 20 \times 30 + 7 \times 30 + 20 \times 2 + 7 \times 2 \\ = 10 \times 30 + 10 \times 30 + 10 \times 2 + 7 \times 20 + 7 \times 20 + 7 \times 2 \\ = 1,000 + 900 + 20 + 2,000 + 140 + 14 \\ = 4,014 \end{array}$$

Use partial products to fill in the blanks and solve these equations.

1. $34 \times 52 = 20 \times \underline{30} + 14 \times \underline{50} + 2$
 $= 10 \times \underline{90} + 10 \times 2 + 0 + \underline{80} + 8 \times \underline{2}$
 $= \underline{800} + 20 + \underline{800} + 16$
 $= \underline{1,740}$

2. $48 \times 27 = 20 \times \underline{20} + \underline{28} \times \underline{20} + 8$
 $= 20 \times \underline{20} + 20 \times 2 + 0 + 0 + \underline{20} \times 8 + 8 \times \underline{2}$
 $= 400 + 40 + 200 + 20 + 0 + \underline{160} + 16$
 $= \underline{8,176}$

Use partial products to solve these equations.

3. $72 \times 18 = \underline{11,880}$ 6. $270 \times 36 = \underline{9,800}$
 4. $32 \times 25 = \underline{7,988}$ 5. $34 \times 48 = \underline{56,216}$

Differentiation Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 45–46

Lesson 5.6
Additional Practice

Name: _____

Review
Use one partial product to find products of multi-digit factors. Find 16 × 28. Decompose the factors by place value. Then use partial products.

$$\begin{array}{r} 16 \\ \times 28 \\ \hline 128 \\ 320 \\ \hline 448 \end{array}$$

The product is 448. *← Add the partial products.*

Use partial products to solve.

5. $37 \times 45 = 1,665$	7. $45 \times 20 = 900$
6. $1,500 + 180 + 180 = 3,360$	8. $2,000 + 200 + 100 = 2,300$
8. $42 + 82 = 3,072$	9. $3,500 + 80 + 48 = 3,628$

Student Practice Book



Extend Thinking

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication using area models.



Use It! Application Station

Make a Pulley System Students use measurements to create a pulley system.

The content of this card has concepts covered later in Lesson 5-7. You may want to assign this card to students ready to explore content covered later in this unit.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Student Practice Book, pp. 45–46

Use partial products to solve.

9. 412×27

$$\begin{array}{r} 32,800 + 5,600 + 800 \\ + 1,200 + 270 + 6 \\ \hline 11,178 \end{array}$$

10. $50,000 + 0 + 90$

$$\begin{array}{r} 50,000 + 0 + 90 \\ + 3,500 + 0 + 30 \\ \hline 53,520 \end{array}$$

11. A teacher printed an investigation with three 844-foot long and 10-foot-wide sheets of paper. How many sheets of paper did she use?

2,484 sheets of paper.

12. A basketball costs \$29. A team orders 20 basketballs. How much more do they need to buy the basketballs?

21,950

13. A rectangle has a perimeter of 220 meters long and 54 meters wide. What is the area of the rectangle?

22,912 square meters.

14. A 1-inch cube can hold out 250 cubes of side length $\frac{1}{2}$ inch. How many cubes can the container hold if it is $\frac{1}{2}$ inch high?

12,500 cubes.

Math
or
Home
Activity

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GO ONLINE

Differentiation Resource Book, p. 46

Lesson 5-5: Extend Thinking

Use Partial Products to Multiply Multi-Digit Factors

Name: _____

Use the partial products to determine the factors in the equations.

1. $\begin{array}{r} 215 \\ \times 34 \\ \hline 7,310 \end{array}$

$5,000 = 20 \times 250$	$\times 200$
$600 = 20 \times 30$	$\times 30$
$100 = 20 \times 5$	$\times 5$
$400 = 4 \times 100$	$\times 100$
$40 = 4 \times 10$	$\times 10$
$24 = 4 \times 6$	$\times 6$

2. $\begin{array}{r} 581 \\ \times 17 \\ \hline 9,877 \end{array}$

$5,000 = 50 \times 100$	$\times 100$
$800 = 10 \times 80$	$\times 80$
$10 = 10 \times 1$	$\times 1$
$2,000 = 20 \times 100$	$\times 100$
$500 = 5 \times 100$	$\times 100$
$7 = 7 \times 1$	$\times 1$

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INDEPENDENT WORK

Relate Partial Products to an Algorithm

Learning Targets

- I can multiply using an algorithm.
- I can describe an algorithm for multiplication.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- ◆ **5.NBT.B.5** Fluently multiply multi-digit whole numbers using the standard algorithm.

Math Practices and Processes

- MPP** Make sense of problems and persevere in solving them.
- MPP** Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

algorithm
partial products
regroup

Academic Terms

procedure
prove

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- number cubes

Focus

Content Objectives

- Students use an algorithm to multiply multi-digit factors by a one-digit factor.
- Students understand and explain a multiplication algorithm.

Language Objectives

- Students discuss strategies to multiply while using *as...as*.
- To support optimizing output, ELs participate in MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students collaborate with peers to complete a mathematical task and offer constructive feedback to the mathematical ideas posed by others.

Coherence

Previous

- Students multiplied two two-digit numbers, using strategies based on place value and the properties of operations (Grade 4).
- Students used the partial products strategy to multiply a multi-digit number by a multi-digit number (Unit 5).

Now

- Students connect the partial products strategy to an algorithm, and use that algorithm to multiply multi-digit numbers by 1-digit numbers.

Next

- Students will use an algorithm to multiply two multi-digit factors (Unit 5).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students develop an understanding of how they can solve problems using a multiplication algorithm.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students demonstrate procedural skill and fluency in performing the steps to solve multiplication equations using an algorithm.

Application

- Students solve real-world multiplication problems using partial products and an algorithm.

Application is not a targeted element of rigor for this standard.

Number Routine

Greater Than or Less Than

5–7 min

Build Fluency

Students build number sense as they determine whether sums of three decimals are greater than 1,200 or less than 1,200. Remind students that they should use mental math strategies to form their comparisons and that they should not be computing exact sums.

These prompts encourage students to talk about their reasoning:

- What strategies did you use to estimate if each sum is greater than 1,200 or less than 1,200?
- How can you use place value to help you estimate the sum?
- Which place-value position in each number has the greatest impact in the sum? Which place-value position is next most important? Explain.
- How do you know your estimates are reasonable?





Purpose Students explore how partial products relate to a multiplication algorithm.

Notice & Wonder

- What do you notice? What do you wonder?

Teaching Tip You may want to have students copy down the equations themselves so that they can more easily compare them as they Notice & Wonder.

1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' curiosity about how partial products relate to an algorithm and are based on possible comments and questions that students may make during the share out.

- What strategy was used on the left to solve the equation?
- How do you think the multiplication equation on the right was solved?

Math is... Mindset

- How can you be part of the classroom community?

1.2 Relationship Skills: Social Engagement

As students engage in collaborative discourse around the Notice & Wonder routine, invite them to give constructive or helpful feedback to their peers. As students engage and discuss how the strategies for multiplying are similar and different, they are strengthening their relationship skills. Remind students that active listening and building on the ideas of others can help them connect with one another and work toward achieving shared goals.

Transition to Explore & Develop

Ask questions that get students thinking about how each multiplication strategy is using place value to find the product. Guide the discussion to have students think about how these strategies can help them determine the product of other multi-digit numbers.

1.1 Establish Mathematics Goals to Focus Learning

- Let's explore an algorithm for multiplying that is related to the partial products strategy.

Lesson 5-6
Relate Partial Products to an Algorithm

Be Curious
What do you notice?
What do you wonder?

$$\begin{array}{r} 342 \\ \times 3 \\ \hline 1026 \end{array}$$

$$\begin{array}{r} 342 \\ \times 30 \\ \hline 10260 \end{array}$$

Math is... Mindset
How can you be part of the classroom community?

Be Curious
What do you notice?
What do you wonder?

$$\begin{array}{r} 342 \\ \times 3 \\ \hline 1026 \end{array}$$

$$\begin{array}{r} 342 \\ \times 30 \\ \hline 10260 \end{array}$$

GO ON!

Learn
The distance from Los Angeles to New York City is 2,450 miles. How far from Los Angeles to Phoenix?

How can you distribute the distance from Los Angeles to New York City?



You can multiply using an algorithm.

Step 1: Multiply the ones.
 $3 \times 3 = 9$
 Partial Products and Tens: 9
 $3 \times 3 = 9$

Step 2: Multiply the tens.
 $3 \times 30 = 90$
 Add the 9 from Step 1:
 $90 + 9 = 99$

Step 3: Multiply the hundreds.
 $3 \times 400 = 1,200$
 The distance from Los Angeles to New York City is 2,450 miles.

Step 4: Summands
 Find the partial products.
 Sum the partial products.

Work Together
 Find the product using an algorithm.

$3021 \times 8 = 24,168$

1 Pose the Problem

Pose Purposeful Questions

- What are you trying to find?
- What strategies do you already know that you can use to calculate the product?

2 Develop the Math

Choose the option that best meets your instructional goals.

Stronger and Clearer Each Time

Pair students and give them a multiplication problem to solve using this algorithm. Have them individually write sentences explaining the steps they took to solve the problem. Then have them share their writing with their partner and revise if necessary. Revisit throughout the lesson for reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How is using this algorithm related to using partial products?
- How do you use this algorithm to solve a multiplication equation?

Key Takeaway

- An algorithm is another way to determine a product.

Work Together

Direct students to estimate the product before they calculate using this algorithm. After students have calculated the product using this algorithm, encourage them to check the product by using partial products. Encourage students to discuss how the two strategies are related. When multiplying using an algorithm, it is a common practice to start by multiplying the digits in the ones place.

Common Error The Work Together problem has a factor with an “internal” zero (3,021). Make sure students understand that this means when they multiply 4 by the digit in the hundreds place, the value will be 0. Encourage students to think of how they would represent the hundreds place in 3,021 using base-ten blocks.

Language of Math

Algorithm comes from the name of the 9th century Persian mathematician, astronomer, and geographer Muhammad ibn Mūsā al-Khwārizmī who was called *Algorismi* in Latin. His Arabic book *Al-jabr* is the first work dedicated to what would come to be known as algebra.

Activity-Based Exploration

Students explore using an algorithm to solve a multiplication problem.

Materials: base-ten blocks

Directions: Display the following multiplication problem. Have students work in small groups to determine a logical sequence of steps that was taken to determine the product. Have students record their steps and explanations. Students may choose to use base-ten blocks or an area model to help make sense of the solution method.

$$\begin{array}{r} 2 \\ 413 \\ \times 7 \\ \hline 2,891 \end{array}$$

Support Productive Struggle

- How can you represent the factors using base-ten blocks?
- How are the two tens regrouped?
- How can you use what you know about partial products to find the sequence of steps used to solve the equation?

Math is... Generalizations

- How are the partial products strategy and this algorithm related?

Students notice if calculations are repeated in the partial products strategy and look for shortcuts.

Activity Debrief: Have students share their sequence of steps to explain the solution method. Explain that an *algorithm* is a step-by-step method for performing calculations. Walk through the steps for the multiplication algorithm shown.

English Learner Scaffolds

Entering/Emerging Support students in understanding using *as...as* for comparing, using manipulatives. Choose two objects that have something in common to compare, such as a ruler and a pencil. Say *The ruler is as straight as the pencil*. Choose two more sets of objects to compare using *as...as*. Finally, show students two more pairs of objects. With one pair make a correct comparison, and with the other pair, make an incorrect one.

Developing/Expanding Support students in understanding using *as...as* for comparing, using manipulatives. Choose two objects that have something in common to compare, such as a ruler and a pencil. Say *The ruler is as straight as the pencil*. Choose two more sets of objects to compare using *as...as*. Finally, ask students to choose two classroom objects to compare, using *as...as*. Provide sentence frames for students who need more guidance.

Guided Exploration

Students apply what they know about solving multiplication equations using partial products to use an algorithm to solve multiplication equations.

Use and Connect Mathematical Representations

- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - Will you use compatible numbers or rounded numbers to estimate the solution? Why?
- Have the students find the product using the partial products strategy. Ask:
 - How will you decompose the factors by place value to find partial products?
- **Think About It:** What other algorithms do you already know how to use?
- Why do you regroup the two tens? How is this different from using partial products? How is it different?
- Have the students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Generalizations

- How are the partial products strategy and this algorithm related?

Students notice if calculations are repeated in the partial products strategy and look for shortcuts.



Bridging/Reaching Ask students to compare two objects using *as...as*. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, that's not correct because...* or *No, that isn't as... as...*

Go My Own

Name _____

What is the product?

1. 207×6
 $\begin{array}{r} 207 \\ \times 6 \\ \hline 1242 \end{array}$

2. 344×2
 $\begin{array}{r} 344 \\ \times 2 \\ \hline 688 \end{array}$

3. 199×3
 $\begin{array}{r} 199 \\ \times 3 \\ \hline 597 \end{array}$

4. 492×2
 $\begin{array}{r} 492 \\ \times 2 \\ \hline 984 \end{array}$

What is the product? Choose the correct answer.

5. $167 \times 7 = ?$
 A. $1,169$
 B. $1,174$
 C. $1,161$
 D. $1,168$

6. $217 \times 6 = ?$
 A. $1,302$
 B. $1,305$
 C. $1,304$
 D. $1,311$

7. $2,832 \times 2 = ?$
 A. $5,664$
 B. $4,236$
 C. $5,662$
 D. $5,666$

8. $2,246 \times 2 = ?$
 A. $4,492$
 B. $4,493$
 C. $4,491$
 D. $4,494$

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9. If You Can Do It... The Empire State Building is 1,250 feet tall. How many feet tall is the Willis Tower in Chicago? **1,450 feet**

10. Money Matters A book costs \$12. How much money does it cost to buy 5 books? **\$60**

11. The Game Plan The number of seats in a stadium is 64,000. How many seats are there in 7 stadiums? **448,000 seats**

12. On a Good Day Emily sold her family's lemonade for 3 days. Each day she sold 300 lemonades. How many lemonades did she sell in all? **900**

13. Extend Your Thinking Explain why it is important to label each step of the algorithm when multiplying. **The calculation will not be correct if one of the steps is left out.**

Reflect

How are partial products used in algorithms for multiplication? **Answers may vary.**

Math is... Mindset

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 1–8 While using this algorithm, some students may add a regrouped amount before performing the multiplication. For example, while calculating Exercise 1 and finding that $6 \times 7 = 42$, students may regroup the 4 tens and add them to the 2 tens before multiplying by 6, rather than multiplying then adding.

Item Analysis

Item	DOK	Rigor
1–8	1	Procedural Skill and Fluency
9–12	2	Application
13	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How are partial products and an algorithm for multiplication related?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you connect with your classmates today?

Students reflect on how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can multiply using an algorithm.
- I can describe an algorithm for multiplication.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Multiply multi-digit numbers by a 1-digit number using an algorithm	5.NBT.B.5
2	2	Multiply multi-digit numbers by a 1-digit number using an algorithm	5.NBT.B.5
3	2	Multiply multi-digit numbers by a 1-digit number using an algorithm	5.NBT.B.5
4	3	Multiply multi-digit numbers by a 1-digit number using an algorithm	5.NBT.B.5

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do	
4 of 4	Additional Practice or any of the ✔ or ✔ activities
3 of 4	<i>Take Another Look</i> or any of the ✔ activities
2 or fewer of 4	Small Group Intervention or any of the ✔ activities

Key for Differentiation

- ✔ Reinforce Understanding
- ✔ Build Proficiency
- ✔ Extend Thinking



Lesson 5-6
Exit Ticket

Name: _____

- Which product is correct? Check all that apply.

<input type="checkbox"/> A. $204 \times 3 = 612$	<input type="checkbox"/> B. $402 \times 3 = 1,206$
<input type="checkbox"/> C. $204 \times 3 = 602$	<input checked="" type="checkbox"/> D. $612 \times 3 = 1,836$
- What is the product? Use an algorithm to solve.

$$\begin{array}{r} 247 \\ \times 6 \\ \hline 1,482 \end{array}$$
- A theater has capacity for 1,024 people. The previous 3 shows have all been sold out. How many people attended the fourth show? Use an algorithm to solve.

<input type="checkbox"/> A. 1,024 people	<input type="checkbox"/> B. 3,072 people
<input type="checkbox"/> C. 3,072 people	<input checked="" type="checkbox"/> D. 1,024 people
- The average attendance at a town's high school basketball games is 2,124 people per game. How many people attended the games if four games are to be played? Use an algorithm to solve.

25,872 people

Reflect On Your Learning

How confident? 1 2 3 4

How ready to understand? 1 2 3 4

How interested? 1 2 3 4

How much did you like it? 1 2 3 4

© Assessment Resources

R Reinforce Understanding

SMALL GROUP

Roll to Multiply

Work with students in pairs. Have students roll a number cube 4 times to create a 3-digit number by 1-digit number multiplication problem. Work with the students to solve the problem, with one student using partial products and the other using an algorithm. Make sure students understand how the algorithm relates to the partial products. Have students switch roles and repeat the process with new numbers.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Multiply 3- by 1-Digit Numbers
- Multiply 4- by 1-Digit Numbers



INDEPENDENT WORK

Differentiation Resource Book, p. 47

Lesson 5.8 • Reinforce Understanding

Relate Partial Products to an Algorithm

Name: _____

Review

Roll a 3-digit number and a 1-digit number. Multiply them using partial products and the standard algorithm.

Example: Roll 352 and 4. Multiply 352×4 .

Partial products: $4 \times 2 = 8$, $4 \times 50 = 200$, $4 \times 300 = 1200$. Add: $8 + 200 + 1200 = 1408$.

Standard algorithm: $352 \times 4 = 1408$.

Find the products of the equations first using partial products and then using an algorithm. Show the steps.

1. $60 \times 8 =$ <u>480</u>	3. $2,024 \times 5 =$ <u>10,120</u>
2. $426 \times 3 =$ <u>1,278</u>	4. $12,000 \times 4 =$ <u>48,000</u>
5. $4,000 \times 3 =$ <u>12,000</u>	6. $7,000 \times 2 =$ <u>14,000</u>
7. $400 \times 2 =$ <u>800</u>	8. $1,000 \times 3 =$ <u>3,000</u>

Find the products of the equations using an algorithm.

9. $60 \times 8 =$ <u>480</u>	10. $2,952 \times 3 =$ <u>8,856</u>
11. $202 \times 4 =$ <u>808</u>	12. $2,814 \times 2 =$ <u>5,628</u>

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Multiplication Standard Algorithm Task Cards

Students identify errors in multiplication using the standard algorithm.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



Student Practice Book, pp. 47–48

Lesson 5.8

Additional Practice

Name: _____

Review

You can use an algorithm to multiply a multi-digit factor and a single-digit factor.

Find the product $2,234 \times 6$. Use the standard algorithm for multiplication.

$$\begin{array}{r} 2,234 \\ \times 6 \\ \hline 13,404 \end{array}$$

The product is 13,404.

Solve using the standard algorithm for multiplication.

1. $4 \times 6 =$ <u>24</u>	2. $10 \times 3 =$ <u>30</u>	3. $200 \times 4 =$ <u>800</u>
4. $7 \times 2 =$ <u>14</u>	5. $3 \times 5 =$ <u>15</u>	6. $4 \times 8 =$ <u>32</u>
7. $3,240 \times 3 =$ <u>9,720</u>	8. $1,775 \times 2 =$ <u>3,550</u>	9. $3,823 \times 4 =$ <u>15,292</u>
10. $4,177 \times 2 =$ <u>8,354</u>	11. $2,000 \times 7 =$ <u>14,000</u>	12. $1,104 \times 8 =$ <u>8,832</u>

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication using area models.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 47–48

Solve using the standard algorithm for multiplication.

$8 \cdot 200$	$8 \cdot 600$	$8 \cdot 800$
$\begin{array}{r} 8 \\ \times 2 \\ \hline 16 \end{array}$	$\begin{array}{r} 8 \\ \times 6 \\ \hline 48 \end{array}$	$\begin{array}{r} 8 \\ \times 8 \\ \hline 64 \end{array}$
592	4,800	6,400

$20 \cdot 40$	$40 \cdot 200$	$40 \cdot 2,000$
$\begin{array}{r} 20 \\ \times 4 \\ \hline 80 \end{array}$	$\begin{array}{r} 40 \\ \times 2 \\ \hline 80 \end{array}$	$\begin{array}{r} 40 \\ \times 2 \\ \hline 80 \end{array}$
800	8,000	80,000

Estimate the product. Think aloud.

12. Maria earns \$100 each month and her part-time job also makes about the same amount for 2 months?
Sample answer: about \$1,200; \$176

14. Jimmy is 27 inches tall. He is growing $\frac{1}{2}$ inch per inch the last month. How tall will he be next month?
Sample answer: about 5,800; 9,678

16. The average attendance at a baseball game is about 30,000 people per game. How many people attended the game 4 times in a row?
Sample answer: about 24,000; 23,126

MATH
Home
Activity

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E

Extend Thinking

Use It! Application Station

Let's Celebrate Students use charts to create a budget for a graduation celebration.



Websketch Exploration

Assign a websketch exploration to apply skills and extend thinking.



Differentiation Resource Book, p. 48

Lesson 5-6 • Extend Thinking

Relate Partial Products to an Algorithm

Name: _____

Break down each problem into a more manageable problem. Use the algorithm to find the product you see. The first problem has been started for you. **Directions: Do complete first sentence only every.**

1. To find the product 200×12 , I could find 200×10 and multiply the result by 2.
 $200 \times 10 = 2,000$
 $200 \times 12 = 2,400$

2. To find the product 400×20 , I could find the product 40×2 and multiply the result by 10.
 $40 \times 2 = 80$
 $400 \times 20 = 8,000$

3. To find the product 300×50 , I could find the product 30×5 and multiply the result by 100.
 $30 \times 5 = 150$
 $300 \times 50 = 15,000$

4. To find the product 100×30 , I could find the product 10×3 and multiply the result by 100.
 $10 \times 3 = 30$
 $100 \times 30 = 3,000$

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WORKSTATIONS

GO ONLINE

INDEPENDENT WORK

Collect and Assess Student Work

Collect and review student responses to determine possible misconceptions. See examples in If-Then chart.

IF incorrect...	THEN the student likely ...	Sample Misconceptions
Student 1: No has difficulty interpreting an area representation for multiplication. The student may not be able to connect the partial products shown in the area representation with the partial products derived in the partial-products strategy.		In this case, the student does not reason about the sum of the partial products shown.
Student 2: Yes does not fully understand the process of using partial products to multiply two 2-digit numbers. The student believes that multiplying the value of the tens digits (40×10) and multiplying the ones digits (2×3), then adding the two partial products, provides the product for 42×13 .		In this case, the student does not consider whether the decomposition of the numbers shown is accurate.
Student 3: No has difficulty recognizing decomposition as a strategy that works for multiplication. Some students fail to recognize that multiplication is commutative: $42 \times 13 = 13 \times 42$, and you can think of this as 13 groups of 40 and 13 groups of 2.		In this case, the student does not recognize when multiplying, a 2nd can be decomposed and each multiplied by 13.

Many of the above difficulties result in a combination of correct and incorrect responses.

For correct responses, be sure to check for sound reasoning.

Take Action

Choose from the following resources or suggestions:

- Revisit estimation and partial products in Lessons 5-3 and 5-5.
- Encourage a routine of using estimation as a tool for determining the reasonableness of answers and approaches.
- Show examples of both correct and incorrect approaches to multiplication to spark a discussion about correct strategies and to address common misconceptions.
- Provide practice decomposing 2-digit numbers to reinforce place-value ideas, such as the fact that the value of a 4 in the tens place is 40, not 4. Discuss how decomposing numbers can make computation easier.
- Connect numeric expressions to the area representation to reinforce that in 2-digit multiplication, each digit of a factor is multiplied by each digit of the other factor.

Revisit the Probe After additional instruction, have students review their initial answers to the probe. Use these questions for discussion:

- Are there any answers you would like to change? Explain why you might want to change them.
- Are there any questions that you still have about any of the exercises on this probe?

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Multiply Multi-Digit Factors Fluently

Learning Targets

- I can use an algorithm to multiply multi-digit factors.
- I can explain how to use an algorithm to multiply.

Standards

Major Supporting Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.5** Fluently multiply multi-digit whole numbers using the standard algorithm.

Math Practices and Processes

- MPP** Make sense of problems and persevere in solving them.
- MPP** Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms	Academic Terms
algorithm	analyze
	note
	transition

Materials

The materials may be for any part of the lesson.

- *Multiplication Algorithm* Teaching Resource
- number cubes
- spinners

Focus

Content Objective

- Students use an algorithm to multiply two multi-digit factors.

Language Objectives

- Students explain how to use an algorithm to multiply while answering *Wh-* and *Yes/No* questions.
- To support maximizing linguistic and cognitive meta-awareness and optimizing output, ELs participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students identify and discuss the emotions experienced during math learning.

Coherence

Previous

- Students multiplied two two-digit numbers, using strategies based on place value (Grade 4).
- Students connected the partial products strategy to an algorithm (Unit 5).

Now

- Students use an algorithm to multiply two multi-digit factors.

Next

- Students multiply decimals (Unit 6).
- Students add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build their understanding of multiplying two multi-digit factors.

Conceptual understanding is not a targeted element of rigor for this standard.

Procedural Skill & Fluency

- Students gain proficiency in using an algorithm to multiply two multi-digit factors efficiently.

Application

- Students apply their understanding of an algorithm of multiplication to solve problems with real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

What's Another Way to Write It?

5–7 min

Build Fluency Students build number sense as they write three different expressions that are equivalent to 7.5.

Remind students that there will be many different possible combinations of numbers and operations that are equivalent to 7.5. As solutions are given, record them for students to evaluate and compare.

These prompts encourage students to talk about their reasoning:

- What numbers might you typically think about using first?
- What strategies did you use to get started?
- How can you use one expression to create a new expression?
- Describe a situation when you would need to write an expression that is equivalent to 7.5.

Learn

Land returned to share over 500 tickets.
How can you determine how much money is shared from selling tickets (approximately)?

You can use an algorithm to solve the problem.

Step 1: Multiply 540 by 5.

$$\begin{array}{r} 540 \\ \times 5 \\ \hline 2,700 \end{array}$$

Step 2: Multiply 540 by 20.

$$\begin{array}{r} 540 \\ \times 20 \\ \hline 10,800 \end{array}$$

Step 3: Add partial products.

$$\begin{array}{r} 2,700 \\ + 10,800 \\ \hline 13,500 \end{array}$$

The school made \$13,500 from selling tickets and returned the money to the community.

Use an algorithm to solve the problem.

Work Together

What is the product?

$$\begin{array}{r} 2,300 \\ \times 25 \\ \hline 57,500 \end{array}$$

1 Pose the Problem

Pose Purposeful Questions

- What are you trying to find?
- What information do you already know?

2 Develop the Math

Choose the option that best meets your instructional goals.

Co-Craft Questions and Problems

Pair students and have them co-create a problem similar to the one on the Learn page. Have them work together to solve their problem and then trade their problem with another pair. After each pair solves the other pair's problems, have them form a group of four to check solutions and correct any mistakes that may have been made. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How is using this algorithm to multiply by a 1-digit number similar to using this algorithm to multiply by a 2-digit number? How is it different?

Key Takeaway

- An algorithm has a consistent process for recording products when multiplying two multi-digit factors.

Work Together

Before students begin calculating the product, have them estimate the product. After students have solved the problem using an algorithm, have them use partial products to solve the equation and discuss how the strategies are related.

Common Misconception Students may only pay attention to the digits in the factors and not their place value. Make sure students remember that, for example, they are multiplying 4×60 instead of 4×6 .

Language of Math

Make sure students understand that *regrouping* means different mathematical processes in different mathematical contexts. Discuss with students the similarities and differences in regrouping in adding, subtracting, or multiplying.

Activity-Based Exploration

Students explore extending a multiplication algorithm to multiply two multi-digit factors.

Materials: *Multiplication Algorithm* Teaching Resource

Directions: Distribute copies of the *Multiplication Algorithm* Teaching Resource. Students will extend what they learned in the previous lesson to complete the algorithm for 549×26 .

Support Productive Struggle

- What digits will you multiply first?
- How will you use regrouping while multiplying?
- What is the last step to finding the product?

Math is... Generalizations

- How might using this algorithm be different when multiplying a 3-digit number by a 3-digit number?

Students notice if calculations are repeated and look for general methods.

Activity Debrief: Have students share their thinking as they complete the algorithm to find the product. Encourage students to think about the value of the digits, rather than simply the digits themselves. For example, rather than multiplying the digit 2 by the digit 9, students should think about the values of the digits.

A PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students use an algorithm to multiply two multi-digit factors.

Facilitate Meaningful Discourse

- Have the students create the equation. Ask:
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - Will you use compatible numbers or rounded numbers to estimate the solution? Why?
- Have the students find the product of 549 and 6 using the algorithm from Lesson 6.
 - **Think About It:** How is the partial product $9 \times 6 = 54$ represented in the product of 549 and 6, and why is it represented that way?

Before multiplying 540 by 20, have the students find the product of 549 and 2 using the algorithm from Lesson 6. After they have found the product, ask:

- How can you use that product and place value arguments to determine the product of 549 and 20?
- **Think About It:** Why is there a 0 in the ones place of the product of 549 and 20?

- Have the students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Generalizations

- How might using this algorithm be different when multiplying a 3-digit number by a 3-digit number?

Students notice if calculations are repeated and look for general methods.



English Learner Scaffolds

Entering/Emerging Support students in understanding the phrase *make/made money*. Set up a mock buying and selling role play. Give a classroom object, such as a book, a price and pretend to buy it from one of your students. Walk over to another student. “Sell” the book to the student for a higher price. Say, *I made [two dollars]*. Mock buy and sell another item with two students, this time asking after the final sale *How much money did I make?*

Developing/Expanding Support students in understanding the phrase *make/made money*. Set up a mock buying and selling role play. Give a classroom object, such as a book, a price and pretend to buy it from one of your students. Walk over to another student. “Sell” the book to the student for a higher price. Say, *I made [two dollars]*. Then ask students to perform a mock buying and selling role play with a group of three. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to perform mock buying and selling role plays with a group of three students. Have them talk about how much money they made. Then have students discuss different ways of expressing making money, such as *made a profit*, etc.

On My Own

Name: _____

What is the product?

1.
$$\begin{array}{r} 27 \\ \times 15 \\ \hline 135 \\ 270 \\ \hline 405 \end{array}$$

2.
$$\begin{array}{r} 282 \\ \times 28 \\ \hline 2256 \\ 5640 \\ \hline 7896 \end{array}$$

3.
$$\begin{array}{r} 105 \\ \times 17 \\ \hline 735 \\ 1050 \\ \hline 1785 \end{array}$$

4.
$$\begin{array}{r} 16 \\ \times 6 \\ \hline 96 \end{array}$$

5.
$$\begin{array}{r} 80 \\ \times 17 \\ \hline 560 \\ 6400 \\ \hline 13600 \end{array}$$

6.
$$\begin{array}{r} 271 \\ \times 38 \\ \hline 2168 \\ 8130 \\ \hline 10302 \end{array}$$

7.
$$\begin{array}{r} 421 \\ \times 14 \\ \hline 1684 \\ 16840 \\ \hline 5894 \end{array}$$

8.
$$\begin{array}{r} 1022 \\ \times 77 \\ \hline 7154 \\ 71540 \\ \hline 78714 \end{array}$$

9. The student on the left can see 2200 items in each jar. The other three of them can see 200 items in each jar. How many items can they see together?
8,800 items

10. In a 100-yard game, you can score 100 points for every 100 yards you run. Jack ran 250 yards. How many points did he score?
250 points

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11. On a road trip, a family traveled 420 miles each day. How many miles had they traveled by the end of 8 days?
3,360 miles

12. An amusement park charges \$12 per ticket. How much money did the park make on 150 tickets?
\$1,800

13. **3784** **classmates** each have 120 teeth. How many of a pair of teeth, they replace the teeth of 25 days. How many teeth do they check in all?
2,730 teeth

14. **Extend Your Thinking** How do you know how to solve multiplication equations using partial products? Why do some multiplication equations using an algorithm?

Sample answer: An algorithm involves partial products by adding the product of a factor and a place value digit with another, knowing how to use partial products beforehand makes using an algorithm easier.

Reflect

Why might using an algorithm be more efficient than using partial products when multiplying?

Answers may vary.

Math 3.0 Answer
What does make you feel confident when using partial products when multiplying?

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 1–8 Some students do not consider the value of the digits when using a standard algorithm. Some omit the 0 in the ones place in the second partial product. If this error occurs in Exercises 1-8, have students work the problems again by using partial products to reinforce the place value of the digits that are multiplied and written in the algorithm.

Item Analysis

Item	DOK	Rigor
1–8	1	Procedural Skill and Fluency
9–13	2	Application
14	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- Why might using an algorithm be more efficient than using partial products when multiplying?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How has organizing your work helped you?

Students reflect on how they practiced self-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use an algorithm to multiply multi-digit factors.
- I can explain how to use an algorithm to multiply.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Multiply multi-digit numbers by a 2-digit number using an algorithm	5.NBT.B.5
2	3	Multiply multi-digit numbers by a 2-digit number using an algorithm	5.NBT.B.5
3	3	Multiply multi-digit numbers by a 2-digit number using an algorithm	5.NBT.B.5

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the G or L activities
2 of 3	<i>Take Another Look</i> or any of the G activities
1 or fewer of 3	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- G Build Proficiency
- L Extend Thinking



Lesson 5-7
Exit Ticket

Name: _____

- What is the product? Use an algorithm.

$$\begin{array}{r} 124 \\ \times 171 \\ \hline 1308 \\ + 20520 \\ \hline 21,288 \end{array}$$
- John collects baseball cards. He packs his cards into 28 groups with 175 cards in each group. How many cards does John have in his collection? Use partial products or an algorithm.
4,900 cards
- A clothing factory makes 2,504 shirts each month. How many shirts will it make in one factory in one year? Use partial products or an algorithm.
33,260 shirts

Reflect On Your Learning

1 = I need more practice
2 = I am still learning
3 = I understand
4 = I got it! I can teach others.

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R Reinforce Understanding

SMALL GROUP

Spin 'n' Roll for Products!

Work with students in pairs using a spinner that contains 2-digit numbers. One student spins the spinner to obtain a factor. The other student rolls a number cube twice to produce a 2-digit factor. Help students multiply the two factors and then check their work using estimation. Have students repeat the process with new numbers.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Multiplication Showdown Students practice multiplication of multi-digit numbers.



GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Multiply Multi-Digit by 2-Digit Numbers
- Multiply 3-Digit by 3-Digit Numbers
- Multiply Multi-Digit Numbers



Interactive Additional Practice

Assign the digital version of the Student Practice Book.



GO ONLINE

INDEPENDENT WORK

Differentiation Resource Book, p. 49

Lesson 5.7 • Reinforce Understanding
Multiply Multi-Digit Factors Fluently

Name _____

Review
 Estimate a product by multiplying using partial products.

$$\begin{array}{r} 683 \\ \times 37 \\ \hline 4,781 \\ + 20,591 \\ \hline 25,372 \end{array}$$
 Multiply: 683×37
 Estimate: $683 \times 37 \approx 25,372$
 Check: $25,372 \approx 25,372$ Add the partial products.

Find the product of each equation using partial products.

A.
$$\begin{array}{r} 552 \\ \times 14 \\ \hline 7,728 \end{array}$$

B.
$$\begin{array}{r} 421 \\ \times 25 \\ \hline 10,525 \end{array}$$

C.
$$\begin{array}{r} 632 \\ \times 78 \\ \hline 49,376 \end{array}$$

D.
$$\begin{array}{r} 171 \\ \times 35 \\ \hline 5,985 \end{array}$$

E.
$$\begin{array}{r} 487 \\ \times 55 \\ \hline 26,785 \end{array}$$

F.
$$\begin{array}{r} 179 \\ \times 62 \\ \hline 11,098 \end{array}$$

Find the product of each equation using an algorithm.

A.
$$\begin{array}{r} 270 \\ \times 34 \\ \hline 9,180 \end{array}$$

B.
$$\begin{array}{r} 370 \\ \times 15 \\ \hline 5,550 \end{array}$$

C.
$$\begin{array}{r} 552 \\ \times 78 \\ \hline 43,056 \end{array}$$

D.
$$\begin{array}{r} 179 \\ \times 62 \\ \hline 11,098 \end{array}$$

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INDEPENDENT WORK

Student Practice Book, pp. 49–50

Lesson 5.7
Additional Practice

Name _____

Review
 You can use the standard algorithm to multiply 3-digit and 4-digit factors by a 2-digit factor.
 Find 358×42 using the standard algorithm for multiplication.

$$\begin{array}{r} 358 \\ \times 42 \\ \hline 7,160 \\ + 14,316 \\ \hline 15,076 \end{array}$$
 Multiply: 358×42
 Estimate: $358 \times 42 \approx 15,076$
 Check: $15,076 \approx 15,076$ Use partial products.

Find the product using the standard algorithm.

A.
$$\begin{array}{r} 420 \\ \times 27 \\ \hline 11,340 \end{array}$$

B.
$$\begin{array}{r} 504 \\ \times 31 \\ \hline 15,624 \end{array}$$

C.
$$\begin{array}{r} 430 \\ \times 80 \\ \hline 34,400 \end{array}$$

D.
$$\begin{array}{r} 677 \\ \times 16 \\ \hline 10,832 \end{array}$$

E.
$$\begin{array}{r} 318 \\ \times 36 \\ \hline 11,448 \end{array}$$

F.
$$\begin{array}{r} 781 \\ \times 21 \\ \hline 16,401 \end{array}$$

G.
$$\begin{array}{r} 485 \\ \times 24 \\ \hline 11,640 \end{array}$$

H.
$$\begin{array}{r} 375 \\ \times 33 \\ \hline 12,375 \end{array}$$

I.
$$\begin{array}{r} 349 \\ \times 31 \\ \hline 10,819 \end{array}$$

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Unit Review Name _____

Vocabulary Review

Choose the correct words to complete each sentence.

operation	exponential form
base	partial products
opponent	power of 10
estimate	round

- When multiplying, all that students get are **partial products** the factors and **partial products**. Then, you add the **partial products** to get the product answer.
- The **exponent** of a number system is equal to that tells you how many times the base is multiplied to that system.
- The **exponential form** of a number includes a base raised to a power called the **exponent**.
- To produce a solution, you can **round** the values used before performing operations.
- Any **power of 10** to perform is exponential to using 10 as the base and the number of times 10 is multiplied by that as the power or exponent.
- Any **estimate** is an approximate solution to a problem.
- Any **algorithm** is a set of steps used to solve a problem.

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Review

- What expression or value is equivalent to $10^3 \times 10^4$?
 - 1000
 - 10×4
 - $10 \times 10 \times 10 \times 10$
 - $10 \times 10 \times 10 \times 10$
- The apple manufacturer has 248 apples in every 8-day harvest month. How many apples does the manufacturer harvest each month? **Answers will vary.** Sample answer is given. There are about **31,000** apples in 123 harvests.
- Use the area model to find the area of the polygon. **Sample answer:** 344 square units.
- Complete the partial products to find 328×4 .

328	
$\times 4$	
1,200	$\rightarrow 10 \times 120$
800	$\rightarrow 10 \times 20$
80	$\rightarrow 10 \times 8$
1,200	$\rightarrow 4 \times 300$
80	$\rightarrow 4 \times 20$
32	$\rightarrow 4 \times 8$
128	$\rightarrow 4 \times 32$
- Scott read 248 pages each week. How many pages did he read in 123 weeks? **Sample answer:** 30,464. Use partial products or an algorithm to find the product of the different place values and add them to find the product. $242 \times 6 = 1,452$.
- Find the product using an algorithm.

125	$\times 21$	=	2,625
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Students can complete the **Unit Review** to prepare for the **Unit Assessment**. Students may complete the Review in their Interactive eBook in the Digital Student Center.

Vocabulary Review

Item Analysis

Item	Lesson
1	5-4
2	5-1
3	5-1
4	5-3
5	5-1
6	5-3
7	5-6

Review

Item Analysis

Item	DOK	Lesson	Standard
8	2	5-1	5.NBT.A.2
9	2	5-3	5.NBT.A.2
10	2	5-4	5.NBT.A.2
11	2	5-5	5.NBT.A.2
12	3	5-6	5.NBT.A.2
13	2	5-7	5.NBT.B.5

To review the lessons in this unit, have students watch the Math Replay video in their Digital Student Center.

Assign the Unit Review practice to students from the Digital Teacher Center.



Item Analysis (continued)

Item	DOK	Lesson	Standard
14	2	5-2	5.NBT.A.2
15	2	5-3	5.NBT.A.2
16	2	5-5	5.NBT.A.2
17	2	5-7	5.NBT.B.5
18	2	5-7	5.NBT.B.5
19	2	5-2	5.NBT.A.2

Performance Task

Standards: 5.NBT.A.2, 5.NBT.B.5

Rubric (6 points)

Part A (DOK 2) – 3 points

- 3 POINTS** Student's work reflects a proficiency with subtraction when using exponential forms of a number as a product.
- 2 POINTS** Student's work reflects a developing proficiency when using exponential forms of a number as a product. The error is a result of subtraction and not with writing an exponential form of a number as a product.
- 1 POINT** Student's work reflects a developing proficiency when using exponential forms of a number as a product. The error is a result of writing an exponential form of a number as a product.
- 0 POINTS** Student's work reflects a a poor understanding of using exponential forms of a number as a product.

Part B (DOK 2) – 3 points

- 3 POINTS** Student's work reflects a proficiency with multiplying multi-digit numbers with no errors.
- 2 POINTS** Student's work reflects a proficiency with multiplying multi-digit numbers. The error is a result of multiplying by less than 52 weeks in a year.
- 1 POINT** Student's work reflects developing proficiency with multiplying multi-digit numbers.
- 0 POINTS** Student's work reflects a poor understanding of multiplying multi-digit numbers.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

14. Which equation is equivalent to $10^2 \times 10^3 = 10^5$?

A. $1 \times 100 = 1 \times 10 \times 10 \times 10$

B. $1 \times 1,000 = 1 \times 10^2$

C. $10 \times 10 \times 10 \times 10 \times 10 = 100,000$

D. $10 \times 10^2 = 10 \times 10 \times 10$

E. $10 \times 10^2 = 100$

15. Which equation represents the only composite factor of 210?

A. $200 \div 20 = 10,000$

B. $200 \div 20 = 10,000$

C. $400 \div 20 = 10,000$

D. $400 \div 20 = 10,000$

16. Write the area model and use whole products to find 52×31 .

Area Model:

	50	2	
30	1,500	60	
2	60	62	
	1,560	62	
			1,622

$52 \times 31 = 1,622$

17. The rock band sells a combined average of 100 tickets per show. How many tickets might the band sell in 6 weeks? Estimate the number. How close is your estimate? $6,000$ tickets. $6,450$ tickets.

18. Complete the algorithm and find the product.

```

  621
x   62
-----
 1,242
+3,726
-----
 39,162
  
```

19. Write 10^4 as a product of 10. Then write the product 100×10^4 as $10 \times 10 \times 10 \times 10 \times 10 \times 10$.

$10^4 = 10 \times 10 \times 10 \times 10$

$100 \times 10^4 = 1,000,000$

Performance Task

Oliver is studying how much honey is produced by honey bees at two different locations. The bees at location A have 15 × 10 honey bees and produce about 101 ounces of honey each week. The bees at location B have 27 × 10³ honey bees and produce about 344 ounces of honey each week.

Part A What is the difference between the number of honey bees at each location?

$2,700 - 1,200 = 1,500$ honey bees

Part B What is the combined amount of honey produced each year?

$6,363 + 17,886 = 24,249$ oz.

Reflect

What are some different strategies you can use to multiply multi-digit numbers?

Answers may vary.

Unit 5
Fluency Practice

Name: _____

Fluency Strategy

You can choose a strategy to add. You can adjust the numbers and place value, or use an algorithm.

Model the numbers: $1,521 + 2,208$

$$\begin{array}{r} 1,521 \\ + 2,208 \\ \hline 3,729 \end{array}$$

$1,520 + 2,200 = 3,720$

6. Adjust the numbers to find the sum.

$$\begin{array}{r} 3,411 \\ + 1,887 \\ \hline 5,298 \end{array}$$

$3,400 + 1,900 = 5,300$

Fluency Flash

What is the sum?

1	0	9	7
+	2	4	8
+	3	0	5

8	2	7	9
+	3	5	8
+	5	0	4

Math • Multiply Multi-Digit Whole Numbers • 48

Fluency Check

What is the sum or difference?

A. $3,207 + 216 =$ 3,423	B. $418 + 267 =$ 685
C. $107 + 452 =$ 559	D. $54 + 103 =$ 157
E. $521 + 16 =$ 537	F. $817 + 525 =$ 1,342
G. $102 + 114 =$ 216	H. $818 + 84 =$ 902
I. $472 + 128 =$ 600	J. $1,019 + 258 =$ 1,277

Fluency Talk

How do you determine which strategy you want to use to add?
Explanations may vary.

Why might you want to multiply or subtract by adjusting using an algorithm?
Explanations may vary.

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Fluency practice helps students develop procedural fluency; that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students practice choosing a strategy to add fluently.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Performance Task

Movie Theaters

Students draw on their understanding of multiplying multi-digit numbers. Use the rubric shown to evaluate students' work.

Standards: 5.NBT.A.2, 5.NBT.B.5

Rubric (12 points)

Parts A and B (DOK 2) – 4 points

- 4 POINTS** Student's work reflects proficiency with multiplying multi-digit factors. Student was able to accurately calculate the answer.
- 2 POINTS** Student's work reflects developing proficiency with multiplying multi-digit factors. Minor error in calculation resulted in an inaccurate final answer.
- 0 POINTS** Student's work reflects a weak proficiency of multiplying multi-digit factors. Multiple errors in calculation resulted in an inaccurate final answer.

Part C (DOK 3) – 2 points

- 2 POINTS** Student's work reflects proficiency with determining which value is the greater of two values. The student justifies their selection with an accurate and reasonable explanation.
- 1 POINT** Student's work reflects a developing proficiency with determining which value is the greater of two values. The student's justification of their selection is lacking.
- 0 POINTS** Student's work reflects a weak proficiency in determining which value is the greater of two values. The student's justification of their selection is not present.

Part D (DOK 2) – 4 points

- 4 POINTS** Student's work reflects proficiency with multiplying multi-digit factors. Student was able to accurately calculate the answer. The student justifies their selection with an accurate and reasonable explanation.
- 2 POINTS** Student's work reflects developing proficiency with multiplying multi-digit factors. Minor error in calculation resulted in an inaccurate final answer. The student's justification of their selection is lacking.
- 0 POINTS** Student's work reflects a weak proficiency of multiplying multi-digit factors. Multiple errors in calculation resulted in an inaccurate final answer. The student's justification of their selection is not present.

Part E (DOK 3) – 2 points

- 2 POINTS** Student's work reflects proficiency with using reasoning in a real-world situation. The student justifies their selection with an accurate and reasonable explanation.
- 1 POINT** Student's work reflects a developing proficiency in using reasoning in a real-world situation. The student's justification of their selection is lacking.
- 0 POINTS** Student's work reflects a weak proficiency of using reasoning in a real-world situation. The student's justification of their selection is not present.

Unit 5
Performance Task

Name _____

Movie Theaters

A movie theater chain, Action Theaters, is comparing advertising standard seats with reclining seats in order to keep competitive with other theaters. The owner of Action Theaters just projected the costs associated with the theaters, as well as the potential gains to ticket sales.

Part A

Action Theaters currently has 21 theaters and each theater has 10 auditoriums. Each auditorium contains 100 seats (only the cost of a seat is listed). Assuming all auditoriums at all 21 theaters are full, how much money is made from ticket sales (do not show your work)?

Sample answer: $21 \times 10 = 210$ total auditoriums
 $210 \times 100 = 210 \times 10^2$ seats
 $210 \times 10^2 \times \$ = 1,880 \times 10^2 = \$188,000$

Part B

If Action Theaters decides they want to reclining seats in all 10 auditoriums in each of their 21 theaters, each auditorium will have 80 seats. Since the reclining seats have 40 more seats, each auditorium immediately loses 20 seats each. Because of the seating cost, the cost of a movie doesn't change by \$5. Assuming all auditoriums at all 21 theaters are full, how much money is made from ticket sales (do not show your work)?

Sample answer: $21 \times 10 = 210$ total auditoriums
 $210 \times 70 = 14,700$ seats
 $14,700 \times 10 = \$147,000$

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Part C

Assuming Action Theaters chooses to have a mixture of 10 auditoriums in each of its theaters and all seats are full, would it be better for the auditoriums to have standard or reclining seats?

Sample answer: It would be better for each auditorium to have standard seats because they would take in \$188,000 on ticket sales instead of \$147,000 with reclining seats.

Part D

It is possible that all seats aren't always full in the theater (usually in an auditorium with standard seats, 70 are full, and in an auditorium with reclining seats, 30 are full). Use the information to determine if it is better for the auditoriums to have standard or reclining seats. Show your work and explain.

Sample answer: $21 \times 10 = 210$ total auditoriums
 $210 \times 70 = 14,700$ seats
 $14,700 \times \$ = \$147,000$

$21 \times 10 = 210$ total auditoriums
 $210 \times 65 = 13,650$ seats
 $13,650 \times 10 = \$136,500$

Based on these new numbers, it is better to have reclining seats because you take in more money from ticket sales.

Part E

What other ways could the theater owner decide to use the concession stand to change their strategy and to be winning?

Sample answer: If there are less people in the theaters because of the reclining seats, the concession stand might not make as much money selling food.

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Unit Assessments

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

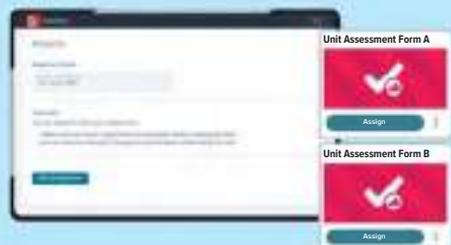
Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

Data When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support Intervention Lesson	Standard
1	2	5-1	Powers of 10 (Exponents)	5.NBT.A.2
2	2	5-1	Introduction to Powers of Ten	5.NBT.A.2
3	2	5-2	Multiply by Powers of 10	5.NBT.A.2
4	2	5-2	Multiply by Powers of 10	5.NBT.A.2
5	2	5-3	Estimate Products (Whole Number Factors)	5.NBT.B.5
6	3	5-3	Estimate Products (Whole Number Factors)	5.NBT.B.5
7	2	5-4	Multiply 2-Digit Numbers (Area Models)	5.NBT.B.5
8	2	5-5	Multiply 2-Digit Numbers (Area Models)	5.NBT.B.5
9	2	5-6	Multiply 3- by 1-Digit Numbers	5.NBT.B.5
10	2	5-7	Multiply Multi-Digit by 2-Digit Numbers	5.NBT.B.5
11	2	5-4	Multiply 2-Digit Numbers (Area Models)	5.NBT.B.5
12	3	5-4, 5-5, 5-7	Multiply 2-Digit Numbers (Area Models)	5.NBT.B.5
13	3	5-3, 5-6	Estimate Products (Whole Number Factors)	5.NBT.B.5
14	3	5-7	Multiply Multi-Digit by 2-Digit Numbers	5.NBT.B.5

Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 5:
Unit Assessment, Form A

Name: _____

1. Which is equivalent to 10^4 ? Choose all that apply.

A. 10,000
 B. $10 \times 10 \times 10 \times 10$
 C. $10 \times 10 \times 10 \times 10 \times 10$
 D. $10 \times 10 \times 10 \times 10 \times 10 \times 10$
 E. 10,000
 F. 100,000

2. A square has side length of 10. Which expressions show the area of the square? Choose all that apply.

A. 10×10
 B. $10 + 10 + 10 + 10$
 C. 10×10
 D. 100

3. Which is equivalent to 10×10^4 ?

A. 100
 B. 10,000
 C. 100,000
 D. 1,000,000

4. What expression best describes the equivalent of 10×10^2 ?

A. 10×100
 B. 10×100
 C. 100×100
 D. $100 \times 1,000$

5. Which is the most reasonable estimate for 29×30^2 ?

A. 20,000
 B. 20,000
 C. 200,000
 D. 200,000

6. A rectangular prism measures 600 feet long and 30 feet wide. About how much area does the end of the prism have?

Sample answer: $600 \times 30 = 18,000$ square feet

7. Which products show the area model?

$$\begin{array}{r} 100 \times 20 = 2,000 \\ 100 \times 30 = 3,000 \\ 100 \times 10 = 1,000 \\ \hline 2,000 + 3,000 + 1,000 = 6,000 \end{array}$$

A. $40 \times 700 = 28,000$
 B. $40 \times 720 = 28,800$
 C. $40 \times 700 = 28,000$
 D. $40 \times 700 = 28,000$

8. Which one shows how to calculate 20×100 using area models?

A.
$$\begin{array}{r} 10,000 \\ 900 \\ 900 \\ 3,000 \\ 340 \\ \hline 13,840 \end{array}$$

 B.
$$\begin{array}{r} 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ \hline 50 \end{array}$$

 C.
$$\begin{array}{r} 100 \\ 10 \\ 10 \\ 10 \\ 10 \\ \hline 130 \end{array}$$

9. Which products are correct? Choose all that apply.

A.
$$\begin{array}{r} 100 \\ 10 \\ \hline 110 \end{array}$$

 B.
$$\begin{array}{r} 100 \\ 10 \\ \hline 1,100 \end{array}$$

 C.
$$\begin{array}{r} 100 \\ 10 \\ \hline 110 \end{array}$$

 D.
$$\begin{array}{r} 100 \\ 10 \\ \hline 1,100 \end{array}$$

6. Answer Key

6. A rectangular prism measures 600 feet long and 30 feet wide. About how much area does the end of the prism have?

Sample answer: $600 \times 30 = 18,000$ square feet

7. Which products show the area model?

$$\begin{array}{r} 100 \times 20 = 2,000 \\ 100 \times 30 = 3,000 \\ 100 \times 10 = 1,000 \\ \hline 2,000 + 3,000 + 1,000 = 6,000 \end{array}$$

A. $40 \times 700 = 28,000$
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 C. $40 \times 700 = 28,000$
 D. $40 \times 700 = 28,000$

8. Which one shows how to calculate 20×100 using area models?

A.
$$\begin{array}{r} 10,000 \\ 900 \\ 900 \\ 3,000 \\ 340 \\ \hline 13,840 \end{array}$$

 B.
$$\begin{array}{r} 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ \hline 50 \end{array}$$

 C.
$$\begin{array}{r} 100 \\ 10 \\ 10 \\ 10 \\ 10 \\ \hline 130 \end{array}$$

9. Which products are correct? Choose all that apply.

A.
$$\begin{array}{r} 100 \\ 10 \\ \hline 110 \end{array}$$

 B.
$$\begin{array}{r} 100 \\ 10 \\ \hline 1,100 \end{array}$$

 C.
$$\begin{array}{r} 100 \\ 10 \\ \hline 110 \end{array}$$

 D.
$$\begin{array}{r} 100 \\ 10 \\ \hline 1,100 \end{array}$$

6. Answer Key

Unit 8
Unit Assessment, Form A, continued

Name _____

10. What is the product of an algorithm?

$$\begin{array}{r} 140 \\ \times 22 \\ \hline 280 \\ + 2800 \\ \hline 3080 \end{array}$$

11. A store owner charges \$2.17 for a set of 400 4-inch-by-6-inch notecards in an album. During the week, the store sold 28 boxes. How much money did the store collect?

- A. \$107
B. \$108
C. \$109
D. \$100

12. In 1998, a technology printing company of notecards sold 28 boxes of notecards each. How much did the company earn? Explain the strategy you used to find the answer.

4,704 square notecards. Sample answer: I used an area model to multiply, then I added the partial products.
 $4,000 + 200 + 400 + 24 = 4,704$.

Assessment Form A, Book 10

13. The average attendance at a town's high school football game is 3,627 people per game. How many people attended the home game? Explain your answer? Give an estimate and the exact number. Explain your strategy.

Sample answer: 26,000; 25,389 people; I rounded 3,627 to 4,000 and multiplied by 7 to get 28,000. I used an algorithm to multiply 7 times 3,627.

$$\begin{array}{r} 3,627 \\ \times 7 \\ \hline 25,389 \end{array}$$

14. A school has 2,705 seats. How many 28-person buses can fit in the seats? How many people can the school hold? Explain the strategy you used to find the answer.

80,765 people. Sample answer: I used an algorithm to multiply, first by multiplying 7 times 2,705 and then by multiplying 20 times 2,705.

$$\begin{array}{r} 2,705 \\ \times 28 \\ \hline 21,640 \\ + 54,100 \\ \hline 80,740 \end{array}$$

Assessment Form A, Book 10

Unit 8
Unit Assessment, Form B

Name _____

1. What is the product of 47,000 and 100?

- A. 4,700
B. 47,000
C. 4,700,000
D. 470,000
E. 470,000,000

2. A school owner charges \$2.17 for a set of 400 4-inch-by-6-inch notecards in an album.

- A. \$107
B. \$108
C. \$109
D. \$100

3. What is the product of 14 and 22?

- A. 280
B. 2800
C. 3080
D. 30800

4. What is the product of 400 and 2.17?

- A. 868
B. 8680
C. 86800
D. 868000

5. What is the total amount of money earned if you?

- A. \$107
B. \$108
C. \$109
D. \$100

Assessment Form B, Book 10

6. What is the product of 14 and 22? Explain your strategy.

$$\begin{array}{r} 14 \\ \times 22 \\ \hline 28 \\ + 280 \\ \hline 308 \end{array}$$

7. What is the product of 400 and 2.17? Explain your strategy.

$$\begin{array}{r} 400 \\ \times 2.17 \\ \hline 868 \\ + 8680 \\ \hline 8680 \end{array}$$

Assessment Form B, Book 10

- A. 868
B. 8680
C. 86800
D. 868000

8. A school owner charges \$2.17 for a set of 400 4-inch-by-6-inch notecards in an album. How much money did the store collect? Explain the strategy you used to find the answer.

4,704 square notecards. Sample answer: I used an area model to multiply, then I added the partial products: $4,000 + 200 + 400 + 24 = 4,704$.

Assessment Form B, Book 10

Assessment Form B, Book 10

9. What is the product of 14 and 22? Explain your strategy. Sample answer: I used an algorithm to multiply, first by multiplying 7 times 14 and then by multiplying 20 times 14.

$$\begin{array}{r} 14 \\ \times 22 \\ \hline 28 \\ + 280 \\ \hline 308 \end{array}$$

Assessment Form B, Book 10

UNIT 6 PLANNER

Multiply Decimals

PACING: 10 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener <i>Area and Decimal Multiplication</i> Explore area of rectangles on a grid to learn to place a decimal point in decimal multiplication.			
6-1 Patterns When Multiplying Decimals by Powers of 10	Students use patterns to multiply a decimal by a power of 10. Students explain patterns when multiplying a decimal by a power of 10.	Students explain how to use patterns to multiply a decimal by a power of 10 with the gerund <i>using</i> .	Students recognize and work to understand the emotions of others and practice empathetic responses.
6-2 Estimate Products of Decimals	Students estimate products of decimals. Students use estimated products to make predictions about a calculated solution. Students use estimated products to assess the reasonableness of a calculated solution.	Students discuss how to estimate products of two decimals using <i>by + gerund</i> .	Students engage in active listening and work collaboratively with a partner to complete mathematical tasks.
6-3 Represent Multiplication Involving Decimals	Students use decimal grids to represent and solve multiplication equations involving decimals.	Students discuss how to solve multiplication equations using decimal grids while answering <i>Wh-</i> and Yes/No questions.	Students identify personal traits that make them good students, peers, and math learners.
Math Probe <i>Decimal Multiplication</i> Estimate products of decimal numbers.			
6-4 Use an Area Model to Multiply Decimals	Students use an area model to determine partial products and add partial products to calculate the product of two decimals.	Students discuss using area models to solve multiplication problems while answering <i>Wh-</i> and Yes/No questions and using the term <i>decompose</i> .	Students discuss and practice strategies for managing stressful situations.
6-5 Generalizations about Multiplying Decimals	Students use patterns based on place value concepts and properties of operations to determine the placement of the digits in a product.	Students explain how to use patterns in calculations to multiply decimals by making generalizations.	Students reflect on and describe the logic and reasoning used to make a mathematical decision or conclusion.
6-6 Explain Strategies to Multiply Decimals	Students can explain their reasoning for using different strategies to solve. Students explain different strategies to multiply decimals.	Students explain their reasoning for using particular strategies to multiply decimals while answering <i>Wh-</i> questions.	Students discuss the value of hearing different viewpoints and approaches to problem solving.
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION:
What strategies can I use to multiply decimals?

LESSON	KEY VOCABULARY	MATERIALS TO GATHER	RIGOR FOCUS	STANDARD
6-1	<u>Math Terms</u>	<ul style="list-style-type: none"> calculator number cubes: 1 whole number cube, 1 decimal cube place-value charts 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.A.2
	exponent factor product			
6-2	<u>estimate</u> <u>range</u> round	<ul style="list-style-type: none"> <i>Blank Open Number Lines</i> number cubes 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.7
	cite speculate			
6-3	decimal grid partition	<ul style="list-style-type: none"> <i>Blank Open Number Lines Teaching Resource</i> <i>10 × 10 Grids Teaching Resource</i> number cubes 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.7
6-4	area area model decompose partial product	<ul style="list-style-type: none"> base-ten blocks 0.5 cm grid paper 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.7
	complement evaluate			
6-5	area model digit partial product	<ul style="list-style-type: none"> place-value charts 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.7
6-6	area model decimal grid decomposition partial product unknown	<ul style="list-style-type: none"> decimal grids <i>Show and Explain Your Reasoning Teaching Resource</i> 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.7
	relevant suggest			

Focus

Multiplying Decimals

In this unit, students extend on their understanding from Grade 4 of multiplying whole numbers and fractions to multiplying decimals. They use estimation to determine the reasonableness of their answers. Students apply their understanding of multiplying decimals to solve problems in real-world contexts.

Students apply their knowledge of decimal fractions, place value, and the properties of operations to multiply decimals. Later in the unit, students revisit and make use of the pattern they discovered to make a generalization about the placement of the decimal in the product.

Students discover that place value and multiplication strategies work the same way with decimal operations as they do with whole number operations.

- Students can extend their understanding based on these explorations with decimal grids to generalize their methods and understanding. They move to the generalized area model, which serves as a template for their thinking and use of the Distributive Property and partial products. For example, consider 0.25×73 .
- Students can decompose the factors by place value and set up the following area representation of the product. Now, if students explore further by finding the products 25×73 , 2.5×73 , 2.5×7.3 , and 0.25×7.3 , they can see that the number of decimal places in the product equals the total decimal places in the factors.

Coherence

What Students Have Learned

- Students used partial products to multiply multi-digit numbers. (Grade 4)
- Students used place value to round decimals. (Grade 5, Unit 3)
- Students identified patterns based on the placement of the decimal point when a decimal was multiplied by a power of 10. (Grade 5, Unit 5)
- Students multiplied multi-digit whole numbers. (Grade 5, Unit 5)
- Students estimated decimal products to determine if calculations were reasonable. (Grade 5, Unit 5)

What Students Are Learning

- Students use strategies based on place value to multiply decimals by powers of 10.
- Students estimate products of decimals to determine reasonable solutions.
- Students represent multiplication with decimals using decimal grids.
- Students use multiplication strategies to multiply decimals to hundredths.

What Students Will Learn

- Students estimate quotients of decimals. (Grade 5, Unit 8)
- Students use strategies to divide with decimals. (Grade 5, Unit 8)
- Students fluently multiply multi-digit decimals using the standard algorithm. (Grade 6)

Rigor

Conceptual Understanding

- Students develop understanding of multiplying decimals by powers of 10.
- Students build on their understanding of partial products and area models to multiply decimals.
- Students extend their understanding of place value to determine the product of two decimal factors.

Procedural Skill and Fluency

- Students develop proficiency in multiplying decimals to hundredths by powers of 10.
- Students use strategies used for multiplying whole numbers to build proficiency with multiplying decimals.
- Students increase proficiency with multiplying decimals by making generalizations about the product of decimal factors.

Application

- Students apply estimated products to successfully solve contextual, real-world problems.
- Students apply their understanding of multiplying using decimals to solve problems with real-world contexts.

Application is not a targeted element of rigor for the standards in this unit.

Effective Teaching Practices

Facilitate Meaningful Mathematical Discourse

In the mathematics classroom, student discourse is an interactive process of collaborative exploration, exchange of ideas, argumentation, and building of shared understanding. It is engaging, commands participation, and promotes deep learning. It is a tool the teacher uses to both ensure and confirm that learning is taking place.

Discourse can be verbal or written and enhanced through visuals. It takes place in a variety of settings and calls for student-student and student-teacher interaction. Student-student discourse allows students to take responsibility for their own learning and the learning of their peers. The student-teacher dynamic has the teacher playing more of a supporting role, making sure that the process follows a productive path. Classroom discourse can also be used to enrich the classroom experience for English language learners.

Each lesson in this program calls for discourse using the think-pair-share model and whole-class discussion. The teacher is a facilitator and performs the following actions—

- Engages students as they explore and share ideas and strategies with each other.
- Observes and gathers information about what students are doing and saying.
- Makes sure the discourse stays relevant to the lesson's goals and progresses toward a meaningful conclusion.

The student is a leader, partner, problem solver, and communicator, and performs the following actions—

- Presents and explains ideas, strategies, representations, and reasoning to peers.
- Seeks to understand the strategies, representations, and approaches of peers.

Math Practices and Processes

Attend to Precision

Attending to precision refers to any action or habit of being accurate, clear, and on point. For example, when students attend to precision, they use care in computations and check their answers, pay attention to units while reasoning about problems, use the clearest possible language to explain ideas, and label representations accurately to connect them to the quantities and relationships in problems. Teachers help students develop the habit of attending to precision by being accurate themselves in their discussions and by requiring it of them in all discourse and classroom activity.

To help students develop the habit of attending to precision, assign tasks that require precision and set clear expectations.

For example:

- Have students talk about their representations with area models and decimal grids.
- Have students discuss how they estimate products, how they know their estimates are reasonable, and how far away a reasonable answer could be from an estimate.
- Have students explain the thought process they use to label their area representations.
- Pay attention to whether and how students attend to the units in the problems they solve and ask them questions that lead to thinking about units.
- Have students describe the pattern they discovered in the position of the decimal point in products.

Social and Emotional Learning

What Skills Will We Develop?

- **Social Awareness – Empathy** (Lesson 6-1): Students who can empathize with others are more able to build positive relationships.
- **Relationship Skills – Build Relationships** (Lesson 6-2): Building positive relationships can help establish a strong classroom community.
- **Self-Awareness – Self-Confidence** (Lesson 6-3): Self-confident students are more willing to take risks, allowing them to learn from mistakes.
- **Self-Management – Manage Stress** (Lesson 6-4): Students who can regulate their stress are resilient and better prepared for academic success.
- **Responsible Decision-Making – Evaluate** (Lesson 6-5): When students evaluate their own logic and reasoning, they can develop understanding that helps them make informed decisions.
- **Social Awareness – Appreciate Diversity** (Lesson 6-6): When students appreciate diversity, they create a stronger, more inclusive classroom community.

Unit Overview

Language of Math

Vocabulary

Students will be using these key terms in this unit.

- **Estimate** – (Lesson 6-2): Students were introduced to this term in the context of solving word problems involving all four operations. Have students discuss how estimation can help them evaluate the reasonableness of a solution.
- **Exponent** – (Lesson 6-1): Students are familiar with this term from their work with place value and expanded form. They know it as a raised number placed next to 10 to tell the number of factors of 10 needed to make products of 100, 1000, and so on. Students use the exponent to determine the number of zeros in those products.

- **Partial products** – (Lesson 6-4): Students were introduced to this term in the context of multiplication in Grade 4. They learned *partial* products as the terms they generate using the Distributive Property.
- **Range*** – (Lesson 6-2): Students are introduced to this term in the context of a range of numbers used for factor pairs. A range gives two numbers between which acceptable values fall.

*This is a new term.

Math Language Development

A Focus on Reading

In many respects, reading in math is the same as reading in any academic discipline. In some ways, reading in math is different and requires different or additional strategies.

Consider these unique characteristics of mathematics text.

- Math text is conceptually dense. A single sentence or equation might communicate multiple layers of interdependent content.
- Math text looks different. It includes prose, equations, graphs, tables, symbols, and other means for communicating ideas.
- Math ideas in instructional texts are developed differently. They are developed in a logical progression with the conclusion at the end.
- Math is a language that uses many words common to everyday texts but with different meanings.
- Math requires students to interpret real-world contexts using abstract methods.

The teacher plays a supportive role. Instruction should give attention to the strategies that students can use to read the language more effectively. As a facilitator, interact with students before, while, and after they read.

Before reading—

- If the passage or problem has a title or other telling features, ask students to use them to predict what the content is about.
- Have students tell whether the passage or problem looks like anything they have encountered before.

While reading—

- Have students restate the content in their own words.
- Have students notice the ways that new ideas are built on familiar ones.

After reading—

- Check with students that the problem or passage makes sense to them.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to multiplying decimals. Because many of the words (using, cost, efficient), phrases (similar to), and structures (by + -ing verbs, if...[then]...) used in this unit could prove challenging to ELs, they are supported in understanding and using them so that the instruction is more accessible.

Lesson 6-1 – *using to express how*

Lesson 6-2 – *by + -ing verbs to answer how questions*

Lesson 6-3 – *costs*

Lesson 6-4 – *similar to*

Lesson 6-5 – *if...[then]...*

Lesson 6-6 – *efficient*

Unit Routines

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

What's Another Way to Write It?

Purpose: Build flexibility with number sense and mental math operations.

Overview: Given a number, students generate and share expressions using operations that, when evaluated, have the same value as the number. Students then look for relationships amongst the expressions.

About How Much?

Purpose: Build estimating skills.

Overview: Students estimate the value of expressions (with operations) shown, explaining their strategies and thinking. The teacher records students' estimates, then reveals the value of the expression. Students analyze the estimates and discuss which are closest to the actual value of the expression.

Find the Missing Values

Purpose: Build identification of patterns and efficiency with solving equations while examining a list of related equations.

Overview: Students analyze a series of equations to look for patterns that they can use to determine the missing values in the equations. As students share their analyses and solutions, the teacher can reveal the missing values.

Where Does It Go?

Purpose: Build estimating skills using benchmarks.

Overview: Students place a target number on number lines with different endpoints and justify their placement. In some instances, as a challenge, the target number may not actually belong on one of the number lines.

Sense-Making Routines

- **Notice & Wonder: What do you notice? What do you wonder?** (Lesson 6-1) In this lesson, students are presented with two sets of equations to think about multiplication and the patterns it creates.
- **Notice & Wonder: How are they the same? How are they different?** (Lesson 6-3) Students compare two dozen eggs to see how they are alike and how they are different.
- **Which Doesn't Belong?** (Lesson 6-4) Students explore the relationships between numbers with common digits but different place values to determine which value has the digits in a different order.
- **Is It Always True?** (Lesson 6-5) Students are provided with a scenario where they have to consider what happens to a product when a factor is multiplied by a power of ten.
- **Numberless Word Problem** (Lessons 6-2 and 6-6) Students are presented with a problem where they need to multiply decimals, but they are not given any numbers. They have to think through what information they would need and how they would solve the problem.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. For more information on the Math Language Routines, see the Appendix.

- Lesson 6-1 – Students participate in MLR2: Collect and Display and MLR1: Stronger and Clearer Each Time.
- Lesson 6-2 – Students participate in MLR5: Co-Craft Questions and Problems.
- Lesson 6-3 – Students participate in MLR8: Discussion Supports and MLR6: Three Reads.
- Lesson 6-4 – Students participate in MLR7: Compare and Connect.
- Lesson 6-5 – Students participate in MLR8: Discussion Supports and MLR7: Compare and Connect.
- Lesson 6-6 – Students participate in MLR1: Stronger and Clearer Each Time.

1200 6
How Ready Am I?

Name: _____

1. The height of a person is 228 inches. What is the measurement rounded to the nearest whole number of feet?

A. 3 inches B. 3 meters
C. 2 meters D. 3 inches

2. What is 10 to the power of 5?

A. 20,000 B. 10,000
C. 1,000 D. 10

3. What is the value of 8¹⁰?

A. 80,000 B. 8,000
C. 1,000 D. 30

4. What is 1000 to the power of 2?

A. 2,000 B. 1,000,000
C. 1,000 D. 10,000

5. What is 25 to the power of 2?

A. 50 B. 500
C. 1,000 D. 1,400

6. Jerome makes 175 newspapers in each of 8 days every morning. What is the total number of newspapers Jerome makes every morning?

A. 1,375 newspapers
B. 1,280 newspapers
C. 1,400 newspapers
D. 1,512 newspapers

7. Which number is equivalent to 47×10^2 ?

A. 47 + 10 B. 47 + 1,000
C. 470 + 10 D. 470 + 1,000

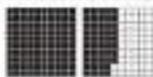
Answer Key: 44

8. What number is represented by the shaded grid?



A. 600
B. 60
C. 0.60
D. 6000

9. What number is represented by the shaded grid?



A. 0.149
B. 149
C. 1.49
D. 14.9

10. What is $300 + 20 + 30$ rounded to the nearest hundred?

A. $40 + 20 + 30 = 90$
B. $300 + 200 + 20 = 520$
C. $3,000 + 200 + 300 = 3,500$
D. $3,000 + 3,000 + 300 = 6,300$

Answer Key: 44

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

Use Guided Support intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill		Guided Support Intervention Lesson	Standard
1	2	Round to nearest whole number	Round Decimals to Nearest Whole > 1	5.NBT.A.4
2	2	Multiply by power of 10	Introduction to Powers of Ten	5.NBT.A.2
3	2	Powers of 10	Powers of 10 (Exponents)	5.NBT.A.2
4	2	Multiply 4-digit by 1-digit whole numbers	Multiply 4- by 1-Digit Numbers	4.NBT.B.5
5	2	Multiply 2-digit by 2-digit whole numbers	Partial Products (2- by 2-Digit Numbers)	4.NBT.B.5
6	2	Multiply 3-digit number by 1-digit number	Multiply 3- by 1-Digit Numbers	4.NBT.B.5
7	2	Multiplication as partial products	Multiply 2- by 1-Digit Numbers	4.NBT.B.5
8	1	Identify decimal number from decimal grid	Standard & Word Form (Large Numbers)	5.NBT.A.3
9	1	Identify decimal number from decimal grid	Standard & Word Form (Large Numbers)	5.NBT.A.3
10	2	Multiplication as partial products	Partial Products (2- by 2-Digit Numbers)	4.NBT.B.5

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.



Unit Opener

Focus Question

Introduce the Focus Question: *What strategies can I use to multiply decimals?* Ask students to think about what they know about multiplication.

- What strategies did you use to multiply whole numbers?
- How do you think multiplying decimals will be different?

Remind students that at the end of the unit, they will reflect back on what they learned in this unit.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

STEM in Action

Videos

Students can watch the two STEM videos.

STEM Career: Geologist Maya talks about her aspirations to be a geologist.

Maya Finds the Weight of Boulders Maya talks about how to find the weight of several boulders.

STEM Project Card

Students can complete the STEM Project Card during their workstation time.

STEM Adventure

Students can complete the STEM Adventure during their workstation time.

Unit 6

Multiply Decimals

Focus Question
What strategies can I use to multiply decimals?

Hi, I'm Maya.
I want to be a geologist. The geologist weighs boulders. Each boulder weighs 2.5 tons, so I will need to multiply whole numbers to find how much they weigh. I'll use the strategies I know to multiply decimals to become a geologist.

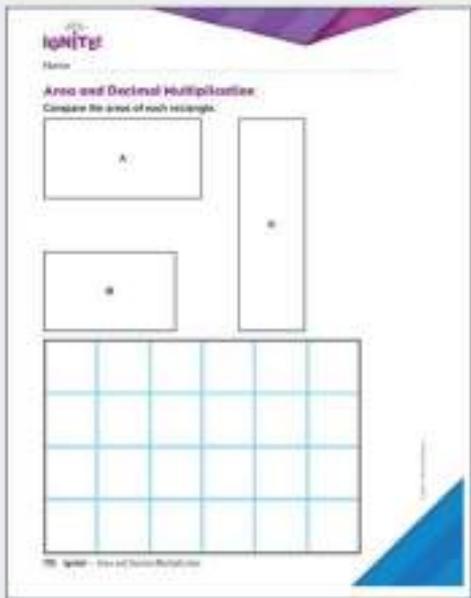
STEM | GO ONLINE

STEM Career: Geologist

GO ONLINE

Maya Finds the Weight of Boulders

GO ONLINE



Ignite!

Area and Decimal Multiplication

Students apply their knowledge of area as they explore preliminary work with decimal multiplication and the intuitive placing of the decimal point in a product.

Materials: scissors, plain paper per student

- Have students work in pairs to observe Rectangles A, B, and C.
 - Which rectangle do you think has the greatest area? Why?
 - Which rectangle do you think has the least area? Why?
- Have students trace Rectangles A, B, and C onto their own paper. Then have students cut the copied rectangles and trace them onto the grid.
 - Each square on the grid paper has an area of 1 square unit. Use the grid paper to help you find out the area of each rectangle.
- Select a few students to explain how they found the area of each rectangle. Make sure the class agrees on the area of each rectangle.
 - How did your original guesses compare with the areas that you found?
- What are the dimensions of Rectangle A, using decimals?
 - To find 1.5×3 , think: How much is 3, and half of 3 more?
 - How does that result compare to the area of Rectangle A that you traced on the grid paper?
- Mention that if we were to multiply the dimensions of Rectangle A without regard to the decimal point, we would obtain $15 \times 3 = 45$.
 - Where would the decimal point need to go in 45 so that it matches the area of Rectangle A?
 - So, what is the product 1.5×3 ?
- Repeat Steps 4 and 5 for Rectangles B and C.

For Rectangle B, students observe that the product of the dimensions without regard to the decimal points is $15 \times 25 = 375$. Based on the area of Rectangle B, students should conclude that to find the product 1.5×2.5 , they should place the decimal point between the 3 and the 7 to produce 3.75. So, $1.5 \times 2.5 = 3.75$.

For Rectangle C, students observe that the product of the dimensions without regard to the decimal point is $125 \times 4 = 500$. Based on the area of Rectangle C, students should conclude that to find the product 1.25×4 , they should place the decimal point between the 5 and the 0 to produce 5.00, or 5. So, $1.25 \times 4 = 5.00$, or 5.

Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson
Game Station	Game Station	Students build proficiency with multiplying decimals.	
		<ul style="list-style-type: none"> • Multiply by Powers of 10 Showdown 6-1 • Estimating Decimal Products Bingo 6-2 • Decimal Multiplication Task Cards 6-3 • Decimal Multiplication Tic Tac Toe 6-4 • Related Decimal Multiplication Task Cards 6-5 • Related Decimal Multiplication Task Cards 6-6 	
	Digital Game	Mad Lab Mix-Up Students multiply multi-digit numbers.	6-1
			
	Have students complete at least one of the Use It! activities for this unit.		
Application Station	STEM Project Card	Rock Garden Students use metric measurements to 6-6 create a model of a rock garden.	
			
	Connection Card	School Spirit Students use area and multiplication to 6-4 create a school wall mural.	
			
Real World Card	Move to the Left. Now Right! Students create a maze and write step-by-step directions for getting through it.	6-3	
			

Additional Resources

Use the resources below to provide additional support for this unit.



Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the new terms on the front side of the card.



Foldables

Use the unit foldables with Lessons 6-3 and 6-4.



Spiral Review

Students can complete the Spiral Review at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
6-1	5.MD.C.4
6-2	5.NBT.B.5
6-3	5.NBT.A.2
6-4	5.MD.C.3
6-5	5.NBT.A.1
6-6	5.NBT.B.7

Patterns When Multiplying Decimals by Powers of 10

Learning Targets

- I can use patterns to multiply a decimal by a power of 10.
- I can explain patterns when multiplying a decimal by a power of 10.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.A** Understand the place value system.
- ◆ **5.NBT.A.2** Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

Math Practices and Processes

MPP Attend to precision.

MPP Look for and make use of structure.

Vocabulary

Math Terms

exponent
factor
product

Academic Terms

analyze
reflect

Materials

The materials may be for any part of the lesson.

- calculator
- number cubes: 1 whole number cube, 1 decimal cube
- place-value charts

Focus

Content Objectives

- Students use patterns to multiply a decimal by a power of 10.
- Students explain patterns when multiplying a decimal by a power of 10.

Language Objectives

- Students explain how to use patterns to multiply a decimal by a power of 10 with the gerund *using*.
- To support maximizing linguistic and cognitive meta-awareness and optimizing output, ELs participate in MLR2: Collect and Display and MLR1: Stronger and Clearer Each time.

SEL Objective

- Students recognize and work to understand the emotions of others and practice empathetic responses.

Coherence

Previous

- Students determined that a digit in one place represents ten times what it represents in the place to its right (Grade 4).
- Students multiplied multi-digit whole numbers (Unit 5).

Now

- Students use their knowledge to create strategies based on place value to multiply decimals by powers of 10.

Next

- Students will estimate products of decimals to assess calculated solutions (Lesson 2).
- Students will write and evaluate numerical expressions involving whole-number exponents (Grade 6).

Rigor

Conceptual Understanding

- Students understand multiplying decimals by powers of 10 using strategies based on place value, properties of operations, and patterns in the powers of 10.

Procedural Skill & Fluency

- Students develop proficiency in multiplying decimals to hundredths by powers of 10.

Application

- Students apply their understanding to solve contextual problems.

Application is not a targeted element of rigor for this standard.

Number Routine

What's Another Way to Write It?



5–7 min

Build Fluency Students build number sense as they write three different expressions equivalent to 13.75.

Remind students that there will be many different possible answers to the problem. As solutions are given, record them for students to evaluate and compare.

These prompts encourage students to talk about their reasoning:

- Which of the expressions that you wrote are related? Why?
- Explain how you can use one expression to create a new expression.
- Do you notice any patterns? Explain.

Purpose Students notice patterns of zeros when multiplying whole numbers by powers of 10 and consider whether that pattern extends to decimals.

Notice & Wonder

- What do you notice? What do you wonder?

Teaching Tip You may want to have students work in pairs as they notice and wonder. This can help build a productive question and ponder environment that fosters further points of notice and questions for exploration as they collaborate ideas.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of how to use patterns to multiply decimals by powers of 10 and are based on possible comments and questions students that may make during the share out.

- Do you think any patterns you noticed work for decimal numbers?
- How do think the patterns might work for decimal numbers?

Math is... Mindset

- How can working with your peers help when solving problems?

Social Awareness: Empathy

As students work through the Notice & Wonder routine, invite them to collaborate with peers to think about multiplication patterns. Encourage students to share ideas and work together to identify the problem, choose an appropriate model or strategy, and execute the steps necessary to solve the problem.

Transition to Explore & Develop

Have students think about multiplication patterns involving the relationship between the zeros and the powers of 10 as they consider the equations. Guide them toward discussing the effects on place value in the products.

Establish Mathematics Goals to Focus Learning

- Let's think about how to use patterns to multiply decimals by powers of 10.



Lesson 6-1
Patterns When Multiplying
Decimals by Powers of 10

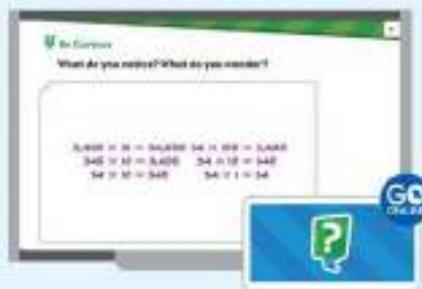
Be Curious
What do you notice? What do you wonder?

$$3,400 \times 10 = 34,000 \quad 34 \times 100 = 3,400$$

$$340 \times 10 = 3,400 \quad 34 \times 10 = 340$$

$$34 \times 10 = 340 \quad 34 \times 1 = 34$$

How can you show this relationship with a concrete model?



Be Curious
What do you notice? What do you wonder?

$$3,400 \times 10 = 34,000 \quad 34 \times 100 = 3,400$$

$$340 \times 10 = 3,400 \quad 34 \times 10 = 340$$

$$34 \times 10 = 340 \quad 34 \times 1 = 34$$

GO ON!

Activity-Based Exploration

Students explore place-value patterns when multiplying by powers of 10 and use their patterns to multiply decimals by powers of 10.

Materials: calculator

Directions: Students enter any decimal number on the calculator (e.g. 1.45), then multiply their decimal by 10. Have them predict the product before they press the equal key. Students continue to multiply by 10 mentally, challenging themselves to predict the product before they press the equal key.

Implement Tasks That Promote Reasoning and Problem Solving

- How did you use mental math to predict the product?
- What happens to the digits each time the number is multiplied by 10?
- What are some ways to record your work to look for patterns?
- How could you summarize the results to predict how multiplying a decimal by a power of 10 affects the decimal value?

Math is... Structure

- How are multiplying decimals and whole numbers by 10 similar?

Students use patterns to connect what happens when whole numbers are multiplied by a power of 10 to what happens when decimals are multiplied by a power of 10.

Activity Debrief: Have students share their findings when repeatedly multiplying by 10. Encourage students to write their multiplication expressions by writing the powers of 10 in exponential form. Discuss the relationship between the exponent and the number of places the digits shifted.

Have students revisit the Pose the Problem question and discuss answers.

- How can you determine the value of these expressions?

English Learner Scaffolds

Entering/Emerging Support students in understanding how the gerund *using* signals how to do something. Using manipulatives, say *I can show how to [name a task] using [your manipulatives]*. Demonstrate. Repeat the task twice, once using a correct object to show how to do something, and once using an incorrect object. Ask, *Can I show how to [name task] using this?*

Developing/Expanding Support students in understanding how the gerund *using* signals how to do something. Using manipulatives, say *I can show how to [name a task] using [your manipulatives]*. Demonstrate. Repeat the task twice, once using a correct object to show how to do something, and once using an incorrect object. Ask, *Can I show how to [name task] using this?* Then ask students to make their own sentence with *using*. Provide sentence frames for students who need extra guidance.

Bridging/Reaching Instruct students to use the gerund *using* in their response to the Math Is...Structure question on the Learn page. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding, and explaining why something may be incorrect. For example, *No, that's wrong because.... or No, that's incorrect because....*

Guided Exploration

Students write out the factors of 10 to multiply a decimal by a power of 10 to explore and recognize patterns.

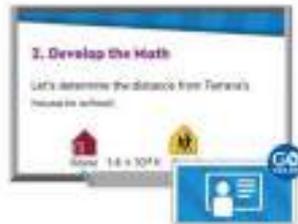
Facilitate Meaningful Mathematical Discourse

- Have the students find the product of 1.4 and 10. Ask:
 - How can you use decimal grids, equal groups, or place value to find the product?
- Have the students find the product of 14 and 10^4 . Ask:
 - How can you use the patterns you have seen to find the product?
- **Think About It:** Can you think of additional ways to write 1.4×10^4 ?
- Have the students justify the ways of writing 2.4×10^3 . Ask:
 - What is the exponent? How do you know?
 - How many zeros will there be? How do you know?
 - What happens to the digits in 24 ?

Math is... Structure

- How are multiplying decimals and whole numbers by 10 similar?

Students use patterns to connect what happens when whole numbers are multiplied by a power of 10 to what happens when decimals are multiplied by a power of 10.



On My Own

Name _____

Write the multiplicative expression using factors of 10. Then, find the value.

1. 3.4×10^2 3. 22×10^3
 $3.4 \times 10 = 34, 34 \times 10 = 340$ $2.2 \times 10 = 22, 22 \times 10 = 220$

2. 1.8×10^3 4. 19×10^2
 $1.8 \times 10 = 18, 18 \times 10 = 180$ $1.9 \times 10 = 19, 19 \times 10 = 190$

3. **Anchor** Write the value to the left of the decimal. The ones digit is 10⁰ because it is the greatest. How many times does it fit in 100?
 $1.2 \times 10^2 = 1.2 \times 100 = 120$ (20)

4. **Anchor** Write the value to the left of the decimal. The ones digit is 10⁰ because it is the greatest. How many times does it fit in 1000?
Sample answer: Juan: $4.7 \times 10^2 = 4.7 \times 100 = 470$
 Mary: $9.3 \times 10^2 = 9.3 \times 100 = 930$; Juan walks farther.

5. **Anchor** Write the value to the left of the decimal. The ones digit is 10⁰ because it is the greatest. How many times does it fit in 1000?
Sample answer: Sasha: $3.5 \times 10^4 = 3.5 \times 10,000 = 35,000$
 $3.2 \times 10^4 = 3.2 \times 10,000 = 32,000$
 $2.8 \times 10^4 = 2.8 \times 10,000 = 28,000$
Sample answer: Sasha added zeros using the exponent, rather than shifting five digits based on the exponent. So, $3.5 \times 10^4 = 35,000$.

Math 6 • Multiplicands 10

8. **STEM Connection** A geologist measures the width of the gully at the water point. How can the geologist estimate the width of the gully?
Sample answer: multiply the width by five power of 10.
 $3.4 \times 10^2 = 340$ feet



9. What is the product? Use patterns to help you solve.

9. $3.4 \times 10^2 = 340$ 10. $1.2 \times 10^2 = 120$
 $3.4 \times 10^3 = 3,400$ $1.2 \times 10^3 = 1,200$
 $3.4 \times 10^4 = 34,000$ $1.2 \times 10^4 = 12,000$

11. $0.8 \times 10^2 = 80$ 12. $0.7 \times 10^2 = 70$
 $0.8 \times 10^3 = 800$ $0.7 \times 10^3 = 700$
 $0.8 \times 10^4 = 8,000$ $0.7 \times 10^4 = 7,000$

13. **Visual Thinking** How are these two expressions related?
 30.2×10^2 3.02×10^3
Sample answer: Both expressions are equal to 3,020. The exponents differ by 1 and so does the number of digits to the left of the decimal point.

Reflect

How can you estimate what it means to multiply a decimal by a power of 10?
Answers may vary.

Math is... Connected

How are you doing your standards? How often are you?

14. **Anchor** Write the value to the left of the decimal. The ones digit is 10⁰ because it is the greatest. How many times does it fit in 1000?
Sample answer: Juan: $4.7 \times 10^2 = 4.7 \times 100 = 470$
 Mary: $9.3 \times 10^2 = 9.3 \times 100 = 930$; Juan walks farther.

Math 6 • Multiplicands 10

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 1–4 Students may confuse the notation for multiplication with factors of 10 with the normal order of operations. Watch for students first multiplying the value by 10, and then raising the result to the given power. You may want to remind students that the exponent is only applied to the 10, and not the entire expression.

Item Analysis

Item	DOK	Rigor
1–4	1	Procedural Skill and Fluency
5–8	2	Application
9–12	1	Procedural Skill and Fluency
13	4	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you explain what it means to multiply a decimal by a power of 10?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did working with your peers help when solving problems?

Students reflect on how they practiced social awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use patterns to multiply a decimal by a power of 10.
- I can explain patterns when multiplying a decimal by a power of 10.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Multiplying decimals by powers of 10	5.NBT.A.2
2	2	Multiplying decimals by powers of 10	5.NBT.A.2
3	2	Multiplying decimals by powers of 10	5.NBT.A.2
4	2	Multiplying decimals by powers of 10	5.NBT.A.2

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 4 Then have students do

4 of 4 Additional Practice or any of the **U** or **E** activities

3 of 4 *Take Another Look* or any of the **U** activities

2 or fewer of 4 Small Group Intervention or any of the **U** activities

Key for Differentiation

U Reinforce Understanding

U Build Proficiency

E Extend Thinking



Lesson 6-1
Exit Ticket

Name: _____

- Which of these are equivalent to 11×10^3 ? Choose all that apply.
 - A. $11 \times 10^3 \times 3$
 - B. $11 \times 10^3 \times 10^3$
 - C. 1100
 - D. 10,000
- What is the value of 3.4×10^2 ? Write the multiplication using powers of 10.

$3.4 \times 10^2 = 10 \times 10 \times 34 = 3400$
- Knowing that $0.5 \times 10^4 = 500$, what is 5×10^4 ?
 - A. 500
 - B. 5,000
 - C. 50,000
 - D. 500,000
- According to the 2010 Census, June has walked 1.1 million steps at the end of each hour every day of April each during the year.
 - A. 63 steps
 - B. 630 steps
 - C. 6,300 steps
 - D. 63,000 steps

Reflect On Your Learning

On _____ The exit _____ I understand _____ I can work _____

Lesson 6-1 Exit Ticket 61

R Reinforce Understanding

SMALL GROUP

Multiply with Decimals!

Work with students in small groups. Provide each group with a decimal number cube labeled with tenths and a whole number cube. The number rolled on the whole number cube will represent the power of 10. A student rolls both number cubes. All students multiply the two numbers (such as 0.2×10). If necessary, help students write the expression without the exponents to see the pattern. Have students repeat the steps until each one has had a turn to roll the cubes.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Multiply by Powers of 10 Showdown
Students practice multiplication of decimals.

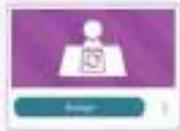


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Multiply by Powers of 10 (Decimal Point)



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 51

Lesson 81 • Reinforce Understanding
Patterns When Multiplying Decimals by Powers of 10

Review
You can take patterns when multiplying decimal by powers of 10.
 $7.3 \times 10^1 = 73$
 $\rightarrow (7.3 \times 10) \times 10 = 73 \times 10 = 730$
 $\rightarrow (7.3 \times 10) \times 10 \times 10 = 73 \times 10 \times 10 = 7,300$

Write the multiplication using factors of 10. Then find the value.

5. $5.7 \times 10^2 =$ 57,000	8. $3.4 \times 10^3 =$ 34,000
$3.7 \times 10 \times 10 = 10 \times 10 = 100$ $3.7 \times 100 =$ 370	$3.4 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ $3.4 \times 1,000 =$ 3,400
6. $3.2 \times 10^3 =$ 3,200	9. $2.1 \times 10^2 =$ 210
$3.2 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ $3.2 \times 1,000 =$ 3,200	$2.1 \times 10 \times 10 = 10 \times 10 = 100$ $2.1 \times 100 =$ 210
7. $4.5 \times 10^2 =$ 450	10. $4.5 \times 10^3 =$ 4,500
$4.5 \times 10 \times 10 = 10 \times 10 = 100$ $4.5 \times 100 =$ 450	$4.5 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ $4.5 \times 1,000 =$ 4,500

Use patterns to help you find the value of each expression.

11. $1.3 \times 10^3 =$ 1,300	13. $5.4 \times 10^2 =$ 540
$1.3 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ $1.3 \times 1,000 =$ 1,300	$5.4 \times 10 \times 10 = 10 \times 10 = 100$ $5.4 \times 100 =$ 540
12. $1.2 \times 10^2 =$ 120	14. $6.8 \times 10^3 =$ 6,800
$1.2 \times 10 \times 10 = 10 \times 10 = 100$ $1.2 \times 100 =$ 120	$6.8 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ $6.8 \times 1,000 =$ 6,800

14. The distance between two cities is about 3.4×10^3 miles. About how many miles would you have to drive? about 3,400 miles

INDEPENDENT WORK

Student Practice Book, pp. 51–52

Lesson 81
Additional Practice

Review

You can multiply a decimal by a power of 10.
There are 6.2×10^3 people at the football game. How many people are at the game?
The exponent 3 tells you to move three factors of 10 to multiply the number. Multiply 6.2 by three factors of 10.
 $6.2 \times 10^3 = 6.2 \times 10 \times 10 \times 10 = 6,200$
There are 6,200 people at the football game.

Write the multiplication using factors of 10. Then find the value.

1. 2.8×10^2	2. 5.4×10^3
$2.8 \times 10 \times 10 = 10 \times 10 = 100$ 280	$5.4 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ 5,400
3. 2.1×10^3	4. 5.8×10^2
$2.1 \times 10 \times 10 \times 10 = 10 \times 10 \times 10 = 1,000$ 2,100	$5.8 \times 10 \times 10 = 10 \times 10 = 100$ 580

15. The distance between two cities is about 3.4×10^3 miles. About how many miles would you have to drive? about 3,400 miles

E

Extend Thinking

Use It! Application Station

Move to the Left. Now Right! Students create a maze and write step-by-step directions for getting through the maze. *The content of this card has concepts covered later in Lesson 6-3. You may want to assign this card to students ready to explore content covered later in this unit.*



WORKSTATIONS

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication of multi-digit numbers.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



GO ONLINE

Student Practice Book, pp. 51–52

Use patterns to help you find the value of each expression.

$3.2 \times 10^1 =$ <u>320</u>	$3.2 \times 10^2 =$ <u>32</u>
$3.2 \times 10^3 =$ <u>3,200</u>	$3.2 \times 10^4 =$ <u>320</u>
$3.2 \times 10^5 =$ <u>32,000</u>	$3.2 \times 10^6 =$ <u>3,200</u>

13. $2.8 \times 10^4 =$ 2,800

14. $2.8 \times 10^5 =$ 28,000

15. $2.8 \times 10^6 =$ 280,000

16. The diameter of the Earth at the equator is about 7,927 miles. About how many times is the diameter of the Earth about 3,900 miles?

17. How many 1.8 $\times 10^7$ meter cables (cables for a water tower) could I buy with \$100? How many cables could I buy with \$1,000? How many cables could I buy with \$10,000? **Hint:** Sample answer: \$100 would buy 5 cables and \$1,000 would buy 50 cables.

18. How far is the sun from the Earth? The distance between the Earth and the sun is about 93 million miles. How many times farther is the sun from the Earth than the distance between the Earth and the moon? **Hint:** The distance between the Earth and the moon is about 238,900 miles. **Hint:** 9.3×10^7 miles.

Math in Motion Activity

Differentiation Resource Book, p. 52

Lesson 6-1 • Extend Thinking

Patterns When Multiplying Decimals by Powers of 10

Write the product of each multiplication. Write the relationship between the factors and the product.

Factor 1	Factor 2	Product
0.45	10^1	4.5
0.45	10^2	45
0.45	10^3	450
0.45	10^4	4,500
0.45	10^5	45,000
0.45	10^6	450,000

Use the pattern to help you find the product of each multiplication.

1. $0.45 \times 10^7 =$ 4,500,000

2. $0.45 \times 10^8 =$ 45,000,000

3. $0.45 \times 10^9 =$ 450,000,000

4. $0.45 \times 10^{10} =$ 4,500,000,000

5. $0.45 \times 10^{11} =$ 45,000,000,000

6. $0.45 \times 10^{12} =$ 450,000,000,000

7. $0.45 \times 10^{13} =$ 4,500,000,000,000

8. $0.45 \times 10^{14} =$ 45,000,000,000,000

9. $0.45 \times 10^{15} =$ 450,000,000,000,000

10. $0.45 \times 10^{16} =$ 4,500,000,000,000,000

11. $0.45 \times 10^{17} =$ 45,000,000,000,000,000

12. $0.45 \times 10^{18} =$ 450,000,000,000,000,000

13. $0.45 \times 10^{19} =$ 4,500,000,000,000,000,000

14. $0.45 \times 10^{20} =$ 45,000,000,000,000,000,000

15. $0.45 \times 10^{21} =$ 450,000,000,000,000,000,000

16. $0.45 \times 10^{22} =$ 4,500,000,000,000,000,000,000

17. $0.45 \times 10^{23} =$ 45,000,000,000,000,000,000,000

18. $0.45 \times 10^{24} =$ 450,000,000,000,000,000,000,000

19. $0.45 \times 10^{25} =$ 4,500,000,000,000,000,000,000,000

20. $0.45 \times 10^{26} =$ 45,000,000,000,000,000,000,000,000

21. $0.45 \times 10^{27} =$ 450,000,000,000,000,000,000,000,000

22. $0.45 \times 10^{28} =$ 4,500,000,000,000,000,000,000,000,000

23. $0.45 \times 10^{29} =$ 45,000,000,000,000,000,000,000,000,000

24. $0.45 \times 10^{30} =$ 450,000,000,000,000,000,000,000,000,000

INDEPENDENT WORK

Estimate Products of Decimals

Learning Targets

- I can explain how to estimate products of two decimals.
- I can use an estimated product to make predictions about a calculated solution.
- I can estimate products of decimals to assess if calculations are reasonable.

Standards

Major Supporting Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

- **MPP** Reason abstractly and quantitatively.
- **MPP** Use appropriate tools strategically.

Vocabulary

Math Terms	Academic Terms
estimate	cite
range	speculate
round	

Materials

The materials may be for any part of the lesson.

- *Blank Open Number Lines* Teaching Resource
- number cubes

Focus

Content Objectives

- Students estimate products of decimals.
- Students use estimated products to make predictions about a calculated solution.
- Students use estimated products to assess the reasonableness of a calculated solution.

Language Objectives

- Students discuss how to estimate products of two decimals using *by + gerund*.
- To support optimizing output, ELS participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students engage in active listening and work collaboratively with a partner to complete mathematical tasks.

Coherence

Previous

- Students added and subtracted multi-digit whole numbers (Grade 4).
- Students created place-value strategies to multiply decimals by powers of 10 (Lesson 1).

Now

- Students estimate products of decimals to assess if calculated solutions are reasonable.

Next

- Students will represent multiplication of decimals using decimal grids (Lesson 3).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students extend their understanding of estimation as a strategy for determining whether products are reasonable.

Procedural Skill & Fluency

- Students build proficiency estimating products of decimals.

Application

- Students find products to solve real-world problems.
- Application is not a targeted element of rigor for this standard.*

Number Routine About How Much



5–7 min

Build Fluency Students build number sense as they estimate the difference of two 2-digit decimal numbers.

Remind students that this is a mental activity, and exact answers are not needed.

These prompts encourage students to talk about their reasoning:

- How did you determine your estimate?
- Was your strategy the same or different for each expression? Why?
- What is a different way you could estimate the difference?

Purpose Students realize they need the price of gas per gallon, the number of gallons she needs, how much money she has, and to estimate a product of decimals to solve the problem.

Numberless Word Problem

- What math do you see in this problem?

Teaching Tip You may want to have students to first come up with their own noticing and wondering. Then have students form small discussion groups where they can share their comments and questions about the map.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of how to estimate products of decimals and are based on possible comments and questions that students may make during the share out.

- What operation would you use to solve this problem? Explain.
- Do you need an exact answer to solve this problem? Explain why or why not?

Math is... Mindset

- What are some ways you or your classmates can contribute to the group today?

Relationship Skills: Build Relationships

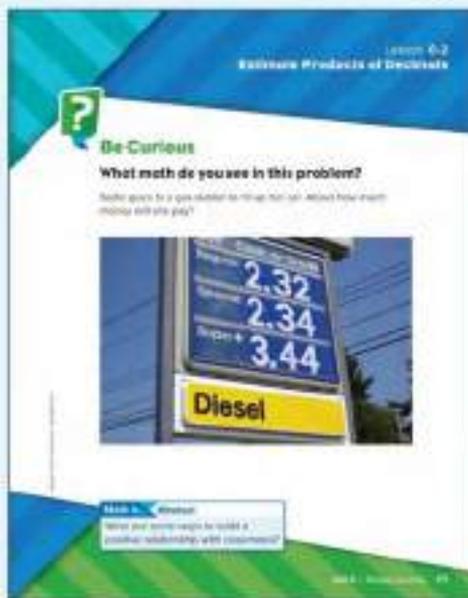
Help students identify and understand the value of their role(s) within the class community. As students collaborate in small groups to complete the Numberless Word Problem routine, invite each student to acknowledge the value of each group member. As students discuss what they notice and wonder, have them identify their peers' as well as their own contributions to the collaborative group effort.

Transition to Explore & Develop

Ask questions to get students thinking about the uses of estimates. Guide the discussion to have students think about reasonableness. Students might notice that different estimating strategies will lead to different estimates, and if so, allow it to become part of the conversation.

Establish Mathematics Goals to Focus Learning

- Let's think about how we might estimate the product of two decimals, and how we could use the estimate.



Lesson 6-2
Estimate Products of Decimals

Be Curious

What math do you see in this problem?

Radio spots in a gas station to help her get an idea how much money she will need?

2.32
2.34
3.44

Diesel

Math is... Mindset

What are some ways you or your classmates can contribute to the group today?



Be Curious

What math do you see in this problem?

Radio spots in a gas station to help her get an idea how much money she will need?

2.32
2.34
3.44

Diesel

GO ONLINE

Learn

Sadie will buy 28 gallons of regular gasoline to fill up her car.

What are some ways to estimate the total cost?

How can you use a number line to estimate products of decimals?

Think Way Estimate by rounding.

28 gallons is 30. 2.92 rounds to 3.
 $3 \times 3 = 9$
 Sadie will pay about \$9 for gas.

Another Way Estimate using a number line.

Math Is... Choosing Tools
 Why is a number line helpful when estimating?

$2.92 \times 28 = 81.76$ $3 \times 30 = 90$

A reasonable estimate is between \$80 and \$90.

Sadie calculated that the total cost is \$81.76. This is reasonable because it is within the range of \$80 to \$90 and closer to \$80.

You can use rounding or finding a range to estimate. You can use a number line to determine the reasonableness of an answer.

Work Together

Is this answer reasonable? Explain your thinking.
 $5 \times 27.8 = 139$

Key Strategy *Answer*: A reasonable estimate for the product is between 125 and 150.

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1 Pose the Problem

1.1 Pose Purposeful Questions

- Why might Sadie want to estimate the total cost?
- How will the total cost be related to the price per gallon and number of gallons?

2 Develop the Math

Choose the option that best meets your instructional goals.

2.1 Co-Craft Questions and Problems

Pair students and have them co-create and solve a problem similar to the one on the Learn page, then trade their problem with another pair. After each pair solves the other pair's problems, have them form a group of four to check solutions and correct any mistake. Revisit the task throughout the lesson for reinforcement.

3 Bring It Together

3.1 Elicit and Use Evidence of Student Thinking

- How can you use estimates when multiplying decimals?
- How is estimating the products of whole numbers similar to estimating the products of decimal numbers? How is it different?

Key Takeaways

- Estimating products helps make predictions about a calculated solution.
- Estimating products helps assess the reasonableness of a calculated solution.
- Strategies used to estimate products of whole numbers, such as rounding, compatible numbers, and front-end estimation, can also be used to estimate products of decimals.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of how to assess the reasonableness of the product of decimals. Have students work on the activity in pairs before asking them to explain whether the answer provided is reasonable.

Common Error Students may miss the decimal point in 27.8 and round 278 to 280 or 300 to estimate the product instead of multiplying 5 by 27, 28, or 30.

3.1.1 Language of Math

Have students share examples of situations in their life outside of school where they make estimates and how they make them. Make sure they include math language like *rounding* or *compatible numbers*, and use it correctly.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students explore whether an estimated product is greater than or less than an actual product based on comparing factors.

Directions: Display an expression, such as 5.6×3.9 . For each of the estimates below have students decide whether the product will be greater than or less than the calculated solution. Students should explain their reasoning.

$$\begin{array}{ll} 5 \times 3 & 6 \times 3 \\ 5 \times 4 & 6 \times 4 \end{array}$$

Support Productive Struggle

- How can you make an estimate that you know is greater than the calculated product?
- How can you make an estimate that you know is less than the calculated product?

Activity Debrief: Have students share their ideas about the estimated products. Facilitate a discussion to ensure that students understand that one estimate (6×4) is determined by rounding both factors to the nearest whole number. Two estimates (5×3 and 6×4) create a *range* for reasonable calculated products.

Math is... Choosing Tools

- Why is a range helpful when estimating?

Students detect possible errors by strategically using estimation and other mathematical knowledge.

Have students revisit the Pose the Problem question and discuss answers.

- What are some ways to estimate the total cost?

English Learner Scaffolds

Entering/Emerging Support students in understanding how to use *by + -ing* by expanding on what students learned using the gerund *using* in Lesson 1. Show students two tens rods. Say, *I can make twenty by connecting two tens rods*. Connect the two rods. Repeat the task twice with new objects, using *by + ing*. Finally, put a group of fifteen chips on the table. Write the following two sentences on the board: *I can find out how many by counting the chips. I can find out how many by count the chips*. Ask *Which is correct?* Accept pointing.

Developing/Expanding Support students in understanding how to use *by + -ing* by expanding on what students learned using the gerund *using* in Lesson 1. Show students two tens rods. Say, *I can make twenty by connecting two tens rods*. Connect the two rods. Repeat the task twice with new objects, using *by + ing*. Next, put a group of fifteen chips on the table. Provide the following sentence frame: *I can find out how many___ (counting) the chips*. Finally, have students find an example of this structure on the Learn page. (*You can*] estimate by rounding.)

Guided Exploration

Students build on their understanding of multiplication of whole numbers to estimate products of two decimals.

Facilitate Meaningful Mathematical Discourse

- **Think About It:** What strategies do you know for estimating?
 - How would you estimate the product of whole numbers?
 - Explain why 7.8 rounds to 8 and 2.32 rounds to 2.
-  Have the students create the equation after rounding. Ask:
- What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
-  Make available the *Blank Open Number Lines* Teaching Resource for students to use as a tool to help them estimate. Ask:
- Between which two whole numbers is 2.32? How do you know?
 - Between which two whole numbers is 7.8? How do you know?
-  Have the students use their estimate to assess the reasonableness of a calculated solution. Ask:
- If Sadie calculated the total cost to be \$18.10, is her calculated solution reasonable? Why or why not?

Math is... Choosing Tools

- Why is a range helpful when estimating?

Students detect possible errors by strategically using estimation and other mathematical knowledge.



Bridging/Reaching Instruct students to explain how to do something using *by + -ing*. Allow students to interject, pointing out any mistakes that they may catch in structure, meaning or understanding. For example, *No, you forgot to use by....* or *No, you didn't use....*

On My Own

Name _____

Estimate each product by rounding. Show your work.

1. $5.78 \times 5.36 \approx ?$
about 30

2. $3.02 \times 3.02 \approx ?$
about 24

3. $3.0 \times 4.92 \approx ?$
about 147

4. $0.15 \times 0.92 \approx ?$
about 320

5. $15.91 \times 39.71 \approx ?$
about 590

6. $24.09 \times 12.32 \approx ?$
about 292

Estimate each product by finding a range. Show your work.

7. $4.32 \times 1.88 \approx ?$
 $4 \times 2 = 8$; $5 \times 2 = 10$
between 8 and 10

8. $2.75 \times 3.95 \approx ?$
 $3 \times 3 = 9$; $3 \times 4 = 12$
between 9 and 12

9. $2.94 \times 1.9 \approx ?$
 $3 \times 2 = 6$; $3 \times 1 = 3$
between 3 and 6

10. $4.5 \times 1.5 \approx ?$
 $4 \times 1 = 4$; $5 \times 1 = 5$
between 4 and 5

11. $20 \times 9 \approx 180$; $21 \times 10 \approx 210$
between 180 and 210

12. $16 \times 2 \approx 32$; $17 \times 4 \approx 68$
between 32 and 68

13. Diego is buying 5.23 liters of water. The store charges \$1.71 per liter for all orders. About how much will the water cost? Can he spend his money on water?

Sample answer: about \$9. I rounded each decimal to the nearest whole number to estimate.

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14. Amy has \$100 to spend on a new bicycle. She has found a bicycle that costs \$120. How much more money does she need to buy the bicycle? Can she buy the bicycle with the money she has?

Yes. Sample answer: 1.20 is between 1 and 2; $16 \times 2 = 32$; the 16 wheels will cost less than \$32.

15. **11th-Grade Connection** Maya has 3.8 liters of a solution. She needs 4.7 liters more than she already has. About how many liters of the solution does she need?

Sample answer: $4 \times 4 = 16$; Maya needs about 16 liters of the solution.

16. **11th-Grade Connection** Find the product of each pair of numbers. Round to the nearest hundredth.

Sample answer: 3.2×5.6 and 2.8×6

Reflect

Why is estimating useful to solve these problems?

Answers will vary.

How do you know when to use estimation?

Answers will vary.

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 7–12 Students may round each factor to the nearest whole number rather than thinking about which two whole numbers the decimals falls between.

Item Analysis

Item	DOK	Rigor
1–12	1	Procedural Skill and Fluency
13–14	2	Application
15	2	Conceptual Understanding
16	2	Application
17–18	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- Why is estimating products of decimals helpful?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you or your classmates contribute to the group today?

Students discuss or how they developed stronger relationship skills.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain how to estimate products of two decimals.
- I can use an estimated product to make predictions about a calculated solution.
- I can estimate products of decimals to assess if calculations are reasonable.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Estimating products of decimals	5.NBT.B.7
2	2	Estimating products of decimals	5.NBT.B.7
3	2	Estimating products of decimals	5.NBT.B.7
4	2	Estimating products of decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 4 Then have students do

- 4 of 4 Additional Practice or any of the **U** or **E** activities
- 3 of 4 *Take Another Look* or any of the **U** activities
- 2 or fewer of 4 Small Group Intervention or any of the **U** activities

Key for Differentiation

- U** Reinforce Understanding
- U** Build Proficiency
- E** Extend Thinking



Lesson 6-2
Exit Ticket

Name _____

- What is the estimate for the product? Use rounding.
 51.2×4.2 7.8×75.3
about 200 about 912
- Which estimate is more accurate? Check off the one(s) you think is/are most accurate.
 - A. 5.3×2.1 is about 75.
 - B. 10.8×8.9 is about 90.
 - C. 5.4×75.3 is about 700.
 - D. 10.2×10.8 is about 850.
 - E. 10.8×25.6 is about 250.
- The distance around the earth is 25,000 kilometers. Diego rides his bike about 100 miles (16 kilometers) each day. About how many kilometers does Diego ride his bike?
about 28 kilometers
- Write two expressions that could be used to find a range of unknown numbers for this product 62.5×0.43 .
Sample answer: 62×3 and 63×4

Reflect On Your Learning

1. How confident
2. How well learning
3. Understanding
4. How much more you

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R Reinforce Understanding

SMALL GROUP

Reasonable Estimates!

Work with students in small groups. Provide each group with 3 number cubes. One student rolls a number cube to get a whole number. A second student rolls 2 cubes and uses the digits to make a decimal number that is less than 9.9. The numbers are recorded as a multiplication equation (e.g., 6×3.2). The other students estimate the product. Have students explain how they found their estimates.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Estimating Decimal Products Bingo
Students practice finding estimated products.



GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Estimate Products (Decimal Number Factors)



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 53

Lesson 6-2 Reinforce Understanding
Estimate Products of Decimals

Name _____

Review
Estimate the product of 8 and 7.2 to the nearest whole number.
 8×7.2 so we will round 7.2 to 7.
 $8 \times 7 = 56$, so we will round 56 to 56.

$8 \times 9 = 72$, so we will round the product 8×9.2 to 72.

Estimate each product by rounding to the nearest whole number.

1. 3.4×1.2 **about 21** 2. 38.6×7.9 **about 280**

3. 7.2×5.6 **about 40** 4. 20.5×5.4 **about 480**

Estimate each product by finding a range. The first one is done for you. Show your work.

5. 8.21×1.85
 $8 \times 1 = 8$, so 8.21×1.85 is between 8 and 16.

6. 8.9×13.4
 $8 \times 12 = 96$, $9 \times 13 = 117$, between 96 and 117

7. 9.4×5.3
 $10 \times 5 = 50$, $12 \times 6 = 72$, between 55 and 72

8. 30.79×3.7
 $30 \times 4 = 120$, $31 \times 5 = 155$, between 133 and 155

Differentiated Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 53–54

Lesson 6-2
Additional Practice

Name _____

Review
You can use estimation to determine whether a decimal is reasonable.

The journal at the store costs \$4.79. Henry buys 7.2 pounds of almonds. The cashier charges him \$23.87. Should Henry question the amount he just paid for?

Henry had estimated the cost of the almonds.
 4.79 rounds to 5, 7.2 rounds to 8, $5 \times 8 = 40$. Henry should pay about \$40 for the almonds.
Henry can also find a range of reasonable prices. 4.79 is between 4 and 5, 5.7 is between 5 and 6, for a reasonable range is between 4 and 36, so \$23.87 is not a reasonable price for the almonds.

Henry's amount charged, \$23.87, is not in the reasonable range. Henry should question the reason.

Estimate each product by rounding. Show your work.

1. 4.88×5.28 2. 2.71×5.17
 $4 \times 7 = 28$, about 28 $3 \times 5 = 15$, about 15

3. 3.0×3.8 4. 4.86×1.3
 $3 \times 4 = 12$, about 12 $5 \times 7 = 35$, about 35

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication of multi-digit numbers.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 53–54

Estimate each product by finding a range. Show your work.

8. 2.03×2.1 9. 5.60×10.00
 $7 \times 7 = 49$, $5 \times 5 = 25$, $5 \times 1 = 5$, $6 \times 2 = 12$,
 between 18 and 24 between 5 and 12
7. 0.7×0.8 8. 4.1×4.30
 $6 \times 6 = 36$, $7 \times 10 = 70$, $4 \times 4 = 16$, $5 \times 5 = 25$,
 between 54 and 70 between 16 and 25

6. Find a range of reasonable answers for two prices of 7.34 and 4.10. Explain how you found the range.

Sample answer: between 28 and 40; Since 7.34 is between 7 and 8 and 4.10 is between 4 and 5, the product lies in the range given by $7 \times 4 = 28$ and $8 \times 5 = 40$.

10. Sean has only \$1.00 left for filling station. He has the car's tank with 0.75 gallons of fuel. How many more gallons of fuel would he need for the gas? Explain what's reasonable in your answer.

Sample answer: about \$27; I rounded each decimal to the nearest whole number to estimate, and $8 \times 9 = 72$.

11. Evelyn has \$30 to spend on books. She has the car's tank with 0.75 gallons of fuel. How many more gallons of fuel would she need for the gas? Explain what's reasonable in your answer.

Sample answer: Since 0.75 is between 0 and 1 and 7.25 is between 7 and 8, the range of values for the book cost is between 0 and 7 and 8 and 8 is 8, or between \$70 and \$48. Since Evelyn has only \$30 to spend, she always will have enough money.



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Student Practice Book

M

Extend Thinking

Use It! Application Station

School Spirit Students use area and multiplication to create a school wall mural. *The content of this card has concepts covered later in Lesson 6-4. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 54

Lesson 6-3 • Extend Thinking

Estimate Products of Decimals

Warm-up

Estimate the product of each expression by rounding. Then check up the estimates that are equal. The final one is done for you as an example. Show your work.

Column A	Column B
3.12×0.6	7.34×2.1
$4 \times 6 = 24$	$6 \times 6 = 36$
0.8×0.9	1.9×0.28
$6 \times 8 = 48$	$6 \times 6 = 36$
400×0.1	0.007×4.2
$4 \times 5 = 20$	$0.1 \times 4 = 0.4$
$10.00 \times 2 \times$	3.9×4.02
$11 \times 2 = 22$	$4 \times 5 = 20$
0.1×0.4	0.01×0.1
$3 \times 11 = 33$	$6 \times 4 = 24$
0.7×4.0	0.7×0.8
$8 \times 5 = 40$	$7 \times 6 = 42$
0.02×10.8	0.00×0.1
$4 \times 11 = 44$	$7 \times 8 = 56$
0.44×7.4	1.03×0.2
$6 \times 7 = 42$	$2 \times 11 = 22$
0.7×0.08	0.002×0.9
$8 \times 7 = 56$	$11 \times 3 = 33$

Represent Multiplication of Decimals

Learning Target

- I can use decimal grids to help me represent and solve multiplication equations involving decimals.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Model with mathematics.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms

decimal grid
partition

Academic Terms

complex
negate

Materials

The materials may be for any part of the lesson.

- Blank Open Number Lines* Teaching Resource
- 10 × 10 Grids* Teaching Resource
- number cubes

Focus

Content Objective

- Students use decimal grids to represent and solve multiplication equations involving decimals.

Language Objectives

- Students discuss how to solve multiplication equations using decimal grids while answering *Why* and *Yes/No* questions.
- To support cultivating conversation and sense-making, ELs participate in MLR8: Discussion Supports and MLR6: Three Reads.

SEL Objective

- Students identify personal traits that make them good students, peers, and math learners.

Coherence

Previous

- Students added and subtracted multi-digit whole numbers (Grade 4).
- Students estimated products of decimals (Lesson 2).

Now

- Students represent multiplication of decimals using decimal grids.

Next

- Students will use multiplication strategies to multiply decimals to hundredths (Lesson 4).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students develop understanding of multiplication of decimals by representing multiplication using equations and decimal grids.

Procedural Skill & Fluency

- Students develop proficiency in multiplying with decimals by using decimal grids.

Application

- Students multiply with decimals to solve problems involving real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine About How Much?



5–7 min

Build Fluency Students build number sense as they estimate the difference of two 2-digit decimal numbers.

These prompts encourage students to talk about their reasoning:

- What did you do first to estimate the differences of each expression?
- What strategy did you use to estimate? How did you choose this strategy?
- What is another strategy to use in estimating the difference?



Purpose Students begin thinking of the “fraction of” concept that they will use to model a decimal times a decimal later. The dozen egg containers and the arrangement of the white/brown eggs mimic the grid model used when that is done.

Notice & Wonder

- How are they the same?
- How are they different?

Teaching Tip You may want to have students Think Pair Share to discuss how the eggs are the same and how they are different.

1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students’ understanding of how to represent multiplication of decimals and are based on possible comments and questions that students may make during the share out.

- What fraction of the dozen eggs is brown?
- If there were 10 eggs instead of 12 in each container, how could you use decimals to describe the number of brown eggs?

Math is... Mindset

- How can creative thinking help you solve a problem?

2.1 Self-Awareness: Self-Confidence

As students work through the Notice & Wonder routine, encourage creative thinking by inviting them to explore and consider alternative representations for multiplication. As a class, discuss some of the options students can use to represent multiplication. Then, have students check their answers using an alternative representation.

Transition to Explore & Develop

Ask questions to get students thinking about ways to represent multiplying decimals. Students might notice that they can use decimal grids in different ways to multiply with decimals.

1.1 Establish Mathematics Goals to Focus Learning

- Let’s think about how we might represent multiplication of decimals.

Learn

Joseph had money to buy sandwiches, but only \$0.22 more of money for each sandwich. Let's see how much he can spend.

How can you determine the cost of lettuce for all 5 sandwiches?

How can you determine grids to help you solve the problem?

Find the cost amount unknown, n .

$5 \times 0.22 = n$ **Answer: 1.10 or 110 ¢**

There are 22 hundredths of the whole dollar.

Joseph needs 5 portions of lettuce to make all 5 sandwiches.

Find the unknown n .

$0.22 \times 5 = n$

There are 22 hundredths of the whole dollar.

There are 5 portions of lettuce to make all 5 sandwiches.

The cost of lettuce for 5 sandwiches is \$1.10.

Work Together

We made \$1.10 out of how many sandwiches? How much to make 5 sandwiches? How many cents did we need?

1.2 eggs: $6 \times 0.2 = 1.2$




1 Pose the Problem

Discussion Supports

As students engage in discussing the answers to the three questions below, restate statements they make as a question to seek clarification. Encourage students ask useful questions to improve each others' ideas.

Pose Purposeful Questions

- What operation can help you determine how much the lettuce for all five sandwiches will cost?
- How can you represent the information you have?
- What strategy can you use?

2 Develop the Math

Choose the option that best meets your instructional goals.

Three Reads

1st Read: Have students underline the key number that will be used to solve the problem.

2nd Read: Have students write the meaning of each number in context (numbers, pounds, cost).

3rd Read: Have students work in pairs to create mathematical expressions.

3 Bring It Together

Elicit Evidence of Student Thinking

- How do decimal grids help you understand multiplication of decimals?
- How do you use decimal grids as a tool that help you multiply decimals?

Key Takeaway

- Multiplication of decimals can be represented using concrete models or drawings, such as decimal grids.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of how to find the product of decimals. Have students work on the activity in pairs before asking them to explain how they found their answers.

Common Misconception Students may think that the product of two factors must be greater than both numbers, but that is not true when one or more factors is between 0 and 1.

Language of Math

Students may have heard of the field American football is played on called a *gridiron*. A gridiron is great for broiling food over a flame, and resembles the lines on a football field. Have the students relate this to the appearance of a decimal *grid*.

CHOOSE YOUR OPTION

Activity-Based Exploration

Students develop strategies for multiplying decimals.

Materials: 10×10 Grids Teaching Resource, *Blank Open Number Lines* Teaching Resource

Directions: Read the first part of the Pose the Problem; ensure that students understand that 5×0.04 represents the total amount of lettuce. Encourage students to develop a strategy to solve.

Support Productive Struggle

- Is the answer more than 1 pound? More than 0.5 pound? How do you know?
- How can you use equal groups to help you find the total amount of lettuce?
- What tools can you use to help you find the total amount of lettuce?

Have groups share their products and their strategies for solving. Identify similarities and differences among the strategies and representations. Have students solve the next part of the Pose the Problem; ensure students understand that 0.2×0.9 represents the total cost. Encourage students to develop a strategy to solve.

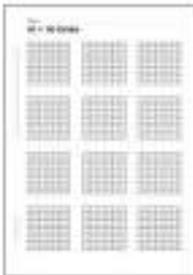
Math is... Modeling

- How do decimal grids help you understand multiplying decimals?

Students assess models to see if they have served their purpose.

Activity Debrief: Facilitate a discussion to ensure students understand multiplication of decimals can be represented as equal groups on a decimal grid. When multiplying two decimals, it is represented as a part of a part.

PDFs of the Teaching Resources are available in the Digital Teacher Center.



English Learner Scaffolds

Entering/Emerging Support students' understanding of *cost*. First, choose a classroom object, such as a notebook. Write a price on a sticker or piece of paper and put it on the object. Say *The price is \$1.00. It costs \$1.00*. Repeat the task with a different classroom objects. Say *The price is \$1.50*. Then prompt them to complete the following sentence saying the correct word (*costs*) aloud: *It _____ \$1.50.*

Developing/Expanding Support students' understanding of *cost*. First, choose a classroom object, such as a notebook. Write a price on a sticker or piece of paper and put it on the object. Say *The price is \$1.00. It costs \$1.00*. Repeat the task with a different classroom object. Say *The price is \$1.50*. Then prompt them to complete the following sentence saying the correct word (*costs*) aloud: *It _____ \$1.50*. Finally, ask students to repeat the task, choosing a classroom object, and make a sentence of their own using *cost*.

Guided Exploration

Students build on their understanding of multiplication to find products of decimals using decimal grids.

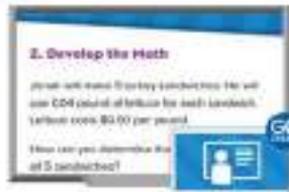
Use and Connect Mathematical Representations

- Have the students estimate the product of 5 and 0.04. Ask:
 - What factors will you use to estimate the solution? Why?
 - How can finding a range help you estimate?
- **Think About It:** What is the size of each group? How many groups are there?
- Have the students use the model to determine the product of 5 and 0.04. Ask:
 - What strategy did you use to find the product?
 - Why did you choose that strategy?
 - How did you use that strategy to find the product?
- Have the students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution of 0.2 reasonable? Why or why not?
 - What different ways could you represent 5×0.04 using decimal grids?
 - Will "tenths times tenths" always result in "hundredths"? Explain why or why not.
 - What do you think "tenths times hundredths" will result in? Why?
- Have the students assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution of 0.18 reasonable? Why or why not?

Math is... Modeling

- How do decimal grids help you understand multiplying decimals?

Students assess models to see if they have served their purpose.



Bridging/Reaching Ensure comprehension of the meaning of *cost*, then have students brainstorm words associated with *cost*; for example, *price, dollars, bucks, cents, etc.*

On My Own

Name _____

Write an equation and use a decimal grid to help you solve.

1. Cameron bought 100 lbs of milk for his class last week. His class will drink 100 lbs over the next 10 weeks. How much milk will they have left in 10 weeks?
 Sample answer: $100 - 100 = 0$.
 Least cost: 0.50 liter of milk for each week.

2. Jason has 0.5 amount of cabbage. The grocery store charges \$2.00 per pound. How much will Jason pay for the cabbage?
 Sample answer: $0.5 \times 0.5 = 0.25$.
 Jason will pay \$0.50 for the cabbage.

3. Tanya took 100 pieces of fabric to make gift bags. She makes 4 gifts. How much fabric does Tanya use?
 Sample answer: $0.4 \times 6 = 2.4$. Tanya uses 2.4 meters of fabric to make the gifts.

4. **STEM Connection** A rock has a mass of 2.4 kilograms. Mike estimates that the amount of granite in the rock is 0.3 of the total mass of the rock. How much granite is in the rock?
 Sample answer: $2.4 \times 0.3 = 0.72$.
 Mike's rock has 0.72 kilograms of granite.






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What is the product? Use a representative color.

$0.4 \times 0.4 = 0.16$ $0.43 \times 0.4 = 0.172$
 $0.02 \times 7 = 0.14$ $0.44 \times 0.8 = 0.352$
 $0.6 \times 0.2 = 0.12$ $0.08 \times 0.4 = 0.032$

6. Write an equation to show the product represented by the decimal grid. Sample answer: $3 \times 0.4 = 1.2$ or $0.4 \times 3 = 1.2$

7. **Satellite Fact Thinking** A movie costs 2 points of data for \$2.50 per year. How much money needs to buy 3.4 years of movie data for three months down Satellite pay for the data? How much will someone pay thinking for the latest?
 $2 \times 2.5 = 5.0$; Kaitoko pays \$5.00 for the data;
 $2.9 \times 0.8 = 2.32$; someone will pay \$13.

Reflect

How do multiplying by decimals relate to multiplying whole numbers?

Answers may vary.

Math is... Mindset

What are your goals for this year?
 What are your strengths?
 What are your challenges?
 What's your action plan?

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Practice

Build Procedural Fluency from Conceptual Understanding

Common Misconception: Exercise 3 Students might not understand why there are not 6 decimal grids to shade. Explain that they can shade the decimal factor repeatedly in one decimal grid until the grid is full, and then continue shading on the next one to see the number of tenths or hundredths.

Item Analysis

Item	DOK	Rigor
1–4	2	Application
5–10	1	Procedural Skill and Fluency
11–12	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How is multiplying decimals similar to multiplying whole numbers?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did creative thinking help you solve a problem?

Students reflect on how they practiced self-awareness.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can use decimal grids to help me represent and solve multiplication equations involving decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Represent Multiplication of Decimals	5.NBT.B.7
2	2	Represent Multiplication of Decimals	5.NBT.B.7
3	2	Represent Multiplication of Decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the D or F activities
2 of 3	<i>Take Another Look</i> or any of the D activities
1 or fewer of 3	Small Group Intervention or any of the F activities

Key for Differentiation

- P** Reinforce Understanding
- D** Build Proficiency
- F** Extend Thinking



Lesson 6.3
Exit Ticket

Name: _____

1. Which equation is represented by the decimal grid?

A. $0.02 \times 0.04 = 0.08$ B. $0 \times 0.4 = 0.4$
 C. $0.2 \times 0.01 = 0.2$ D. $0.2 \times 0.01 = 0.20$

2. Shaina uses a length of ribbon to make a bow. What length of ribbon will she need to make 7 bows? Use the decimal grid to help you solve. **2.7 meters**

3. A seventh-grade class sold 604 pounds of apples at their fundraiser. The shop sold 9 cartons of apples and sold 16 pounds of apples in each carton. How much leftover was used to make the 8 cartons of apples? Use the decimal grid to help you solve. **0.36 pounds**

Reflect On Your Learning

The confidence I feel about my learning is _____

1. I can build on my learning by _____

Assessment Resource Book 184

R Reinforce Understanding

SMALL GROUP

Multiply Whole Numbers and Decimals

Work with pairs of students. Provide students with 2 number cubes to roll. Tell them that the sum of the number cubes is a number in tenths. Repeat to find the second factor in the multiplication of decimals. Help the students multiply the two numbers, for example 1.2×0.5 , using decimal grids. Make sure students evaluate their answers for reasonableness. Repeat the activity as time allows.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Decimal Multiplication Task Cards

Students practice decimal multiplication.



GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Multiply Decimals by Whole Numbers-Model
- Multiply Two Decimal Numbers-Model



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 55

Lesson 6.2 Reinforce Understanding
Represent Multiplication of Decimals

Review

Representations use a hundred grid about solving multiplication problems involving decimals.

$4 \times 0.1 = 0.4$ Shade 4 columns of the grid 10 times.	$4 \times 0.12 = 0.48$ Shade 4 columns of the grid, then shade 2 squares of each column.
---	---

Use a decimal grid to help you solve each equation.

$3 \times 0.4 = 1.2$ 	$0.2 \times 0.6 = 0.12$
$4 \times 0.2 = 0.8$ 	$0.3 \times 0.7 = 0.21$
$0.3 \times 0.4 = 0.12$ 	$0.2 \times 0.6 = 0.12$

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INDEPENDENT WORK

Student Practice Book, pp. 55–56

Lesson 6.2
Additional Practice

Review

You can use a decimal grid to solve multiplication equations involving whole numbers and decimals or decimals and decimals.

Use 100 of 100-point grids. Shade 0.2 of the grids for a whole. What is the weight of the pencil(s) that you?

Write an equation. $0.2 \times 6 = 1.2$

Use a hundred grid to solve.

Shade 2 tenths of the grid. Shade 6 tenths of the 7 tenths.

There are 12 hundredths on the whole pencil.
So the whole pencil weighs 1.20 pound of the pencil.

Write an equation and use a decimal grid to help you solve.

1. Abbey used 0.18 gallons of water to fill a waterline. She has to remember to turn it off by the end of the day. How many gallons of water does Abbey use in all?

$0.18 + 0.18 = 0.36$
 $0.18 + 0.18 = 0.36$
 Abbey uses 0.36 gallons of water.

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Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication of multi-digit numbers.



Use It! Application Station

Move to the Left. Now Right! Students create a maze and write step-by-step directions for getting through the maze.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Student Practice Book, pp. 55–56

2. In a group of students, $\frac{1}{3}$ of the students are wearing a blue shirt. Of those students, $\frac{2}{3}$ of the shirts have a star pattern. What part of the group of students are wearing a blue shirt with a star pattern?

$0.3 \times 0.3 = 9$
 $0.3 \times 0.3 = 0.24$
0.24 of the group are wearing a blue shirt with a star pattern.

Complete each equation.

a. $4 \times 0.2 = 0.8$ b. $7 \times 0.6 = 0.35$
 c. $0.8 \times 0 = 0.26$ d. $0 \times 0.9 = 0.09$

3. Eight identical books are stacked to form a wall. Each centimeter block is $2\frac{1}{2}$ feet tall. How tall is the wall?

0.6 feet tall

4. Annette is buying empty apples. Each apple weighs 0.25 pounds. If Annette buys 7 apples, what is the weight of the apples?

1.82 pounds

5. Jose buys 8 pounds of seeds. Each seed packet costs \$0.33. How does the representation below to find the total cost of the seeds help you understand the problem? Explain. What is Jose's total cost?

Yes, \$4.64. Sample answer: The area is groups of 2 tens rods to show 8×0.30 .

Math in Motion Activity

Differentiation Resource Book, p. 56

Lesson 6-3 • Extend Thinking

Represent Multiplication of Decimals

Write an equation to show the product represented by the decimal grids. Sample answers shown.

1. $0.7 \times 0.8 = 0.56$

2. $0.8 \times 0.8 = 0.64$

3. $0.5 \times 0.3 = 0.15$

4. $0.4 \times 0.7 = 0.28$

5. $0.3 \times 0.4 = 0.12$

6. $0.4 \times 0.4 = 0.16$

7. $0.6 \times 0.7 = 0.42$

8. $0.3 \times 0.4 = 0.12$

9. $0.8 \times 0.8 = 0.64$

10. $0.5 \times 0.3 = 0.15$

11. $0.4 \times 0.7 = 0.28$

12. $0.3 \times 0.4 = 0.12$

13. $0.4 \times 0.4 = 0.16$

14. $0.6 \times 0.7 = 0.42$

15. $0.3 \times 0.4 = 0.12$

16. $0.8 \times 0.8 = 0.64$

17. $0.5 \times 0.3 = 0.15$

18. $0.4 \times 0.7 = 0.28$

19. $0.3 \times 0.4 = 0.12$

20. $0.4 \times 0.4 = 0.16$

21. $0.6 \times 0.7 = 0.42$

22. $0.3 \times 0.4 = 0.12$

23. $0.8 \times 0.8 = 0.64$

24. $0.5 \times 0.3 = 0.15$

25. $0.4 \times 0.7 = 0.28$

26. $0.3 \times 0.4 = 0.12$

27. $0.4 \times 0.4 = 0.16$

28. $0.6 \times 0.7 = 0.42$

29. $0.3 \times 0.4 = 0.12$

30. $0.8 \times 0.8 = 0.64$

31. $0.5 \times 0.3 = 0.15$

32. $0.4 \times 0.7 = 0.28$

33. $0.3 \times 0.4 = 0.12$

34. $0.4 \times 0.4 = 0.16$

35. $0.6 \times 0.7 = 0.42$

36. $0.3 \times 0.4 = 0.12$

37. $0.8 \times 0.8 = 0.64$

38. $0.5 \times 0.3 = 0.15$

39. $0.4 \times 0.7 = 0.28$

40. $0.3 \times 0.4 = 0.12$

41. $0.4 \times 0.4 = 0.16$

42. $0.6 \times 0.7 = 0.42$

43. $0.3 \times 0.4 = 0.12$

44. $0.8 \times 0.8 = 0.64$

45. $0.5 \times 0.3 = 0.15$

46. $0.4 \times 0.7 = 0.28$

47. $0.3 \times 0.4 = 0.12$

48. $0.4 \times 0.4 = 0.16$

49. $0.6 \times 0.7 = 0.42$

50. $0.3 \times 0.4 = 0.12$

51. $0.8 \times 0.8 = 0.64$

52. $0.5 \times 0.3 = 0.15$

53. $0.4 \times 0.7 = 0.28$

54. $0.3 \times 0.4 = 0.12$

55. $0.4 \times 0.4 = 0.16$

56. $0.6 \times 0.7 = 0.42$

57. $0.3 \times 0.4 = 0.12$

58. $0.8 \times 0.8 = 0.64$

59. $0.5 \times 0.3 = 0.15$

60. $0.4 \times 0.7 = 0.28$

61. $0.3 \times 0.4 = 0.12$

62. $0.4 \times 0.4 = 0.16$

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65. $0.8 \times 0.8 = 0.64$

66. $0.5 \times 0.3 = 0.15$

67. $0.4 \times 0.7 = 0.28$

68. $0.3 \times 0.4 = 0.12$

69. $0.4 \times 0.4 = 0.16$

70. $0.6 \times 0.7 = 0.42$

71. $0.3 \times 0.4 = 0.12$

72. $0.8 \times 0.8 = 0.64$

73. $0.5 \times 0.3 = 0.15$

74. $0.4 \times 0.7 = 0.28$

75. $0.3 \times 0.4 = 0.12$

76. $0.4 \times 0.4 = 0.16$

77. $0.6 \times 0.7 = 0.42$

78. $0.3 \times 0.4 = 0.12$

79. $0.8 \times 0.8 = 0.64$

80. $0.5 \times 0.3 = 0.15$

81. $0.4 \times 0.7 = 0.28$

82. $0.3 \times 0.4 = 0.12$

83. $0.4 \times 0.4 = 0.16$

84. $0.6 \times 0.7 = 0.42$

85. $0.3 \times 0.4 = 0.12$

86. $0.8 \times 0.8 = 0.64$

87. $0.5 \times 0.3 = 0.15$

88. $0.4 \times 0.7 = 0.28$

89. $0.3 \times 0.4 = 0.12$

90. $0.4 \times 0.4 = 0.16$

91. $0.6 \times 0.7 = 0.42$

92. $0.3 \times 0.4 = 0.12$

93. $0.8 \times 0.8 = 0.64$

94. $0.5 \times 0.3 = 0.15$

95. $0.4 \times 0.7 = 0.28$

96. $0.3 \times 0.4 = 0.12$

97. $0.4 \times 0.4 = 0.16$

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Unit 6
Decimal Multiplication

Use what you know about decimal multiplication to estimate the product. Do not perform the exact multiplication.

1. 1.37×0.2
Circle a or b to show the better estimate.
 A. less than 1
 B. greater than 1

Explain or show your thinking.
Explanations may vary.

2. 2.55×2.75
Circle a or b to show the better estimate.
 A. less than 1
 B. greater than 1

Explain or show your thinking.
Explanations may vary.

Use what you know about decimal multiplication to estimate the product. Do not perform the exact multiplication.

3. 2.04×5.54
Circle a or b to show the better estimate.
 A. less than 25
 B. greater than 25

Explain or show your thinking.
Explanations may vary.

4. 1.4×0.51
Circle a or b to show the better estimate.
 A. less than 0.5
 B. greater than 0.5

Explain or show your thinking.
Explanations may vary.

Reflect On Your Learning

For each problem, circle the step you found most helpful.

1. Read the problem carefully. 2. Estimate the product. 3. Compare the estimate to the actual product. 4. Check your work.

Analyze the Probe ✔ Formative Assessment

Targeted Concept Reason about the magnitude of decimals and the meaning of multiplication to compare decimal products to common benchmarks.

Targeted Misconceptions Some students think that multiplying always results in a product that is larger than both factors. While this is true when multiplying two whole numbers that are each greater than 1, it is not true when one factor is less than 1. Other students calculate the exact product rather than estimate because they have conceptual difficulty using the meaning of multiplication to estimate the product of two decimals. Some students round each factor to the nearest whole number and then multiply. This may result in an estimate that is not precise enough for the benchmarks that are given.

Sample Student Work

Below are examples of students' explanations.

Sample A

1. 1.37×0.2
Circle a or b to show the better estimate.
 A. less than 1
 B. greater than 1

Explain or show your thinking.
 I know that 1.37 is about 1 1/2. 1/2 of 1 = 1/2. 1/2 of 1/2 = 1/4. not even close to 1.

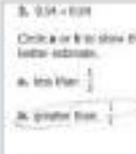
Sample B

2. 1.4×0.51
Circle a or b to show the better estimate.
 A. less than 1
 B. greater than 1

Explain or show your thinking.
 half of 1 + half = 0.75 + 0.75 = 1.50

Collect and Assess Student Work

Collect and review student response to determine possible misconceptions. See examples in If-Then chart.

IF incorrect... THEN the student likely...	Sample Misconceptions
<p>1. b does not use reasoning to estimate the product. In Exercise 1, the student may not reason that 1.37×0.2 represents a little more than 1 group of 0.2 (or a very small portion of 1.37). In Exercise 2, we are looking for about 1 of 2.29. In Exercise 3, we are looking for in Exercise 4. 1.4×0.62 represents more than 1 group of 0.62 (or more than 1 of 1.4).</p> <p>2. a</p> <p>3. b</p> <p>4. a</p>	 
<p>1. b overgeneralizes from whole number multiplication that a product is always greater than its factors. Note that this misconception results in correct choices for Exercises 2 and 4.</p> <p>3. b</p>	 
<p>2. a thinks that all decimals are small numbers; therefore, the product of two decimals must be a decimal less than 1 (or less than 1). Note that this misconception results in correct choices for Exercises 1 and 3.</p> <p>4. a</p>	 
<p>3. b mistakenly interprets multiplying a number by itself as being the same as doubling the number; OR rounds each factor up to 1 and then multiplies. This results in an estimated product of 1, but this is not the better estimate.</p>	 

Many of the above difficulties result in a combination of correct and incorrect responses.

For correct responses, be sure to check for sound reasoning.

Take Action

Choose from the following resources or suggestions:

- Revisit activities and representations for whole number multiplication in Lesson 5-4 to underscore the meaning of multiplication with decimals.
- Encourage students to think about multiplication as groups of a quantity. For about $\frac{11}{2}$ groups of 0.62.
- Provide opportunities for students to use concrete materials and drawings to help them build skill in visualizing the magnitude of a decimal quantity.
- Discuss the impact of rounding and ideas about the precision needed for an estimate.
- For example, if 0.55×0.75 is rounded to 1×1 , the estimate will not be precise enough for the benchmarks, “less than $\frac{1}{2}$ ” or “greater than $\frac{1}{2}$.”

Revisit the Probe after additional instruction. Have students review their initial answers to the probe. Use these questions for discussion:

- Are there any answers you would like to change? Explain why you might want to change them.
- Are there any questions that you still have about any of the Exercises on this probe?

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Use an Area Model to Multiply Decimals

Learning Targets

- I can use an area model to determine partial products.
- I can add partial products to calculate the product of two decimals.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- ◆ **5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Model with mathematics.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms

area
area model
decompose
partial product

Academic Terms

complement
evaluate

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- 0.5 cm grid paper

Focus

Content Objective

- Students use an area model to determine partial products and add partial products to calculate the product of two decimals.

Language Objectives

- Students discuss using area models to solve multiplication problems while answering *Wh-* and *Yes/No* questions and using the academic term *decompose*.
- To support optimizing output, ELs participate in MLR7: Compare and Connect.

SEL Objective

- Students discuss and practice strategies for managing stressful situations.

Coherence

Previous

- Students added and subtracted multi-digit whole numbers (Grade 4).
- Students represented multiplication of decimals using decimal grids (Lesson 3).

Now

- Students use multiplication strategies to multiply decimals to hundredths.

Next

- Students will use place-value patterns to multiply decimals (Lesson 5).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of partial products and area models to multiply decimals.

Procedural Skill & Fluency

- Students use strategies for multiplying whole numbers to proficiently multiply decimals.

Application

- Students multiply decimals to solve problems with real-world contexts.

Application is not a targeted element of rigor for this standard.

Number Routine

Find the Missing Values

5–7 min

Build Fluency

Students build reasoning skills as they are given a set of solved equations and must determine the missing values of *i* in related equations by looking for a pattern.

These prompts encourage students to talk about their reasoning:

- What do you notice about the equations? What pattern do you see in the rows?
- What pattern do you see in the columns?
- How can one equation help you to solve another?



Purpose The lesson content introduces that the digits in numbers move one decimal place to the right when multiplied by 0.1. One way to find the “outlier” here is to find the number that is not “237 with the digits moved the same number of decimal places.”

Which Doesn't Belong?

- Which doesn't belong?

Teaching Tip You may wish to have students' work in pairs as they explore the relationships between the numbers. Students can present their findings with the class and discuss any common or differing results.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of the movement of digits involved in multiplying decimals and are based on possible comments and questions that students may make during the share out.

- How are 237, 0.237, and 2,730 the same? How are they different?
- How is 273 different from the rest of the numbers?

Math is... Mindset

- What can you do to help yourself work independently?

Self-Management: Manage Stress

Begin the Which Doesn't Belong? routine with a short timed period, such as 5 minutes, for students to work independently. Invite students to think about strategies that can help them stay on task and work on their own. In addition to developing a sense of independence, students will also be able to practice self-discipline, self-motivation, and focus.

Transition to Explore & Develop

Have students think about multiplication area models involving whole numbers. Guide them to discuss partial products.

Establish Mathematics Goals to Focus Learning

- Let's think about how area models and place-value patterns can help us solve multiplication problems involving decimals.




Launch
How can you find the area of the board?
You solve one equation ($12 \times 25 = 300$) to determine the perimeter.
You calculate the area model to help you solve the equation.



Decompose rectangles into smaller partial products.
Decompose 12 into tens and ones.
Find partial products by finding the area of each rectangle.
Add the products.

	2	10	
12	$2 \times 25 = 50$	$10 \times 25 = 250$	
25	$2 \times 25 = 50$	$10 \times 25 = 250$	
	$2 \times 25 = 100$	$10 \times 25 = 250$	

The area of the board is 300 square meters.

Work Together
If each board is 18 meters wide and the total cost of the school is \$15,000, how many boards can the school buy?
\$15,000: Check students' work.

1 Pose the Problem

Pose Purposeful Questions

- How do you find the area of a rectangle?
- What types of similar problems have you solved in the past?
- How did you solve similar problems previously?

2 Develop the Math

Choose the option that best meets your instructional goals.

Compare and Connect

Pair students and assign them a problem to solve. Have one student solve it using a multiplication equation, and the other solve it using an area model. Then have the students compare and contrast the strategies they used to solve it. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How would you explain to a friend how to use an area model to multiply decimals?

Key Takeaway

- One multiplication strategy for multiplying decimals is to use an area model to determine partial products, which are then added together to arrive at the product.

Work Together

Students use their knowledge of area models to multiply a whole number and a decimal to find a sales total. Students can work on the activity in pairs before sharing their work.

Common Error Students may use the digits $(1 + 8)$ instead of the place value $(10 + 8)$ in the area model when decomposing 18. Invite students to estimate the solution and use the estimation to check the reasonableness of their solution.

Language of Math

The term *partial product* can be broken down to identify the meaning. The word *partial* means only a part; incomplete. The word *product* represents the answer to a multiplication problem. So, together, the term means part of the answer to a multiplication problem. This may help students remember that they need to combine all of the partial products to completely solve the problem.

Activity-Based Exploration

Students explore area models to determine different ways to decompose them to form partial products.

Directions: Ask students to write a multiplication problem involving two 2-digit numbers and draw an area model to represent the product. Have students record as many ways as possible to decompose the factors. Invite students to share ways they decomposed the factors, focus attention on similar methods of decomposing, such as decomposing by place value.

- Do you think these methods of decomposing will work for multiplying two decimals?

Have students explore different ways to decompose the factors 1.8 and 2.9 to find their product.

Support Productive Struggle

- How can you apply your method of decomposing whole numbers to decomposing decimals?
- Is your answer reasonable? How do you know?
- How is your area model the same as or different from another student's method?

Math is... Modeling

- How are the area models for decimals and whole numbers similar?

Students use a geometric representation to understand multiplication of decimals.

Activity Debrief: Discuss with students that an area model is one method they can use to multiply decimals. Using this method, they can decompose each factor, find partial products, and add the partial products to calculate the product.

English Learner Scaffolds

Entering/Emerging Support students' understanding of the phrase *similar* to using manipulatives. Show students a pair of *similar* objects. Point to one of the objects and say *This one is similar to that one*. Name key similarities. *They both have/are...* Show two objects that are not similar. Point to one of the objects and say *This one is not similar to that one*. Then, choose two new pairs of objects, one pair being similar, and the other not. Point to the two objects in each pair, and ask *Are they similar to each other?*

Developing/Expanding Support students' understanding of the phrase *similar* to using manipulatives. Show students a pair of similar objects. Point to one of the objects and say *This one is similar to that one*. Name key similarities: *They both have/are...* Show two objects that are not similar. Point to one of the objects and say *This one is not similar to that one*. Then, choose two new pairs of objects, one pair being similar, and the other not. Ask students to choose the pair of objects that is similar and to explain how they are similar.

Guided Exploration

Students use an area model to understand and solve a problem.

Use and Connect Mathematical Representations

- **Think About It:** How did you decompose factors when multiplying multi-digit whole numbers?
- Have students find 2×0.8 . Ask:
 - How can you rewrite 0.8 as the product of a whole number and 0.1?
 - How can you use that to rewrite 2×0.8 as the product of a whole number and 0.1?
 - How can you use decimal grids, equal groups, or place value to find that product?
 - What happened to the digits of 16 when it was multiplied by 0.1?
- Have students find 0.9×0.8 . Ask:
 - How can you rewrite 0.9 and 0.8 as the products of a whole number and 0.1?
 - How can you use those to rewrite 0.9×0.8 as the product of a whole number and 0.1s?
 - How can you use decimal grids, equal groups, or place value to find that product?
 - What happened to the digits of 72?
- Have the students estimate 1.8×2.9 to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Modeling

- How are the area models for decimals and whole numbers similar?

Students use a geometric representation to understand multiplication of decimals.



Bridging/Reaching Ask students to explain the phrase *similar* to, using classroom manipulatives to support their explanations. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, those items are not similar to each other because...* or *No, that's not correct because...*

On My Own

Name _____

What is the product? Use an area model to solve.

1. $32 \times 15 = 480$ 2. $14 \times 23 = 322$
 3. $11 \times 9 = 99$ 4. $5.2 \times 10 = 52$
 5. $50 \times 4.5 = 225$ 6. $1.8 \times 1.2 = 4.96$

7. **3** just spent over 4 hours \$5.50 buying 1 meter of fabric required for a skirt. He had enough for both the skirt, 3 meters. How many meters of fabric did he buy?
Sample answer:
 $5.5 \times 1.2 = 7$
 $9 + 1.2 + 5.5 + 0.1 = 14.8$
 The fabric will cost Michael \$14.80

8. **Erin** bought 4 items and an area model to multiply 14×11 is shown. How do you complete her work?

		10	1
10	$14 \times 10 = 140$	$14 \times 1 = 14$	
1	$1 \times 10 = 10$	$1 \times 1 = 1$	
	$14 \times 11 = 140 + 14 + 10 + 1 = 165$		

Sample answer: I disagree with Evelyn's work. I would write the value of each digit when setting up the area model ($1 = 0.1$, $7 = 0.4$). Then multiply to find the partial products. $7 + 1.4 + 5.4 + 0.08 = 8.88$

MATH • GO ONLINE

9. The Mathias family shop sold 15 pairs of sneakers and made \$121.50. How much did the pair they made today profit for today?
 $15 \times 8.1 = 121.50$ The old shop made \$121.50 selling 15 sneakers last week.

10. How far can you travel 15.4 miles per gallon of gas if you have 8.2 gallons of gas in a tank? How many miles can you travel with the gas in the tank?
 $15.4 \times 8.2 = 126.28$ Miles.

11. **Samuel** has 1.8 kg of flour. He used 0.32 kg of flour in each of the 5 loaves of bread she made. How much flour did Evelyn use? $0.32 \times 5 = 1.6$. Evelyn used 1.6 kg of flour.

Reflect

How can you use partial products and an area model to find the product of two one-factor decimals?
Answers may vary.

Math is... Mindset
 What do you think you will learn from this video?
 (See Math Replay video)

MATH • GO ONLINE

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 1-7 Students may incorrectly decompose the decimals creating an area model. Remind students to evaluate and decompose the factors by place value. Ask: *Is 15 is the same as $1 + 0.5$ or $10 + 5$?*

Item Analysis

Item	DOK	Rigor
1-6	1	Procedural Skill and Fluency
7	2	Application
8	3	Conceptual Understanding
9-10	2	Application
11	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you use partial products and an area model to find the product of two decimal factors?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What have you done that helped you work independently?

Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can use an area model to determine partial products.
- I can add partial products to calculate the product of two decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Use area models to multiply decimals	5.NBT.B.7
2	2	Use area models to multiply decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score Then have students do

2 of 2	Additional Practice or any of the 1 or 4 activities
1 of 2	<i>Take Another Look</i> or any of the 2 activities
0 of 2	Small Group Intervention or any of the 3 activities

Key for Differentiation

- 3 Reinforce Understanding
- 2 Build Proficiency
- 4 Extend Thinking



Lesson 6-4
Exit Ticket

Name: _____

1. What is the product 0.2×3.47 ? Use the area model to help you solve.

	2	+	0.4	
0.2	$0.2 \times 2 = 0.4$		$0.2 \times 0.4 = 0.08$	
+	$0.2 \times 0.4 = 0.08$		$0.2 \times 0.07 = 0.014$	

A. 0.68 B. 0.72
C. 0.8 D. 1.0

2. A rectangular floor mat is 2.7 meters long and 0.6 meters wide. What is the area of the floor mat? Use the area model to solve.

	2	+	0.6	
0.7	$0.7 \times 2 = 1.4$		$0.7 \times 0.6 = 0.42$	
+	$0.1 \times 2 = 0.2$		$0.1 \times 0.6 = 0.06$	

21.00 square meters

Reflect On Your Learning

Use confidence I'm still learning I understand I can teach someone else

○ ○ ○ ○

Mr. Johnson/Student Name

R Reinforce Understanding

SMALL GROUP

Fill It In

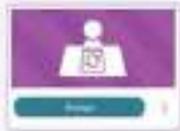
Work with pairs of students. Draw an area model with two rectangles. Students each estimate the product 6×0.46 . They take turns filling in the area model or the decomposed factors and the partial products. Ask students to identify the value of each partial product. When complete, both students add the partial products and discuss whether the result makes sense based on their estimate.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Multiply Decimal Numbers (Area Model)



INDEPENDENT WORK

Differentiation Resource Book, p. 57

Lesson 6-4 • Reinforce Understanding
Use an Area Model to Multiply Decimals

Name: _____

Review
 Decompose the factors by place value. Use this to set up your area model to find the product.

$36 \times 23 = (30 + 6) \times (20 + 3)$

30	6
30 × 20 = 600	30 × 3 = 90
6 × 20 = 120	6 × 3 = 18
600 + 90 + 120 + 18 = 828	

$36 \times 23 = 828$

Use an area model to solve.

$1.23 \times 12 = 14.76$ $(1.00 + 0.20 + 0.03) \times (10 + 2)$ $1.00 \times 10 = 10$ $1.00 \times 2 = 2$ $0.20 \times 10 = 2$ $0.20 \times 2 = 0.4$ $0.03 \times 10 = 0.3$ $0.03 \times 2 = 0.06$ $10 + 2 + 2 + 0.4 + 0.3 + 0.06 = 14.76$	$1.23 \times 27 = 33.21$ $(1.00 + 0.20 + 0.03) \times (20 + 7)$ $1.00 \times 20 = 20$ $1.00 \times 7 = 7$ $0.20 \times 20 = 4$ $0.20 \times 7 = 1.4$ $0.03 \times 20 = 0.6$ $0.03 \times 7 = 0.21$ $20 + 7 + 4 + 1.4 + 0.6 + 0.21 = 33.21$
$2.1 \times 3.4 = 7.14$ $(2.00 + 0.10) \times (3.00 + 0.40)$ $2.00 \times 3.00 = 6$ $2.00 \times 0.40 = 0.8$ $0.10 \times 3.00 = 0.3$ $0.10 \times 0.40 = 0.04$ $6 + 0.8 + 0.3 + 0.04 = 7.14$	$3.2 \times 2.5 = 8.00$ $(3.00 + 0.20) \times (2.00 + 0.50)$ $3.00 \times 2.00 = 6$ $3.00 \times 0.50 = 1.5$ $0.20 \times 2.00 = 0.4$ $0.20 \times 0.50 = 0.1$ $6 + 1.5 + 0.4 + 0.1 = 8.00$
$8.5 \times 1.6 = 13.6$ $(8.00 + 0.50) \times (1.00 + 0.60)$ $8.00 \times 1.00 = 8$ $8.00 \times 0.60 = 4.8$ $0.50 \times 1.00 = 0.5$ $0.50 \times 0.60 = 0.3$ $8 + 4.8 + 0.5 + 0.3 = 13.6$	$6.2 \times 2.1 = 13.02$ $(6.00 + 0.20) \times (2.00 + 0.10)$ $6.00 \times 2.00 = 12$ $6.00 \times 0.10 = 0.6$ $0.20 \times 2.00 = 0.4$ $0.20 \times 0.10 = 0.02$ $12 + 0.6 + 0.4 + 0.02 = 13.02$

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Decimal Multiplication Tic Tac Toe
 Students practice multiplication of decimals.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 57–58

Lesson 6-4
Additional Practice

Name: _____

Review
 You can use an area model to find the product of two decimal factors or a mixed number and a decimal.

Shelly has a stack of 12 books. Each book weighs 2.9 pounds. How much does the stack of books weigh?

Write an equation to represent the problem. Use an area model to solve.

12	2.9	34.8
10	2.9	29
2	2.9	5.8
29 + 5.8 = 34.8		

The stack of books weighs 34.8 pounds.

Write an equation to represent the problem. Then use an area model to solve.

4. A banner that 78 inches wide is shown in the form of the train. Each rail is 4.5 inches long. What is the total perimeter of the train? $13 \times 4.5 = 58.5$ inches.

13	4.5	58.5
10	4.5	45
3	4.5	13.5
45 + 13.5 = 58.5		

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Generalizations about Multiplying Decimals

Learning Targets

- I can use patterns based on place value concepts and properties of operations to make generalizations about multiplying decimals.
- I can use those generalizations to determine the placement of digits in a product.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Look for and make use of structure.

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

area model
digit
partial product

Academic Terms

assert
expand

Material

The materials may be for any part of the lesson.

- place-value charts

Focus

Content Objective

- Students use patterns based on place-value concepts and properties of operations to determine the placement of digits in a product.

Language Objectives

- Students explain how to use patterns in calculations to multiply decimals by making generalizations.
- To support sense-making and maximizing meta-awareness, ELs participate in MLR8: Discussion Supports and MLR7: Compare and Connect.

SEL Objective

- Students reflect on and describe the logic and reasoning used to make a mathematical decision or conclusion.

Coherence

Previous

- Students added and subtracted multi-digit whole numbers (Grade 4)
- Students used multiplication strategies to multiply decimals to hundredths (Lesson 4).

Now

- Students use place-value patterns to multiply decimals.

Next

- Students will choose and use strategies to multiply decimals (Lesson 6).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students extend their understanding of place value to determine the product of two decimal factors.

Procedural Skill & Fluency

- Students increase proficiency with multiplying decimals by making generalizations about the products of decimal factors.

Application

- Students apply generalizations to solve real-world problems.
- Application is not a targeted element of rigor for this standard.*

Number Routine

Find the Missing Value

5–7 min

Build Fluency Students build reasoning skills as they are given a set of solved equations and must determine the missing values in related equations by looking for a pattern.

Remind students that this is a mental math activity.

These prompts encourage students to talk about their reasoning:

- How did a pattern help you evaluate the remaining equations?
- How do the number of zeros in the factors compare to the number of zeros in the products?
- Will the number of zeros in the products always be equal to the number of zeros in the factors? Do the equations after 5×6 follow this pattern? What is different about 5×6 ?



Purpose Students think about what happens to a product if one of its factors is multiplied by a power of 10 and look for a pattern.

Is It Always True?

- Is the pattern always true?

Teaching Tip You may wish to have students work in small groups to discuss what they notice about the multiplication problems. Invite them to share what they are wondering and how they decide how to analyze the equations. Encourage students to share their observations and to listen respectfully to classmates. Students can build off of each other's ideas in order to fully develop the pattern.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of using place-value patterns to multiply decimals and are based on possible comments and questions students may make during the share out.

- What is happening in each of the equations? What did you do first to find the pattern?
- How can we check a pattern to see if it works?
- What are you wondering about the pattern?

Math is... Mindset

- How can you think about the equations in different ways?

Responsible Decision-Making: Evaluate

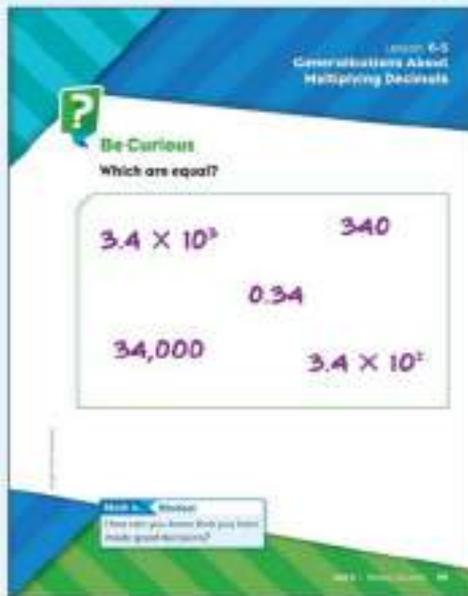
As students begin the Is It Always True? routine, have them think about different ways to analyze or describe the equations. As they analyze the equations, encourage them to think about different attributes or characteristics.

Transition to Explore & Develop

Focus students' attention on what generalizations they can make about what happens to a product if one of its factors is multiplied by a power of 10.

Establish Mathematics Goals to Focus Learning

- Let's think about what happens to a product if one of its factors is multiplied by a power of 10.



Lesson 6-5
Generalizations About
Multiplying Decimals

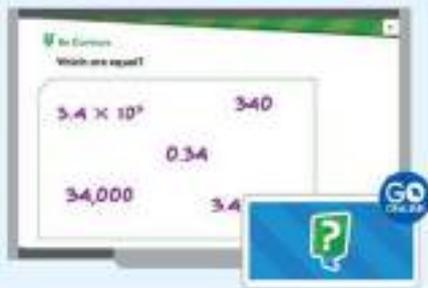
Be Curious
Which are equal?

3.4×10^3 340

0.34

34,000 3.4×10^2

Math is... Mindset
How can you think about the equations in different ways?



Be Curious
Which are equal?

3.4×10^3 340

0.34

34,000 3.4

GO ON!

Learn

How can you use the solution from one equation to solve the other two equations?

$9x + 2y = 14$ $9x + 2y = 4$ $9x + 2y = 10$

You know $9x + 2y = 20$ or $1,200$. You can use place value to help you understand the relationship between the equations.

$9x + 2y = 1,200$	$9x + 2y = 1,200$
$9x + 2y = 120.0$	$9x + 2y = 120.0$
$9x + 2y = 12.00$	$9x + 2y = 12.00$
$9x + 2y = 1.200$	$9x + 2y = 1.200$

If the digits in each factor move across to the right, the digits in the product have the same number of places to the right.

Activity *Number patterns*
How can you use the patterns in the equations to help you understand the relationship between the equations?

You can use patterns to make generalizations about multiplying decimals.

Now Try This

How can you use the solution for the first equation to solve the others?

$33 \times 24 = 7$	Simplify answers. I can compare the digits of the factors and move the digits in the product the same number of places.
$3.3 \times 24 = 7$	
$33 \times 2.4 = 7$	
$3.3 \times 2.4 = 7$	

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1 Pose the Problem

Discussion Supports

As students engage in discussing the answers to the four questions, restate statements they make as a question to seek clarification. Encourage students to challenge each other's ideas when warranted, as well as to elaborate on their ideas and give examples.

Pose Purposeful Questions

- If the factors in multiplication equations share the same digits in the same order, what do you predict about the digits in their products?
- How can numbers have the same digits in the same order, but different values?

2 Develop the Math

Choose the option that best meets your instructional goals.

Compare and Connect

Pair students. Provide them with three equations similar to those on the Learn page. Assign one unsolved equation to each student to work on individually. Then have the students compare and contrast the strategies they used to solve their equation. Revisit this activity throughout the lesson to help students build proficiency.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- How can you use the products of whole numbers to help you multiply decimals?

Key Takeaway

- Place-value concepts and properties of operations can justify patterns in the placement of digits when multiplying two decimal numbers.

Work Together

Students analyze equations with factors that are multiples of powers of ten to determine how the whole number product can be used to find the similar decimal products.

Common Error Make sure students (especially ones who are moving the decimal point), are careful with left/right. If the digits in a factor move right, the digits in the product move right.

Language of Math

Students need reinforcement in the proper naming of decimals, as errors in pronunciation can lead to confusion, e.g., tens and tenths. Provide opportunities for students to say the names of decimal numbers repeatedly and remind them that Math Is...Precision is about communicating precisely to others in addition to calculating accurately and efficiently.

Activity-Based Exploration

Students analyze products of related decimal factors to identify place value patterns when multiplying decimals.

Directions: Have students work on their own or in small groups. Ask them to write down the equations from the Pose the Problem. Before calculating the products, ask students to predict similarities and differences of the products and discuss how they came to these conclusions.

After students have had time to record their prediction, have them find the products using previously taught strategies. Students should determine whether their prediction was true, and discuss why. Ask each student or group to create a generalization statement about multiplying decimals to share with the class.

Support Productive Struggle

- How are each of the expressions related to the whole-number expression?
- What did you do first to find a pattern?
- How can you check a pattern to see if it works?
- How can you think about the expressions in a different way?

Math is... Generalizations

- How can you use the patterns in the calculations to efficiently multiply decimals?

Students use repeated calculations to create general methods.

Activity Debrief: Facilitate a discussion about patterns in place value when multiplying decimals. Ensure students understand how the relationship between factors impacts the relationship between products.

Have students revisit the Pose the Problem question and discuss answers.

- How can you use the solution from one equation to solve the other two equations?

English Learner Scaffolds

Entering/Emerging Support students in understanding cause and effect as expressed by *If... then...* statements. Go to your classroom door. Point at *then...* statements. Go to your classroom door. Point at *then...* statements. Go to your classroom door. Point at the doorknob, and say, *If I turn this, the door opens*, then demonstrate. Repeat with a new classroom object or manipulative. Then, show students two more object or manipulative. Then, ask students to perform understanding. For example, *No, that's not correct because... or No, if the digits...*

Developing/Expanding Support students in understanding cause and effect as expressed by *If... then...* statements. Go to your classroom door. Point at the doorknob, and say, *If I turn this, the door opens*, then demonstrate. Repeat with a new classroom object or manipulative. Then, ask students to perform understanding. For example, *No, that's not correct because... or No, if the digits...*

Bridging/Reaching Ask students to explain what happens if the digits in one place moves places to the right. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, that's not correct because... or No, if the digits...*

Guided Exploration

Students extend their understanding of multiplying decimals to make a generalization using place value patterns.

Facilitate Meaningful Mathematical Discourse

- **Think About It:** What do you notice about these equations?

Have the students use area models to solve $48 \times 26 = m$, $48 \times 2.6 = n$, and $48 \times 0.26 = p$. Ask:

- How can you estimate each product?
- How will you decompose each factor? Why?
- How can you find the partial products?
- How can you find each product?
- Are your calculated products reasonable? How do you know?

Distribute place-value charts as a tool to assist students answering the following. Ask:

- How do the digits in 26 and 1,248 relate to the digits that are in $\frac{1}{10}$ of 26 and in $\frac{1}{10}$ of 1,248?
- How do the digits in 26 and 1,248 relate to the digits that are in 26×0.1 and in $1,248 \times 0.1$?
- How do the digits in 26 and 1,248 relate to the digits that are in $\frac{1}{100}$ of 26 and $\frac{1}{100}$ of 1,248?
- How do the digits in 26 and 1,248 relate to the digits that are in 26×0.01 and $1,248 \times 0.01$?

Math is... Generalizations

- How can you use the patterns in the calculations to efficiently multiply decimals?

Students use repeated calculations to create general methods.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Use patterns to multiply decimals	5.NBT.B.7
2	2	Use patterns to multiply decimals	5.NBT.B.7
3	2	Use patterns to multiply decimals	5.NBT.B.7
4	2	Use patterns to multiply decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 4 Then have students do

4 of 4 Additional Practice or any of the **U** or **F** activities

3 of 4 *Take Another Look* or any of the **U** activities

2 or fewer of 4 Small Group Intervention or any of the **U** activities

Key for Differentiation

U Reinforce Understanding

U Build Proficiency

F Extend Thinking



Lesson 6.5
Exit Ticket

Name: _____

- Complete the patterns.
 $4.2 \times 1 = 4.2$, $4.2 \times 10 = 42$, $4.2 \times 100 = 420$, of the product 4.2×5 .
 a. 210 b. 210.7
 c. 21 d. 210
- Draw arrows that show $2.3 \times 7 = 16.1$ like-powers patterns in both numbers each operation in True or False.

	True	False
$0.23 \times 7 = 1.61$		<input checked="" type="checkbox"/>
$23 \times 7 = 161$	<input checked="" type="checkbox"/>	
$23 \times 7 = 16.1$		<input checked="" type="checkbox"/>
$2.3 \times 7 = 16.1$	<input checked="" type="checkbox"/>	
- What is the product? Use place-value patterns to solve the equations.
 $34 \times 55 = 1870$
 $34 \times 5.5 = 187.2$
 $34 \times 0.55 = 18.72$

Reflect On Your Learning

On confidence On all learning Confident I can work on my own.

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R Reinforce Understanding

SMALL GROUP

Fill It In and Predict

Work with pairs of students. Draw an area model with two rectangles. Students find the product of 6×76 by taking turns filling in each empty space in the area model for the decomposed factors and the partial products. Both students add the partial products. Have students predict the products answers for $.6 \times 76$, 6×7.6 , and $.6 \times .76$ and explain their reasoning. Assist students in revising their model to show these products before solving.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Multiply Decimal Numbers (Patterns)



INDEPENDENT WORK

Differentiation Resource Book, p. 59

Lesson 8.6 • Reinforce Understanding Generalizations about Multiplying Decimals

Name _____

Review

Answer:

- $22 \times 12 = 2,386$
 $2.2 \times 12 = 23.86$ This is 10 times $2,386$.
 $22 \times 1.2 = 23.86$ This is 10 times $2,386$ of 1.2 .
 $2.2 \times 1.2 = 2.386$ This is 100 times $2,386$ of 1.2 of 1.2 .

Complete each sentence.

1. $2.6 \times 5 = 13.0$ of $26 \times 5 = 130$ of the product 26×5 .
 2. $2.6 \times 5 = 13.0$ of $26 \times 5 = 130$ of 2.6 of the product 26×5 .
 3. $2.6 \times 5 = 13.0$ of $26 \times 5 = 130$ of $2.6 \times 5 = 13.0$ of the product 26×5 .

What is the product?

4. $82 \times 21 = 1,722$
 $8.2 \times 2.1 = 17.22$
 $82 \times 2.1 = 172.2$
5. $82 \times 21 = 1,722$
 $8.2 \times 2.1 = 17.22$
 $82 \times 2.1 = 172.2$
6. $82 \times 21 = 1,722$
 $8.2 \times 2.1 = 17.22$
 $82 \times 2.1 = 172.2$
7. $2.7 \times 36 = 97.2$
 $2.7 \times 3.6 = 9.72$
 $2.7 \times 36 = 97.2$

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station Related Decimal Multiplication Task Cards

Students practice decimal multiplication.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 59–60

Lesson 8.6 Additional Practice

Name _____

Review

You can use place value to help make generalizations about multiplying decimals.

Solve each of the equations.

$25 \times 16 = 400$ $2.5 \times 1.6 = 4$ $25 \times 1.6 = 40$

You know $25 \times 16 = 400$. Use this information to help you find the solutions to the other equations.



Complete each sentence.

1. $1.6 \times 25 = 40$ of $16 \times 25 = 400$ of the product 16×25 .
 2. $1.6 \times 25 = 40$ of $16 \times 25 = 400$ of 1.6 of the product 16×25 .
 3. $1.6 \times 25 = 40$ of $16 \times 25 = 400$ of $1.6 \times 25 = 40$ of the product 16×25 .

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Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication of multi-digit numbers.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 59–60

What is the product?

4. $88 \times 27 = 2,376$ 5. $27 \times 29 = 783$ 6. $88 \times 27 = 2,376$
 $88 \times 2.7 = 237.6$ $27 \times 2.9 = 78.3$ $88 \times 27 = 2,376$
 $88 \times 0.27 = 23.76$ $2.7 \times 2.9 = 7.83$ $88 \times 0.27 = 23.76$
14.95 **7.83** **31.08**

What is the product? Explain how you can use place-value patterns to solve.

Sample answer: If one factor is $\frac{1}{10}$ of an original factor, the new product will be $\frac{1}{10}$ of the whole-number product. If one factor is $\frac{1}{100}$ of an original factor, the new product will be $\frac{1}{100}$ of the whole-number product. If both factors are $\frac{1}{10}$ of the original factors, the new product will be $\frac{1}{100}$ of the whole-number product.

7. $36 \times 32 = 1,152$ 8. $41 \times 58 = 2,384$
 $36 \times 3.2 = 115.2$ $41 \times 5.8 = 238.4$
 $3.6 \times 3.2 = 11.52$ $4.1 \times 5.8 = 23.84$

9. A fence between a basketball court and 10 basketball courts is 23 feet tall. A copy of the fence is made one-tenth as tall. How long will it be? Find the area of a wall that is 1.3 feet tall. How long will it be? Find the area of the smaller room compared to the area of the larger room?

430 square feet; 4.2 square feet; the area of the second mural is $\frac{1}{100}$ of the area of the larger mural.

Math
Fluency
Activity

Extend Thinking

Use It! Application Station

Rock Garden Students use metric measurements to create a model of a rock garden. *The content of this card has concepts covered later in Lesson 6-6. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Differentiation Resource Book, p. 60

Lesson 6-5 • Extend Thinking

Generalizations about Multiplying Decimals

Notice:

Determine where the decimal point goes to make the equation true. Rewrite the equation. *Sample answers given.*

1. $41 \times 28 = 1,148$
 $4.1 \times 28 = 114.8$

2. $1.6 \times 3 = 4.8$
 $5.36 \times 3 = 16.08$

3. $200 \times 12 = 2,400$
 $20.3 \times 1.2 = 24.36$ or $42,182 \times 0.12$

4. $56 \times 24 = 1,344$
 $5.6 \times 0.24 = 1.344$

Fill in the blanks:

5. $39.5 \times 16 = 632.0$
 $3.95 \times 16 = 63.2$
 $0.395 \times 16 = 6.32$
 $39.5 \times 1.6 = 63.2$
 $3.95 \times 1.6 = 6.32$

6. $22 \times 24 = 528$
 $2.2 \times 24 = 52.8$
 $0.22 \times 24 = 5.28$
 $2.2 \times 2.4 = 5.28$
 $0.22 \times 2.4 = 0.528$

7. $52 \times 6.7 = 348.4$
 $5.2 \times 6.7 = 34.84$
 $0.52 \times 6.7 = 3.484$
 $5.2 \times 0.67 = 3.484$

8. $12 \times 0.81 = 9.72$
 $1.2 \times 0.81 = 0.972$
 $0.12 \times 0.81 = 0.0972$
 $1.2 \times 8.1 = 9.72$
 $0.12 \times 8.1 = 0.972$

Explain Strategies to Multiply Decimals

Learning Targets

- I can explain why I chose a strategy to solve multiplication equations involving decimals.
- I can understand other strategies to solve multiplication equations involving decimals.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Construct viable arguments and critique the reasoning of others.

Vocabulary

Math Terms

area model
decimal grid
decomposition
partial product
unknown

Academic Terms

relevant
suggest

Materials

The materials may be for any part of the lesson.

- decimal grids
- Show and Explain Your Reasoning* Teaching Resource

Focus

Content Objectives

- Students can explain their reasoning for using different strategies to solve.
- Students explain different strategies to multiply decimals.

Language Objectives

- Students explain their reasoning for using particular strategies to multiply decimals while answering *Wh-* questions.
- To support cultivating conversation, ELs participate in MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students discuss the value of hearing different viewpoints and approaches to problem solving.

Coherence

Previous

- Students added and subtracted multi-digit whole numbers (Grade 4).
- Students used place-value patterns to multiply decimals (Lesson 5).

Now

- Students choose and use strategies to solve real-world problems involving the product of decimals.

Next

- Students will divide multi-digit whole numbers (Unit 7).
- Students will add, subtract, multiply, and divide using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of multiplying decimals as they use representations and models to find the product of decimals.

Procedural Skill & Fluency

- Students build proficiency with choosing and using strategies for multiplying decimals.

Application

- Students apply their understanding of multiplication of decimals to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Where Does It Go?

5–7 min

Build Fluency

Students build number sense as they place the same decimal number on number lines with different end points.

These prompts encourage students to talk about their reasoning:

- What did you notice about 16.72?
- What did you notice about each number line?
- How did you decide where to place 16.72 on each number line?
- How could you label the number lines to help with placing the number?



Purpose Students think about what the problem represents and how the parts relate to the whole. This is an entry point to choosing one of the strategies they know for multiplying decimals to solve the problem.

Numberless Word Problem

- What math do you see in this problem?

Teaching Tip You may want to have students work in pairs to discuss what they notice about the word problem.

1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' noticing and wondering about choosing and using strategies to multiply decimals and are based on possible comments and questions that students may make during the share out.

- What operation would you use to solve this problem?
How do you know?
- What kinds of numbers do you think are involved in this problem?
Why?

Math is... Mindset

- How can you show others that you value their ideas?

1.2 Social Awareness: Appreciate Diversity

As students consider the Numberless Word Problem routine, invite them to discuss different strategies that they might use to solve a problem like this. As students share their unique thought processes and ideas, emphasize the value of the differences as well as the similarities so students can understand the importance of diversity within a math context.

Transition to Explore & Develop

Ask questions that get students thinking about strategies and models used to multiply decimals. Guide students to think about how they can explain strategies used to solve real-world problems involving decimal products.

1.3 Establish Mathematics Goals to Focus Learning

- Let's think about choosing and using strategies that can be used to multiply decimals and solve real-world problems.

Lesson 6-6
Explain Strategies to Multiply Decimals

Be Curious

What math do you see in this problem?

Why did the bike rental company choose to spend each day less on the bike to provide the same rate? Any other ideas for how the company could save to reduce costs?

Math is... Mindset

How can you show others that you value their ideas?

Lesson 6-6

Be Curious

What math do you see in this problem?

Why did the bike rental company choose to spend each day less on the bike to provide the same rate? Any other ideas for how the company could save to reduce costs?

GO ONLINE

Lesson 6-6

Learn

Emily takes her bike 2.3 miles to school each day. How far does Emily take her bike to school each day?

Check Stop: Use decimal grids.

2.3×2.3

Use 100 squares to represent 2.3×2.3 . Shade the squares to represent each step.

Attend to: Why did you use 100 squares? (representing 10 by 10 grid)

$2.3 \times 2.3 = 0.2 \times 2 + 0.2 \times 0.3 + 0.3 \times 0.2 + 0.3 \times 0.3$

$= 0.4 + 0.06 + 0.06 + 0.09$

$= 0.4 + 0.12 + 0.09$

$= 0.61$

Check Stop: Explain why you used 100 squares to multiply decimals. Look at the hundreds to determine the most efficient strategy.

Work Together: Check students' explanations.

Answers could vary but should be based on 2.3×2.3 .

What other strategy can you use to solve this problem?

$2 \times 2 = 4$	$0.3 \times 0.3 = 0.09$
$0.2 \times 2 = 0.4$	$0.3 \times 0.2 = 0.06$

1 Pose the Problem

Pose Purposeful Questions

- What strategies can you use to solve the problem?
- In what ways can you model this problem?

2 Develop the Math

Choose the option that best meets your instructional goals.

Stronger and Clearer Each Time

Pair students and give them a multiplication problem. Have them individually write sentences explaining the strategies that can be used to solve the problem. Then have them share their writing with their partner and compare and contrast the strategies they wrote about, choosing by the end of their discussion which strategy they think is the most efficient and why.

3 Bring It Together

Elicit and Use Evidence of Student Thinking

- What do you consider when deciding on a strategy to use to solve a real-world problem involving products of decimals?

Key Takeaway

- Any of the multiplication strategies that students already know can be used to determine a product.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of using an area model to find the product of a real-world problem involving decimals.

Common Misconception: Students may struggle to find other ways to show this product. Tell them that they could use a set of 12 decimal grids in 4 rows of 3 and shade squares as in the earlier example.

Language of Math

The word *strategy* is from the Greek word *stratēgia*, meaning "generalship," or "the skill or practice of exercising military command." Mathematical strategies are skills or practices allow us to exercise command over problem-solving.

Activity-Based Exploration

Students explain strategies used for solving real-world problems involving decimal products.

Materials: *Show and Explain Your Strategies* Teaching Resource

Directions: Provide copies of the *Show and Explain Your Strategies* Teaching Resource. Have students work together to solve the Pose the Problem. Encourage students to solve using more than one strategy.

Support Productive Struggle

- Which strategies or models may be used to solve?
- How did you determine which strategy to use to solve this problem?
- Do you think one strategy is more efficient than another? Explain why.
- Give an example of a multiplication problem that would be most efficient using a representation. An area model? Using patterns in the placement of the decimal?

Math is... exploring

- Why is it useful to know more than one strategy to solve a problem?

Students strive to understand multiple approaches to problems.

Activity Debrief: Have groups share and compare their strategies for solving. Discuss similarities and differences between the strategies.

A PDF of the Teaching Resource is available in the Digital Teacher Center.



English Learner Scaffolds

Entering/Emerging Support students in understanding the term *efficient* by completing a task first in an efficient way, and then in an inefficient way. For example, move from point A to point B using the shortest path. Say *This is an efficient way to [get to the door]*. Repeat, this time in an inefficient manner and say *This is not an efficient way to [get to the door]*. Use another example, and ask, *Is this an efficient way to [get to the desk]*?

Developing/Expanding Support students in understanding the term *efficient* by completing a task first in an efficient way, and then in an inefficient way. For example, move from point A to point B using the shortest path. Say *This is an efficient way to [get to the door]*. Repeat, this time in an inefficient manner, and say *This is not an efficient way to [get to the door]*. Ask students use another example, and using the word *efficient*.

Bridging/Reaching Ask students to discuss which patterns they find most efficient for solving the problem. Allow students to interject, pointing out any mistakes that they may catch in meaning or understanding. For example, *No, I disagree because...* or *No, that's not an efficient way because...*

Guided Exploration

Students consider which strategy they would use to solve a real-world problem involving decimal products.

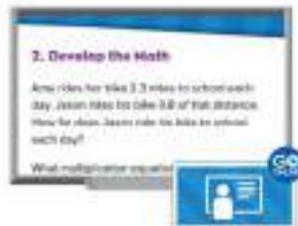
Facilitate Meaningful Mathematical Discourse

- Have the students estimate the solution. Ask:
 - What factors will you use to estimate the solution? Why?
- Have students share strategies to determine the total number of squares in the overlapping shaded region. Ask:
 - How can you explain how your strategy works?
 - How can you explain how someone else's strategy worked?
 - How does the decimal grid represent the problem?
- Have students use the fact $23 \times 8 = 184$ and patterns based on place value concepts and properties of operations to solve the problem. Ask:
 - How many places to the right did each digit in 23 move?
 - How many places to the right did each digit in 8 move?
 - How many places to the right should each digit in 184 move?
 - Use your estimate to assess the reasonableness of your calculated solution. Is your calculated solution reasonable? Why or why not?
- **Think About It:** Which strategies would be less efficient for solving $2.3 \times 0.8 = d$?

Math is... exploring

- Why is it useful to know more than one strategy to solve a problem?

Students strive to understand multiple approaches to problems.



On My Own

Name _____

What is the product? Explain the strategy you used to solve. **Check students' explanations.**

1. $1.8 \times 0.7 = 1.26$ **1.26**

2. $3.5 \times 3.7 = 12.95$ **12.95**

3. Each bottle holds the same amount when full. How much water can the bottles hold? **3.25 L**

4. Estimate the show tickets for the same night show each night. How many tickets can you sell? **6.88 m**

5. Cooper's recommendation says you have 4.7 grams of potassium per day. Last week, Wilson recommended 3.8 grams as much potassium as the recommendation says each potassium pill. How many pills each day does he need? **4.23 g**

6. 4 protein bars in quantity of 3.8 bars. A protein bar is usually 3.2 grams. What is the quantity of the order? **35.88 L**

Notes: Explain the strategy used to solve:

1. Area of a bag of apples. Each apple weighs 0.4 pound on average. There are 7 apples in the bag. What is the total weight of the apples? **6.8 pounds; Sample explanation: $10 \times 0.4 = 4.0$, $7 \times 0.4 = 2.8$, $4 + 2.8 = 6.8$**

2. Lately, some cars that fuel by alcohol use 0.7 gallon of gasoline per day in every gallon of daily miles. John manages 50 6-gallon cars. How much gasoline does he use?

40.6 gallons; $50 \times 0.7 = 35$, $5 \times 0.7 = 3.5$, $35 + 3.5 = 40.6$

3. Ania took five bags of 2.8 items per bag and 2.7 items for an hour. How many items did she take for the hour?

34.9 items; $7 \times 2 = 14$, $7 \times 0.2 = 0.2$, $0.2 \times 5 = 1$, $0.8 \times 0.7 = 0.56$, $2.7 + 0.7 + 2.4 + 0.56 = 24.36$

4. **11.66 Grams** Mrs. Lee bought 1.5 kg of apples that cost \$0.75 per kg. She also bought 2 kg of oranges that cost \$0.59 per kg. How much did she pay for the apples? Explain how you solved the problem.

0.388 kg; I can use the area model to show the 2 partial products and then add the partial products.

5. Carol buys 3.5 pounds of potatoes. The store charges \$0.62 per pound of potatoes. How much does Carol pay for the potatoes? Explain how you solved the problem.

\$2.17; Sample explanation: I used decimal grids to show the factors as 35 columns and 6 rows in 4 grids, and the product as the area 2.10.

6. **Extend Your Thinking** How many decimal places do you think are in the product of $1.2 \times 1.8 \times 0.7$? Write a strategy you used to solve the problem. Multiply to check your prediction.

Sample answer: 4 decimal places; I used place-value patterns to make my prediction; calculated solution is 0.594

Reflect

How did I show my understanding when explaining how to multiply decimals?

Answer may vary.

How do I show my understanding when explaining how to multiply decimals?

Answer may vary.

Practice

Build Procedural Fluency from Conceptual Understanding

Common Error: Exercises 1–11 Students may make place value errors when multiplying decimals. Suggest that they estimate the products first.

Practice Item Analysis

Item	DOK	Rigor
1–2	1	Procedural Skill and Fluency
3–11	2	Application
12	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How did I think like a mathematician when explaining how to multiply decimals?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you show others that you value their ideas?

Students reflected on how they practiced social awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain why I chose a strategy to solve multiplication equations involving decimals.
- I can understand other strategies to solve multiplication equations involving decimals.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Explain strategies to multiply decimals	5.NBT.B.7
2	2	Explain strategies to multiply decimals	5.NBT.B.7
3	2	Explain strategies to multiply decimals	5.NBT.B.7

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the U or P activities
2 of 3	<i>Take Another Look</i> or any of the U activities
1 or fewer of 3	Small Group Intervention or any of the P activities

Key for Differentiation

- P** Reinforce Understanding
- U** Build Proficiency
- I** Extend Thinking



Lesson 6-6
Exit Ticket

Answer

What is the product? Use a multiplication strategy to solve.

- Abel's printing plant has a capacity of 5.2 tons. The factory that is using has a capacity 22.5 times greater. What is the capacity of the factory?

112.5 tons
- Each book is 75 cents more than the last. How many of these books will he need to make it back from going to Atlanta's?

67.5 are
- All the eggs in each basket weigh 0.025 pounds. Each basket has 250 of these eggs. How much do all the eggs weigh?

125.00

Reflect On Your Learning:

I do not understand
 I am still learning
 I understand
 I understand completely

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R Reinforce Understanding

SMALL GROUP

Apply It!

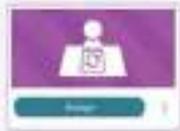
Work with students in small groups. Provide students with decimal grids that represents a decimal product such as 4.2×0.9 or 1.1×2.7 . Each student writes the multiplication equation that goes with the decimal grids and a real-world problem that matches the model. Help students use strategies for finding each product. Students then present the decimal grids, equation, and problem to the group.

GO ONLINE

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Multiply Decimal Numbers (Area Model)
- Multiply Decimal Numbers (Patterns)



INDEPENDENT WORK

Differentiation Resource Book, p. 61

Lesson 9-6 • Reinforce Understanding
Explain Strategies to Multiply Decimals

Review
 You can use a variety of strategies including decimal grids, area models, and partial products to multiply decimals. Don't be afraid to try more than one strategy!

Solve each problem. Explain the strategy you use.

1. The cost of almonds is 4 dollars per pound. How much do 2.5 pounds of almonds cost? *Sample answer: grid.*
 $4.00 \times 2.5 = 10.00$
 $4.00 \times 2 = 8.00$
 $4.00 \times 0.5 = 2.00$
 $8.00 + 2.00 = 10.00$

2. A box of cereal costs \$7.99. How much do 3 boxes of cereal cost?
 $7.99 \times 3 = 23.97$
 $7.99 \times 3 = 23.97$

3. A box of cereal costs \$7.99. How much do 3 boxes of cereal cost?
 $7.99 \times 3 = 23.97$
 $7.99 \times 3 = 23.97$

B Build Proficiency

WORKSTATIONS

Practice It! Game Station
Related Decimal Multiplication Task Cards

Students practice decimal multiplication using patterns.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



Student Practice Book, pp. 61–62

Lesson 9-6
Additional Practice

Review
 You can use different methods to multiply decimals.

Use a decimal grid to solve: $0.7 \times 2.4 = ?$
 Partial Products:
 $0.7 \times 2 = 1.40$
 $0.7 \times 0.4 = 0.28$
 $1.40 + 0.28 = 1.68$

Use an area model and partial products to solve 0.8×0.3 .

What is the product?
 $0.8 \times 0.3 = 0.24$



Extend Thinking

Use It! Application Station

Rock Garden Students use metric measurements to create a model of a rock garden.



WORKSTATIONS

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with multiplication of multi-digit numbers.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



GO ONLINE

Student Practice Book, pp. 61–62

Solve each problem. Explain the strategy used to solve.

- Write each number in standard form. Write the number in words. Write the number in expanded form.

3.4 million; Sample answer: 1 zeroed decimal grid and about 3 groups of 9 tenths to show 2 whole grids and 4 tenths of another.
- 88 pages 4.6 miles on Saturday. On Monday, he rode 33 of the miles. How many miles did he ride on Monday?

3.88 miles; Sample answer: I used partial products: $8 \times 0.6 = 4.8$ and $0.8 \times 0.6 = 0.48$, then $4.8 + 0.48 = 5.28$.
- 8 rectangular picture frames measure 2.1 feet long and 1.2 feet wide. What is the perimeter in inches of the frames?

4.96 square feet; Sample answer: I used an area model and partial products: $2 \times 1 = 2$, $2 \times 0.6 = 1.2$, $0.6 \times 2 = 1.2$ and $0.6 \times 0.6 = 0.36$, then $2 + 1.2 + 0.6 + 0.36 = 4.16$.
- Each of the 4 bags of oranges weighs about 3.3 pounds. Sam's best friend had 14 oranges. How many pounds of oranges weigh?

about 4.2 pounds; Sample answer: I used partial products: $0.3 \times 14 = 4.2$ and $0.3 \times 4 = 1.2$, then $3 + 1.2 = 4.2$.
- 8 rectangular geometric garden measures 44 meters long and 1.2 meters wide. What is the area of this region in square meters?

52.8 square meters; Sample answer: I used an area model and partial products: $40 \times 1 = 40$, $40 \times 0.2 = 8$, $4 \times 1 = 4$ and $4 \times 0.2 = 0.8$, then $40 + 8 + 4 + 0.8 = 52.8$.

Math in Motion Activity

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INDEPENDENT WORK

Differentiation Resource Book, p. 62

Lesson 8-6 • Independent Thinking

Explain Strategies to Multiply Decimals

Answer

Numbers 1–6 are solutions to multiplication problems.

- $1.32 \times 0.4 = 0.528$ and $0.528 \div 0.4 = 1.32$
- $0.05 \times 0.2 = 0.01$ and $0.01 \div 0.2 = 0.05$
- $0.22 \times 0.3 = 0.066$ and $0.066 \div 0.3 = 0.22$
- $0.15 \times 0.4 = 0.06$ and $0.06 \div 0.4 = 0.15$

Match each problem (A–C) to its solution above (1–6).

A. 0.15×0.4	B. 0.22×0.3	C. 0.05×0.2
D.	E.	F.
G. 0.05×0.2	H. 0.22×0.3	I. 0.15×0.4
J. Explain how 5.2 pounds of oranges that cost \$0.25 a pound. How much does the basket weigh?	K. A teacher has a batch of balls, each 3.6 inches in size. How much flour is needed to make 2 batches?	L. Student says: 96 fishing boats. Each boat costs \$0.05. How much does the school need to pay?

Differentiation Resource Book

Unit Review

Unit Review Name _____

Vocabulary Review

Choose the correct word(s) to complete the sentence.

estimate partial products
 quotient range

- To find the quotient, you can use a **partial product**.
- When multiplying powers of 10, the **quotient** tells us the number of places the digits shift to the left.
- Any **range** gives two numbers between which all possible answers fall.
- When using an area model to multiply, the product is the **partial products**.

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Review

- Which is equivalent to 35×10^3 ?
 - 35
 - 300
 - 3,500**
 - 35,000
- Which number is represented by the 1000's place?
 
 - $500 \times 100 = 50,000$
 - $50 \times 100 = 5,000$
 - $4 \times 1,000 = 4,000$**
 - $4 \times 100 = 400$
- What two numbers are equivalent to 12×40 ?
 - $12 \times 40 = 2,240$
 - $12 \times 40 = 204$
 - $12 \times 40 = 20,40$
 - $12 \times 40 = 480$**
- Use a grid to find the product. Then use 7 parts to the product. How many hundreds does 12×40 have?
 - 56 hundreds
- Which is equivalent to $1,000 \times 10^3$?
 - 100
 - 100,000
 - 10,000
 - 100,000,000
- Which number is represented by the 100's place?
 
 - $500 \times 100 = 50,000$
 - $50 \times 100 = 5,000$
 - $4 \times 1,000 = 4,000$**
 - $4 \times 100 = 400$
- What two numbers are equivalent to 12×40 ?
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 - 100
 - 100,000
 - 10,000
 - 100,000,000
- Which number is represented by the 100's place?
 
 - $500 \times 100 = 50,000$
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 - $4 \times 1,000 = 4,000$**
 - $4 \times 100 = 400$
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 - $12 \times 40 = 20,40$
 - $12 \times 40 = 480$**
- Use a grid to find the product. Then use 7 parts to the product. How many hundreds does 12×40 have?
 - 56 hundreds

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Students can complete the **Unit Review** to prepare for the **Unit Assessment**. Students may complete the Review in their Interactive eBook in the Digital Students Center.

Vocabulary Review

Item Analysis

Item	Lesson
1	6-2
2	6-1
3	6-2
4	6-4

Review

Item Analysis

Item	DOK	Lesson	Standard
5	1	6-1	5.NBT.A.2
6	1	6-3	5.NBT.B.7
7	1	6-5	5.NBT.B.7
8	2	6-2	5.NBT.B.7
9	2	6-6	5.NBT.B.7
10	1	6-1	5.NBT.A.2
11	2	6-4	5.NBT.B.7
12	2	6-6	5.NBT.B.7

To review the lessons in this unit, have students watch the Math Replay video in their Digital Student Center.

Assign the Unit Review practice to students from the Digital Teacher Center.



Item Analysis (continued)

Item	DOK	Lesson	Standard
13	2	6-2	5.NBT.B.7
14	1	6-4	5.NBT.B.7
15	2	6-3	5.NBT.B.7
16	1	6-1	5.NBT.A.2
17	1	6-5	5.NBT.B.7
18	1	6-5	5.NBT.B.7
19	1	6-4	5.NBT.B.7

13. Keller has a battery that weighs 50 grams. His other has a bigger battery that weighs 75 grams. How many grams more does the bigger battery weigh?
 The bigger battery is **25** grams more.

14. Find the product.
 $32 \times 17 = \mathbf{544}$

15. Elizabeth's 22 boxes each ship to schools. Which model shows how the markers in 3 boxes?
 A. B. C. D.

16. Choose a product of 37 x 25.
 A. 3 x 25
 B. 37 x 25
 C. 37 x 5
 D. 37 x 2

17. Use partial products to find the product of 37 x 25.
 $3 \times 25 = 75$
 $37 \times 2 = 74$
 So, $37 \times 25 = 929$

18. She worked 2.5 hours for 6.0 hours and 2 weeks for $\frac{50}{8}$ hours, she would make exactly \$300.
 $6 \times 2 = 12$
 $37 \times 2 = 74$
 So, $37 \times 25 = 929$

Performance Task

Standards: 5.NBT.A.2, 5.NBT.B.7

Rubric (4 points)

Part A (DOK 2) – 2 points

2 POINTS Student's work reflects a proficiency with decimal multiplication. The solution shows a reasonable solution.

1 POINTS Student's work reflects developing proficiency with decimal multiplication. The solution is not reasonable due to computational errors.

0 POINTS Student's work reflects a poor understanding of decimal multiplication. The solution is not reasonable.

Part B (DOK 2) – 2 points

2 POINTS Student's work reflects a proficiency with decimal multiplication. The solution is accurate.

1 POINTS Student's work reflects developing proficiency with decimal multiplication. The solution is incorrect due to computational errors, not conceptual weakness.

0 POINTS Student's work reflects a poor understanding of decimal multiplication. The solution is incorrect.

Performance Task
 Carter worked with a partner to find prices for books. She is paid \$120 for each hour of work. Last week, she worked 2.5 hours.
Part A: She can work for 2.5 hours for \$300 or more in a month.
Sample answer: If she worked 2 weeks for 6.0 hours and 2 weeks for $\frac{50}{8}$ hours, she would make exactly \$300.
Part B: How many hours did she work? She paid for 2.5 hours.
 $50 \times 2 = 100$

Reflect
 How can I improve myself?
 Answers may vary.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

Unit 6
Fluency Practice
Name _____

Fluency Strategy

You can choose a strategy to subtract. You can adjust the numbers, rearrange the starting numbers, or use an algorithm.

Adjust the numbers. $8,710 - 6,738$

$$\begin{array}{r} 8,710 \\ - 6,738 \\ \hline 1,972 \end{array}$$

$$8,730 - 5,400 = 3,330$$

6. Adjust the numbers to find the difference.

$$\begin{array}{r} 3,978 \\ - 1,700 \\ \hline 2,278 \end{array}$$

Fluency Flash

What is the difference?

8.

Tens	Ones	Tens	Ones
5	3	8	0
1	0	7	2
4	2	1	8

9.

Tens	Ones	Tens	Ones
2	8	1	8
1	0	5	7
4	5	0	0

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Fluency Check

What is the sum or difference?

A. $3,028 + 242 = 3,270$

B. $812 - 275 = 537$

C. $450 + 24 = 474$

D. $305 + 28 = 333$

E. $795 + 28 = 823$

F. $824 - 21 = 803$

G. $342 - 450 = -108$

H. $524 + 91 = 615$

I. $3,028 + 312 = 3,340$

J. $1,007 - 328 = 679$

Fluency Talk

How do you decide when to use adjusting or an algorithm to subtract?

Explanations may vary.

How many representations of a hundred did it require to subtract?

Explanations may vary.

Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students choose a strategy to subtract.

Fluency Progression

Unit	Skill
1	Use Partial Sums to Add
2	Decompose by Place Value to Subtract
3	Use an Algorithm to Add
4	Use an Algorithm to Subtract
5	Choose a Strategy to Add
6	Choose a Strategy to Subtract
7	Multiply by Multiples of 10
8	Multiply by Multiples of 100
9	Divide Multiples of 10
10	Divide Multiples of 100
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)
13	Choose a Strategy to Multiply
14	Choose a Strategy to Multiply

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Unit Assessments

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

Data When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support	Intervention Lesson	Standard
1	2	6-1		Multiply by Powers of 10 (Decimal Point)	5.NBT.A.2
2	2	6-1		Multiply by Powers of 10 (Decimal Point)	5.NBT.A.2
3	2	6-2		Estimate Products (Decimal Number Factors)	5.NBT.B.7
4	2	6-1		Multiply by Powers of 10 (Decimal Point)	5.NBT.A.2
5	2	6-4		Multiply Decimal Numbers (Area Model)	5.NBT.B.7
6	2	6-3		Multiply Two Decimal Numbers-Model	5.NBT.B.7
7	2	6-3		Multiply Decimals by Whole Numbers-Model	5.NBT.B.7
8	2	6-4		Multiply Decimal Numbers (Area Model)	5.NBT.B.7
9	2	6-5		Multiply Decimal Numbers (Patterns)	5.NBT.B.7
10	2	6-5		Multiply Decimal Numbers (Patterns)	5.NBT.B.7
11	2	6-2		Estimate Products (Decimal Number Factors)	5.NBT.B.7
12	2	6-5		Multiply Decimal Numbers (Patterns)	5.NBT.B.7
13	3	6-6		Multiply Decimal Numbers (Patterns)	5.NBT.B.7
14	3	6-6		Multiply Decimal Numbers (Patterns)	5.NBT.B.7
15	2	6-2		Estimate Products (Decimal Number Factors)	5.NBT.B.7

Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 6
Unit Assessment, Form A

Name: _____

1. What of these are equivalent to 1.8×10^4 (Choose all that apply.)

A. 1.8×10^4

B. 1.8×10^3

C. 180

D. 18,000

2. Knowing that $8 \times 10^2 = 800$, what is 8.2×10^3 ?

A. 80

B. 8,200

C. 820

D. 81,000

3. A company sells fuel for \$3.00 per gallon. About how much would it cost to buy a bag of fuel that weighs 3 pounds?

about \$3.00

4. According to her step counter, Jordan walked 18,000 steps yesterday. How many steps did Jordan walk yesterday?

A. 180 steps

B. 18,000 steps

C. 1,800 steps

D. 180,000 steps

5. What unit is equivalent to 4.2×10^2 ?

A. 420

B. 42

C. 28

D. 2,800

Assessment Resource Book 181

6. Which number is represented by the decimal grid?

A. $0.27 \times 100 = 27$

B. $7 \times 0.4 = 2.8$

C. $0.7 \times 0.4 = 0.28$

D. $0.7 \times 0.4 = 0.28$

7. A grocery store sells 200 pounds of berries on each cart. How much berries will the store need to make 5 cartons? (Use the decimal grid to help you solve.)

0.84 pounds

8. A rectangular storage space is 2.4 meters wide and 12 meters long. What is the area of the storage space? Use the area model to label.

	10	+	2	
2	$2 \times 10 = 20$		$2 \times 2 = 4$	
0.4	$0.4 \times 10 = 4$		$0.4 \times 2 = 0.8$	

28.2 square meters

Assessment Resource Book

Divide Whole Numbers

PACING: 11 days

LESSON	MATH OBJECTIVE	LANGUAGE OBJECTIVE	SOCIAL AND EMOTIONAL LEARNING OBJECTIVE
Unit Opener  Division Puzzles	Solve 3 by 3 number puzzles using division facts.		
7-1 Division Patterns with Multi-Digit Numbers	Students use place-value patterns and basic facts to divide a whole number by a multiple of 10.	Students talk about how to use place-value patterns and basic facts to divide a whole number by a multiple of 10 using the modal verb <i>can</i> .	Students recognize personal strengths through thoughtful self-reflection.
7-2 Estimate Quotients	Students estimate quotients of multi-digit numbers using the same strategies used to estimate quotients of lesser numbers. Students use estimated quotients to make predictions about a calculated solution. Students use estimated quotients to assess the reasonableness of a calculated solution.	Students talk about estimating quotients, using the terms <i>greater than</i> , <i>less than</i> , and <i>about</i> .	Students set learning goals and initiate work on tasks to accomplish their goals.
7-3 Relate Multiplication and Division of Multi-Digit Numbers	Students use the relationship between multiplication and division to determine the quotient of multi-digit numbers.	Students describe the relationship between multiplication and division that helps them to find the quotient when dividing by a multiple of 10 using the verb <i>determine</i> and the adjectives <i>same</i> and <i>different</i> .	Students collaborate with peers and contribute to group effort to achieve a collective and mathematical goal.
7-4 Represent Division of 2-Digit Divisors	Students use an area model to determine partial quotients and add partial quotients to calculate the quotient.	Students explain how to use an area model to determine and add partial quotients using comparatives <i>more useful</i> , <i>less useful</i> , <i>more helpful</i> , and <i>less helpful</i> .	Students discuss how a rule or routine can help develop mathematical skills and knowledge and be responsible contributors.
7-5 Use Partial Quotients to Divide	Students record partial quotients using an algorithm.	Students discuss recording partial quotients while using the verb <i>relate</i> .	Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing thoughtful and constructive feedback.
7-6 Divide Multi-Digit Whole Numbers	Students solve division problems using partial quotients, which sometimes include remainders.	Students explain how to solve division problems using partial quotients, which sometimes include remainders, using <i>If... then</i> .	Students set a focused mathematical goal and make a plan for achieving that goal.
7-7 Solve Problems Involving Division	Students solve word problems involving division. Students interpret the remainder, when necessary, to solve problems.	Students talk about solving word problems involving division while using the modals <i>can</i> and <i>could</i> .	Students break down a situation to identify the problem at hand.
Math Probe Solving Division Word Problems Solve a division word problem.			
Unit Review			
Fluency Practice			
Unit Assessment			
Performance Task			

FOCUS QUESTION:
How can I divide
multi-digit numbers?

LESSON	KEY VOCABULARY		MATERIALS TO GATHER		RIGOR FOCUS	STANDARD
7-1	Math Terms	Academic Terms	<ul style="list-style-type: none"> • base-ten blocks • index cards 	<ul style="list-style-type: none"> • number cubes 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
	dividend divisor quotient	accurate evaluate				
7-2	estimate	suggest variation	<ul style="list-style-type: none"> • digit cards 		Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
7-3	dividend divisor	analyze establish	<ul style="list-style-type: none"> • base-ten blocks 	<ul style="list-style-type: none"> • number cubes 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
7-4	partial quotient	reflect speculate	<ul style="list-style-type: none"> • base-ten blocks 	<ul style="list-style-type: none"> • calculators 	Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
7-5	partial quotient	condition drawback	<ul style="list-style-type: none"> • <i>Blank Partial Quotients</i> Teaching Resource 		Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
7-6	partial quotient remainder	address advantage	<ul style="list-style-type: none"> • base-ten blocks 		Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6
7-7	remainder	note transition			Conceptual Understanding, Procedural Skill & Fluency	5.NBT.B.6

Unit Overview

Focus

Dividing Multi-Digit Whole Numbers

In this unit, students build on their understanding of multiplication and division from Grade 4. Students have previously worked with division of up to four-digit dividends and one-digit divisors, including situations involving remainders. They continue to use equations, rectangular arrays, and area models to extend their knowledge of division to include up to four-digit dividends and two-digit divisors. They use estimation techniques to determine the reasonableness of solutions.

Students apply their understanding of dividing multi-digit whole numbers to solve problems in real-world contexts.

When possible, students use area models to represent and solve a problem. By reasoning with the blocks for multiple cases, they develop a general process for approaching problems, which they know as the *partial quotients algorithm*.

Students discover that place value and division strategies work the same way with multi-digit whole number divisors as they do with division by one-digit divisors.

- **Use place-value patterns:** Students can identify and use place-value patterns to divide multi-digit whole numbers.
- **Use models:** Students use models to represent division problems and relate the problem to multiplication. They use their understanding of place-value and multiplication to decompose an area model by factors and use partial quotients to identify the quotient.
- **Solve word problems:** Students use their understanding of equations and models to solve word problems involving division.

Coherence

What Students Have Learned

- Students divided 4-digit dividends by 1-digit divisors and made sense of remainders. (Grade 4)
- Students used partial-quotient strategies to divide multi-digit numbers with single-digit divisors. (Grade 4)
- Students illustrated and explained calculations using equations, rectangular arrays, and/or area models. (Grade 4)

What Students Are Learning

- Students use strategies based on place value to divide multi-digit whole numbers.
- Students estimate quotients of multi-digit whole numbers.
- Student use partial quotients and the standard algorithm to divide multi-digit whole numbers.
- Students solve real-world division problems with multi-digit whole numbers.

What Students Will Learn

- Students fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of division by using place value patterns to calculate quotients.
- Students build their understanding of multiplication and division using basic facts to divide multi-digit numbers.
- Students build on their understanding of division as they begin to divide with 2-digit divisors using area models and partial quotients.

Procedural Skill and Fluency

- Students develop proficiency with dividing whole numbers by multiples of 10.
- Students use estimation strategies to begin to build proficiency with division.
- Students build proficiency with multi-digit division using basic multiplication facts.
- Students build proficiency by using area models and partial quotients to represent division with or without remainders.

Application

- Students apply estimated quotients to successfully solve contextual, real-world problems.
- Students apply their understanding of dividing multi-digit whole numbers to solve problems with real-world contexts.

Application is not a targeted element of rigor for this standard.

Effective Teaching Practices

Build Procedural Fluency from Conceptual Understanding

Procedural fluency is the ability to perform mathematics tasks flexibly, efficiently, and accurately. A common misconception is that math is about knowing mathematical procedures. However, math begins with concepts, and procedures are just tools for applying them.

Conceptual understanding is best achieved by way of exploration, discovery, and making connections to prior knowledge. In this way, learning is more meaningful and interesting to students than mere memorization of procedures. When a student's knowledge is built on conceptual understanding, they can more readily reason through new situations. It is important for students to develop strategic thinking and the ability to find a course of action specific to the situation at hand.

This unit involves computation. Be sure instruction makes strong connections to conceptual understanding.

- Have students recognize that it doesn't matter if they don't maximize the number (of thousands, hundreds, and so on) that they distribute at each step of the algorithm. The result will be the same in the end despite the increased number of steps.
- Ask students to make connections to the area models and to whether they are finding the number of groups or the size of each group.
- It might be cumbersome to represent 4-digit numbers and the division process with area models, but it is a useful step in building the conceptual understanding that will support students' work with the algorithm and vertical format. Consider using smaller numbers if time or availability of materials is an issue.
- Have students spend time explaining connections.

Math Practices and Processes

Attend to Precision

Attending to precision refers to any action or habit of being accurate, clear, and on point. For example, when students attend to precision, they use care in computations and check their answers, pay attention to units while reasoning about problems, use the clearest possible language to explain ideas, label representations accurately to connect them to the quantities and relationships in problems. Teachers help students develop the habit of attending to precision by being accurate themselves in their discussions and by requiring it of them in all discourse and classroom activity.

To help students develop the habit of attending to precision, assign tasks that require precision and set clear expectations and have students think purposefully about precision in their work and discourse.

For example:

- Have students discuss how they estimate quotients using rounding and compatible numbers. Have them recognize and talk about how estimation is connected to the idea of precision and accuracy.
- Have students talk about their area models and connect them to place value concepts using appropriate and precise language.
- Have students describe the units of the quotient and any remainder that results. Have them explain why the context affects the units of the quotient.

Social and Emotional Learning

- **Self-Awareness – Recognize Strengths** (Lesson 7-1): When students recognize their own strengths, they can see themselves as resourceful and may be more willing to attempt to problem solve and help others.
- **Self-Management – Self-Motivation** (Lesson 7-2): Students who self-motivate can take initiative and persevere through challenging tasks.
- **Relationship Skills – Teamwork** (Lesson 7-3): When students work effectively as a team, they establish a stronger learning community.
- **Responsible Decision-Making – Ethical Responsibility** (Lesson 7-4): Understanding rules and routines of the classroom environment can help students be responsible contributors to the learning community.
- **Social Awareness – Respect Others** (Lesson 7-5): When students are respectful of one another, they strengthen their class community.
- **Self-Management – Goal Setting** (Lesson 7-6): Setting goals can help motivate students to take initiative and stay focused.
- **Responsible Decision-Making – Identify Problems** (Lesson 7-7): A key step in problem solving is analyzing information to identify the task.

Unit Overview

Language of Math

Vocabulary

Students will be using these key terms in this unit.

- **Dividend** – (Lesson 7-1): Students were introduced to this term in the context of division fluency. It is the number that gets divided in a division problem.
- **Divisor** – (Lesson 7-1): Students were introduced to this term in the context of division fluency. It is the number that divides another number in a division problem.
- **Quotient** – (Lesson 7-1): Students were introduced to this term in the context of division. This is the result of dividing one number by another number.
- **Estimate** – (Lesson 7-2): Students were introduced to this term in the context of solving word problems involving all four operations. Have students discuss how estimation can help them evaluate the reasonableness of a solution.
- **Partial quotient** – (Lesson 7-4): Students were introduced to this term with the strategy of breaking a dividend into parts and dividing each part by the divisor separately. Each separate quotient generated by this process is called a partial quotient. The total quotient is the sum of the partial quotients. The process is called the partial quotients algorithm. Students use the process repeatedly throughout the unit and refer to it simply as using partial quotients.
- **Remainder** – (Lesson 7-6): Students were introduced to this term in the context of division strategies. A remainder is an amount left over after one whole number is divided by another.

Math Language Development

A Focus on Listening

We start learning our first language by listening. At an early age we are able to begin connecting what we hear with what is happening around us and with how others are interacting with us. Listening to a fluent speaker is the most efficient way to start learning our first language.

Similarly, our earliest encounters with math most likely involve listening. We recite the count sequence and learn to name shapes by listening to and copying a fluent speaker.

Instruction in the math classroom should include plenty of speaking and listening. Such discourse engages students—with you and with each other. It promotes thinking and shared learning. Speakers must dig into their thoughts and process their own understanding, and listeners must also dig into their thoughts as they process the speakers' ideas and compare them to their own.

Promote listening in the classroom by eliciting responses from students during whole-class discussions. Responses may be written or spoken.

The purpose is simply to promote listening. Also, engage students in discussions with each other and have them paraphrase and record each other's ideas.

- Have students work in pairs. Give them quotients to estimate—including problems for which both rounding and compatible numbers can be used. Students take turns explaining estimates to each other. The listener makes the estimate as described by the speaker and explains the process back to the speaker.
- For a chosen division problem, explain to the class your process for finding the quotient using an area model. Have students write a description of the process.
- Have students explain the reasoning they use to determine the units of a quotient. One student explains the case of the quotient being the number of groups, and the other explains the case of the quotient being the size of each group.

English Language Learner

In this unit, students are provided with a number of scaffolds to support their comprehension of the language used to present and explain strategies related to dividing whole numbers. Because many of the words (*needed, hold, solution, none, saved*) and phrases (*as much, as great as, left over*) used in this unit could prove challenging to ELs, they are supported in understanding and using them so that the instruction is more accessible.

Lesson 7-1 – (*10 ×, etc.*) *as much*
Lesson 7-2 – *needed*
Lesson 7-3 – *hold*
Lesson 7-4 – *solution*
Lesson 7-5 – (*24 ×, etc.*) *as great as*
Lesson 7-6 – (*none*) *left over*
Lesson 7-7 – *saved*

Unit Routines

Number Routines

Build Fluency The number routines found at the beginning of each lesson help students build number sense and operational fluency. They also help students develop the thinking habits of mind that are important for proficient doers of math.

Where Does It Go?

Purpose: Build estimating skills using benchmarks.

Overview: Students place a target number on number lines with different endpoints and justify their placement. In some instances, as a challenge, the target number may not actually belong on one of the number lines.

Which Benchmark Is It Closest To?

Purpose: Enhance rounding and reasoning skills.

Overview: Students determine to which benchmark the given number is closest and explain their reasoning.

Find the Pattern, Make a Pattern

Purpose: Build efficiency with recognizing and building patterns.

Overview: Students determine the rule(s) for a given pattern, then use the rule(s) to create a new pattern. The teacher records students' new patterns and facilitates a discussion to validate the pattern and its rules.

Decompose It

Purpose: Build flexibility with numbers.

Overview: Students generate multiple (at least 3) ways to decompose given numbers and share their thinking for each decomposition. The teacher records decompositions and then facilitates a discussion of patterns in the decompositions.

Sense-Making Routines

- **Notice & Wonder: What question could you ask?** (Lesson 7-1) Students are presented with images of grouped items. Students might ask about the total number of items, the number of groups of items, or the number of items in each group.
- **Notice & Wonder: What do you notice? What do you wonder?** (Lessons 7-2 and 7-3) Students are presented with images of grouped items. Students might notice the objects are in groups and wonder about the total number of objects or the number of groups.
- **Notice & Wonder: Tell me everything you can.** (Lesson 7-4) Students are presented with a rectangular image with one dimension labeled. Students might ask about the parts or the whole area.

- **Numberless Word Problem** (Lessons 7-5 and 7-6) Students are given problems containing no numerical information, and asked to identify the math they see.
- **Numberless Word Problem** (Lesson 7-7) Students are presented with a situation in which no numerical information or question is provided, and asked to predict what the question could be.

Math Language Routines

The Mathematical Language Routines used in this unit give teachers a structured, yet adaptable format for amplifying and developing students' social and academic language. These routines can also be used as formative assessment opportunities as students develop proficiency in English and mathematical language. They can be used in ways that support real-time-, peer-, and self-assessment. For more information on the Math Language Routines, see the Appendix.

- Lesson 7-1 – Students participate in MLR8: Discussion Supports.
- Lesson 7-2 – Students participate in MLR7: Compare and Connect.

- Lesson 7-3 – Students participate in MLR2: Collect and Display.
- Lesson 7-4 – Students participate in MLR1: Stronger and Clearer Each Time.
- Lesson 7-5 – Students participate in MLR4: Information Gap.
- Lesson 7-6 – Students participate in MLR5: Co-Craft Questions and Problems.
- Lesson 7-7 – Students participate in MLR6: Three Reads.

100 3
How Ready Am I?

Name _____

1. What is the difference?
 $8,904 - 6,739$
 A. 1,637 B. 1,041
 C. 2,143 D. 2,341

2. What is the difference?
 $902 - 74$
 A. 91 B. 201
 C. 828 D. 97

3. What is the quotient of 2,400 ÷ 4?
 A. 4 B. 40
 C. 400 D. 4,000

4. When 2,432 is rounded to the nearest thousand?
 A. 2,000
 B. 3,000
 C. 1,000
 D. 3,500

5. A teacher has 48 crayons. She gives 10 crayons to each of 3 groups of students. How many crayons does each group get?
 A. 3 crayons B. 16 crayons
 C. 42 crayons D. 14 crayons

6. What is the quotient of 332 ÷ 3?
 A. 100.00 B. 110.67
 C. 10.67 D. 10.00

Answer Record Book

7. On the 225 students, the average math test score is 78. How many students are 95 or more?
 A. 0
 B. 1
 C. 2
 D. 3

8. Approximately 75 fishing boats are registered in a state. About how many boats are 100 feet or longer?
 A. 6 boats
 B. 7 boats
 C. 8 boats
 D. 9 boats

9. What is the product?
 369×3
 A. 279
 B. 648
 C. 234
 D. 27,798

10. What is the product?
 323×3
 A. 9,607
 B. 28,709
 C. 23,847
 D. 10,299

Answer Record Book

Administer the Readiness Diagnostic to determine your students' readiness for this unit.

Targeted Intervention

14 Use Guided Support intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK Skill		Guided Support Intervention Lesson	Standard
1	1	Subtract whole numbers	Subtract Multi-Digit Numbers	4.NBT.B.4
2	1	Subtract whole numbers	Subtract Multi-Digit Numbers	4.NBT.B.4
3	1	Division of 4-digit number by 1-digit number	Four-Digit Dividends (Area Models)	4.NBT.B.6
4	2	Rounding to the thousands	Round to Nearest 10, 100, or 1,000	4.NBT.A.3
5	2	Division as equal groups	Two-Digit Dividends (Partial Quotients)	4.NBT.B.6
6	2	Division of 3-digit number by 1-digit number with remainders	Three-Digit Dividends (Partial Quotients)	4.NBT.B.6
7	2	Interpret remainders in division	Interpret Remainders in Word Problems	4.OA.A.3
8	2	Interpret remainders in division	Interpret Remainders in Word Problems	4.OA.A.3
9	1	Multiply 3-digit number by 1-digit number	Multiply 3- by 1-Digit Numbers	5.NBT.B.5
10	1	Multiply 3-digit number by 2-digit number	Multiply 3- by 1-Digit Numbers	5.NBT.B.5

Assign the digital Readiness Diagnostic to students or download and print PDFs from the Digital Teacher Center.

GO ONLINE

Unit Opener

Focus Question

Introduce the Focus Question: *How can I divide multi-digit numbers?*

Ask students to think about what they know about division.

- What do you already know about division?
- What do you know about representing division?
- How does knowing multiplication facts help you divide?

Remind students that at the end of the unit, they will reflect back on what they learned in this unit.

Family Letter

Each letter presents an overview of the math in the unit and home activities to support student learning.

STEM in Action

Videos

Students can watch the two STEM videos.

STEM Career: Computer Programmer Grace talks about her aspirations to be a computer programmer.

Grace Designs a Game: Grace uses division to determine the length of a sports field in her computer game.

STEM Project Card

Students can complete the STEM project during their workstation time.

STEM Adventure

Students can complete the STEM Adventure during their workstation time.



STEM Career: Computer Programmer



Grace Designs a Game



Ignite!

Name: _____

Division Puzzles

5. Each row and column in this puzzle represents a division problem. Use clues provided to fill in the missing numbers in Puzzles A–E.

Puzzle A

56	8	7
14	2	1
8	8	1

Puzzle B

36	3	12
6	1	1
6	3	2

Puzzle C

12	12	6
3	3	3
3	6	2

Puzzle D

28	7	4
14	7	2
2	1	2

Puzzle E

100	10	10
5	5	1
30	3	10

Puzzle F

54	9	6
27	9	3
2	1	2

6. Show as many ways as you can to solve the division puzzle:

90	6	6
18	3	6
2	2	1

30	12	3
6	3	3
4	4	1

36	3	12
36	3	12
9	3	1

30	9	4
12	3	4
3	3	1

36	36	1
3	2	1
12	12	1

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Ignite!

Division Puzzles

Students use their knowledge of division and factors to solve the puzzles.

- Have students work in pairs to examine Figure 1 and share their thoughts.
 - **What do you notice about the numbers in Figure 1?**
- Encourage students to look for other division relationships in Figure 1. The class should conclude that each row and column (but not the diagonals) could represent a division problem.
- In Part 1, have students work in pairs to solve Puzzles A–E. Remind them that every row and column in Puzzles A–E represents a division equation as discussed for Figure 1. Advise students to check all computations before concluding that a puzzle is solved.
 - **How did you approach solving the puzzles?**
- Now have students draw attention to Part 2 at the bottom of the page. Have them find as many ways as they can to solve the puzzle.
 - **What patterns did you notice in your solutions?**

Extensions

- If you multiply the numbers in all nine squares in a puzzle by the same nonzero number, will the division puzzle still be valid? Explain.
- If you multiply the numbers in the four squares in the top left of a puzzle by the same nonzero number, will the division puzzle still be valid?

Unit Resources At-A-Glance

Workstations

Reveal Math offers rich and varied resources that teachers can use to differentiate and enrich students' instructional experiences with the unit content. The table presents an overview of the resources available for the unit with recommendations for when to use.

	Activity	Description	Use After Lesson	
Game Station		Students build proficiency with dividing multi-digit numbers by 2-digit numbers.		
		• Multi-Digit Division Tic Tac Toe	7-1	
		• Estimating Quotients Showdown	7-2	
		• Multi-Digit Division Tic Tac Toe	7-3	
		• Division with 2-Digit Divisors Task Cards	7-4	
		• Division with 2-Digit Divisors Race	7-5	
		• Remainder Showdown	7-6	
• Dividing with Remainders Bump	7-7			
Digital Station		Batting Practice Students add and subtract decimals.	7-1	
		Have students complete at least one of the Use It! activities for this unit.		
Application Station		STEM Project Card That Is Astronomical Students practice finding quotients, rounding, and writing equations by researching the hours in a day for each planet.	7-7	
			Connection Card Estimate High School Density Students research the density of schools in 10 U.S. states.	7-2
				Real World Card Online Learning: Is It Safe? Students write rules for safely using electronic devices and practice their rules by researching how to divide multi-digit numbers.

Additional Resources

Use the resources below to provide additional support for this unit.



Vocabulary

Use the vocabulary cards to help students learn the vocabulary in this unit. Encourage students to write their own definitions of the new terms on the front side of the card.



Foldables

Use the unit foldables with Lesson 7-5.



Spiral Review

Students can complete the Spiral Review at any point during the unit as either a paper-and-pencil or digital activity.

Lesson	Standard
7-1	5.MD.C.5
7-2	5.NBT.A.3
7-3	5.NBT.B.5
7-4	5.NBT.B.7
7-5	5.NBT.A.4
7-6	5.NBT.A.2
7-7	5.NBT.B.6

Division Patterns with Multi-Digit Numbers

Learning Targets

- I can explain patterns when dividing by a multiple of 10.
- I can use patterns to determine the quotient when dividing by a multiple of 10.

Standards

Major Supporting Additional

Content

- ◆ **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- ◆ **5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Math Practices and Processes

MPP Reason abstractly and quantitatively.

MPP Look for and make use of structure.

Vocabulary

Math Terms

dividend
divisor
quotient

Academic Terms

accurate
evaluate

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- index cards
- number cubes

Focus

Content Objective

- Students use place-value patterns and basic facts to divide a whole number by a multiple of 10.

Language Objectives

- Students talk about how to use place-value patterns and basic facts to divide a whole number by a multiple of 10 using the modal verb *can*.
- To support maximizing cognitive and linguistic meta-awareness, ELs participate in MLR8: Discussion Supports.

SEL Objective

- Students recognize personal strengths through thoughtful self-reflection.

Coherence

Previous

- Students found whole-number quotients and remainders with up to four-digit dividends and one-digit divisor (Grade 4).
- Students multiplied decimals to hundredths (Unit 6).

Now

- Students use place-value patterns to determine quotients when dividing by multiples of 10.

Next

- Students will use compatible numbers to estimate quotients (Lesson 2).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of division by using place-value patterns to calculate quotients.

Procedural Skill & Fluency

- Students develop proficiency with dividing whole numbers by multiples of 10.

Application

- Students apply their understanding of division to solve real-world problems

Application is not a targeted element of rigor for this standard.

Number Routine

Where Does It Go?

5–7 min

Build Fluency Students build number sense as they place 0.485 on a number line between 0 and 1 and then on a second number line between 0 and 0.5.

These prompts encourage students to talk about their reasoning:

- What do you think about first when trying to place 0.485 on a number line?
- Which labeled value is 0.485 closer to? How do you know?
- How can breaking up the number line into smaller intervals help you place 0.485?
- How can you be sure your answer is correct?

Purpose Students think about how objects are grouped in different ways and how they might determine the number of groups.

Notice & Wonder

- What question could you ask?

Teaching Tip Ask students to draw on their prior knowledge of how many pennies, nickels, dimes, and quarters are in a dollar. Have them determine how many of each type of coin are in each roll.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of using place-value patterns and basic facts to divide by multiples of 10 and are based on possible comments and questions that students may make during the share out.

- How can you determine how many coins are in each type of roll?
- What do you notice about how many are in each type of roll?
- How can you figure out if any of the coins are grouped in a similar way?
- If you knew how many of a type of coin you had, how do you think you could find how many rolls you would need to use?

Math is... Mindset

- How can your strengths in other areas help you in math?

Self-Awareness: Recognize Strengths

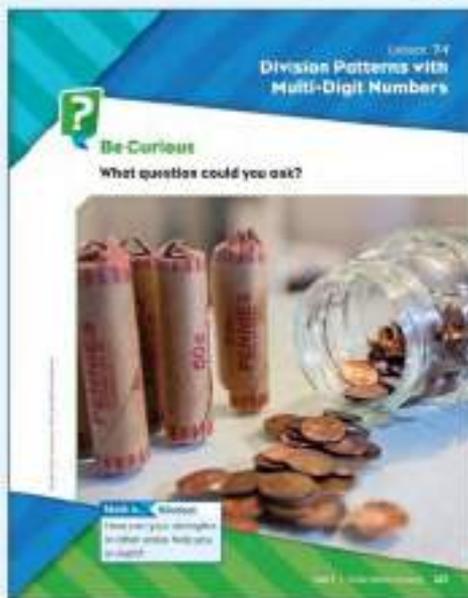
Before students begin the Notice and Wonder routine, invite them to think about their personal areas of strength in math. In addition to specific math skills, students may also acknowledge personal strengths that can help them with their learning, such as listening, staying focused, or explaining. As students work with division patterns throughout the lesson, model giving positive feedback to help them acknowledge their personal strengths. Encourage students to recognize and acknowledge the strengths of their peers.

Transition to Explore & Develop

Ask questions that get students thinking about using place-value patterns and basic facts to divide.

Establish Goals to Focus Learning

- Let's think about how we can use place-value patterns and basic facts to divide whole numbers by multiples of 10.




Learn

There are 2,000 rolls.

How can you find the number of rolls of nickels?

Patience can help you solve the problem.



$2,000 \div 40 = ?$

You can use a basic fact and patterns to help you solve the equation.

$300 \div 3 = 100$ $30 \div 3 = 10$ $3 \div 3 = 1$

With the dividend and divisor are 10 times as much as both of the number.

$300 \div 40 = 7.5$

What if the dividend is 10 times as much, the quotient is also 10 times as much.

$3,000 \div 40 = 75$

10 times the number of times in the dividend increases the number of times in the quotient ten times.

For the 200 rolls of nickels.

$2,000 \div 40 = 50$

Use the 200 rolls of nickels.

You can use patterns in the number of zeros. As the number of zeros in the dividend is 2, the number of zeros in the quotient is 0.

Work Together

What is the quotient? How can you use a basic fact and patterns to help?

Sample equations: The basic fact is $30 \div 3 = 10$. For $300 \div 30 = 10$, because both the dividend and divisor are 10 times as much, the quotient is the same. For the last two steps, when zeros are added to only the dividend, the quotient also increases by the same number of zeros.

$300 \div 30 = 10$ $30 \div 3 = 10$ For $200 \div 50 = 4$, because both the dividend and divisor are 10 times as much, the quotient is the same. For the last two steps, when zeros are added to only the dividend, the quotient also increases by the same number of zeros.

$200 \div 50 = 4$ $20 \div 5 = 4$ $2 \div 1 = 2$

1 Pose the Problem

Discussion Supports

As students talk about what they know, have them pay attention to others' understandings in order to increase their ability to work through division patterns with multi-digit numbers. Restate statements they make as a question to seek clarification and provide vocabulary or grammar prompts for students who need more guidance.

Pose Purposeful Questions

- How can you determine which operation you will use to solve this problem?
- Should the number of rolls be more or less than the number of nickels? How do you know?

2 Develop the Math

Choose the option that best meets your instructional goals.



3 Bring It Together

Elicit Evidence of Student Thinking

- How do basic facts help you divide multi-digit numbers?
- How do place-value patterns help you find the quotient when dividing by multiples of 10?

Key Takeaway

- One way to divide a whole number by a multiple of 10 is to use place-value patterns and basic facts.

Work Together

As students work together to solve the problem, make sure they start with a basic fact rather than jumping into the first equation. Have students discuss how the basic fact helps them solve the other equations.

Common Error When determining the basic fact, students may think they should use the most basic numbers, in this case, $3 \div 5$. Remind students that, in a basic division fact, the dividend is greater than the divisor.

Language of Math

The word *quotient* comes from the Latin word *quotiens* meaning "how many times." The quotient is how many times the divisor is in the dividend.

Activity-Based Exploration

Students explore patterns in division equations involving multiples of ten.

Materials: base-ten blocks

Directions: Display a basic fact, such as $15 \div 3$ and a problem in which the *dividend* and *divisor* are 10 times as much, such as $150 \div 30$. Have students model the division using base-ten blocks. Repeat with different problems. Encourage students to look for patterns as they represent and solve the various problems. After students have discovered and discussed patterns when both the dividend and divisor are 10 times as much. Display division problems in which the dividend is 10 times as much and the divisor stays the same, such as $1,500 \div 30$. Encourage students to look for patterns as they solve these equations.

Implement Tasks That Promote Reasoning and Problem Solving

- How did you determine how to represent the dividends and divisors using base-ten blocks?
- What happens to the quotient when both the dividend and divisor are 10 times as much? How can you show this?
- How does the quotient change when only the dividend is 10 times as much? How can you show this?

Math is... Structure

- How can you use place value to justify the pattern of zeros in the dividends and quotients?

Students explain a pattern that arises as a result of the structure of place value.

Activity Debrief: Have groups share their solutions and the patterns. Facilitate a discussion to ensure students understand that when both the dividend and divisor are 10 times as much, the quotient is the same as the basic fact. When only the dividend is 10 times as much, the quotient is also 10 times as much.

Have students revisit the Pose the Problem question and discuss answers.

- There are 12,000 nickels. How can you find the number of rolls of nickels?

English Learner Scaffolds

Entering/Emerging Ensure understanding of $(10 \times)$ as much. Write the number 10 on the board and say it aloud. Then write $\times 10 = 100$ next to it. Point to the 100 and say *This is ten times as much as 10*. Repeat with another number, such as 40. Ask students *Is 40 ten times as much as 400?* (no) *Is 400 ten times as much as 40?* (yes)

Developing/Expanding Ensure understanding of $(10 \times)$ as much. Write the number 10 on the board and say it aloud. Then write $\times 10 = 100$ next to it. Point to the 100 and say *This is ten times as much as 10*. *Times 10 is ten times as much*. Repeat with another number, such as 60. Then ask students to demonstrate the same task with a new number, such as 80, and to use $10 \times$ as much in their sentence.

Guided Exploration

Students use what they know about place value to use patterns that will help them divide multi-digit numbers that are multiples of ten.

Facilitate Meaningful Discourse

- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- How does the basic fact relate to the original equation?
- How do you think the basic fact might help you solve the equation?
- Have students use base-ten blocks to determine how many groups of 40 can be made by 120. Ask:
 - How do the base-ten blocks help you understand and find how many groups of 40 you can make?
- **Think About It:** How can thinking of 1,200 as 120 tens and 40 as 4 tens help you determine the quotient?

Math is... Structure

- How can you use place value to justify the pattern of zeros in the dividends and quotients?

Students explain a pattern that arises as a result of the structure of place value.



Bridging/Reaching Ask students to use $(10 \times)$ as much in a sentence, focusing on its usage on the Learn page. Then ask students to think of other words that could be used in place of it in their sentences ($(10 \times)$ more, $(10 \times)$ greater, etc.). Allow students to use a dictionary or thesaurus if desired.

Go My Own

Name: _____

Use a base ten block and patterns to solve.

1. $50 \div 10 = 5$ $30 \div 10 = 3$
 $500 \div 10 = 50$ $300 \div 10 = 30$
 $5,000 \div 10 = 500$ $3,000 \div 10 = 300$
 $50,000 \div 10 = 5,000$ $30,000 \div 10 = 3,000$

2. $12,000 \div 10 = 1,200$ A. $12,000 \div 10 = 1,200$

3. $13,000 \div 10 = 1,300$ B. $13,000 \div 10 = 1,300$

4. $27,000 \div 10 = 2,700$ C. $27,000 \div 10 = 2,700$

5. $22,000 \div 10 = 2,200$ D. $22,000 \div 10 = 2,200$

6. $12,000 \div 10 = 1,200$ E. $12,000 \div 10 = 1,200$

7. $13,000 \div 10 = 1,300$ F. $13,000 \div 10 = 1,300$

8. $27,000 \div 10 = 2,700$ G. $27,000 \div 10 = 2,700$

9. $22,000 \div 10 = 2,200$ H. $22,000 \div 10 = 2,200$

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11. There are 24,000 quarters in a roll of 40 quarters each. How many rolls of quarters are there?
800 rolls of quarters

12. **Error analysis:** Three students tried to solve $12,000 \div 10$ by starting with the tens. One student got 12,000. One student got 1,200. One student got 120. How did each student solve? How did they compare their answers?
One student multiplied the dividend by 10 and found 120,000 instead of 12,000. One student divided 12,000 by 10.

13. **270° Exploration:** A building has 22 floors. The building has a total floor area of 45,000 square feet. What is the area of each floor?
2,000 square ft; Sample answer: divide the total area by the number of floors.

14. **Shared Your Thinking:** Write a base ten block pattern to represent the division by 10. Compare the quotient to the dividend.
Sample answer: $10 \div 10 = 1$, $100 \div 10 = 10$, $1,000 \div 10 = 100$. The quotients are the same because the dividend and divisor were both multiplied by the same amount.

Reflection

How does using place-value patterns and basic facts help you divide whole numbers by multiples of 10?
Assess: vary, vary

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Practice

Build Fluency from Understanding

Common Error: Exercises 7–10 Remind students who determine quotients with the incorrect place value what the pattern in terms of the number of zeroes in the quotient looks like.

Practice Item Analysis

Item	DOK	Rigor
1–10	1	Procedural Skill and Fluency
11–13	2	Application
14	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How does using place-value patterns and basic facts help you divide whole numbers by multiples of 10?

Ask students to share their reflections with their classmates.

Math is... Mindset

- When might you use math outside of class?

Students reflect on how they practiced self-awareness.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain patterns when dividing by a multiple of 10.
- I can use patterns to determine the quotient when dividing by a multiple of 10.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Divide by multiples of 10	5.NBT.B.6
2	1	Divide by multiples of 10	5.NBT.B.6
3	2	Divide by multiples of 10	5.NBT.B.6
4	2	Divide by multiples of 10	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the U or T activities
3 of 4	<i>Take Another Look</i> or any of the U activities
2 or fewer of 4	Small Group Intervention or any of the T activities

Key for Differentiation

- T** Reinforce Understanding
- U** Build Proficiency
- T** Extend Thinking



Lesson 7.1
Exit Ticket

Name: _____

- Knowing that $24 \div 6 = 4$, write another fact? (Circle all that apply.)
 - A. $24 \div 6 = 4$
 - B. $48 \div 6 = 8$
 - C. $2,400 \div 60 = 4$
 - D. $2,400 \div 60 = 40$
 - E. $24,000 \div 60 = 40$
 - F. $24,000 \div 60 = 400$
- What is the quotient for $23,000 \div 100$?
 - A. 4
 - B. 100
 - C. 230
 - D. 2,300
- There are 40,000 dollars in one million. How many sets of three are there?

100 sets of three
- A company has 3,000 square feet of space for 40 offices. What is the area of each office?

75 square feet

Reflect On Your Learning

How confident? 1 2 3 4

How well did you do? 1 2 3 4

Assessment Review Book 108

R Reinforce Understanding

SMALL GROUP

Ten and Hundred Patterns

Work with students in small groups. Prepare index cards showing basic division facts. Have students draw a card. Students should use the basic fact and multiply the divisor and dividend by 10 and find the quotient. Then have them multiply only the dividend by 10 and find the quotient. Repeat with 100. Have students discuss the patterns they recognize in the different divisions.

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Multi-Digit Division Tic Tac Toe
Students find quotients of expressions that include multiples of 10 and 100.

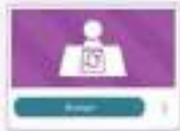


GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Divide by Multiples of 10



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 63

Lesson 3.1 • Reinforce Understanding
Division Patterns with Multi-Digit Numbers

Review

Use your knowledge working with powers of 10 and place value to help you divide.

$80,000 \div 100 = 800$ or $80 \times 1,000 \div 10 = 800$
 Find: $800,000 \div 10 = 80,000$ or $80 \times 10,000 \div 10 = 80,000$
 Find: $8,000,000 \div 100 = 80,000$ or $80 \times 1,000,000 \div 100 = 80,000$

Find the quotient for each equation, starting with a basic fact and showing the pattern you used to find the quotient.

1. $24,000 \div 6 = 4,000$ $24 \div 6 = 4$ $24,000 \div 6 = 4,000$	2. $56,000 \div 7 = 8,000$ $56 \div 7 = 8$ $56,000 \div 7 = 8,000$
3. $35,000 \div 5 = 7,000$ $35 \div 5 = 7$ $35,000 \div 5 = 7,000$	4. $21,000 \div 3 = 7,000$ $21 \div 3 = 7$ $21,000 \div 3 = 7,000$

Complete the pattern.

5. $140 \div 2 = 70$ $1,400 \div 20 = 70$ $14,000 \div 200 = 70$	6. $45 \div 5 = 9$ $450 \div 50 = 9$ $4,500 \div 500 = 9$
--	---

INDEPENDENT WORK

Student Practice Book, pp. 63–64

Lesson 3.1
Additional Practice

Review

You can use basic facts and patterns with factors of 10 to help you divide.

Start with the basic fact $75 \div 3 = 25$.

Multiply the dividend and the divisor by the same number of factors of 10. The quotient remains the same.

Multiply the dividend by 10 and the divisor by 10. The quotient remains the same. Then the quotient multiplies by the same number of factors of 10.

$750 \div 30 = 25$	$7,500 \div 300 = 25$
$7,500 \div 300 = 25$	$75,000 \div 3,000 = 25$

Write the basic fact for the division. Then use a pattern to find the quotient.

1. $3,200 \div 80 = 40$ $32 \div 8 = 4$ $320 \div 8 = 40$	2. $15,000 \div 50 = 300$ $15 \div 5 = 3$ $150 \div 5 = 30$
3. $140 \div 20 = 7$ $14 \div 2 = 7$ $140 \div 20 = 7$	4. $27,000 \div 300 = 90$ $27 \div 3 = 9$ $270 \div 30 = 90$

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with addition and subtraction of decimals.



Use it! Application Station

Online Learning: Is It Safe? Students write rules for safely using electronic devices and practice their rules by researching how to divide multi-digit numbers. *The content of this card has concepts covered later in Lesson 7-6. You may want to assign this card to students ready to explore content covered later in this unit.*



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Student Practice Book, pp. 63–64

Complete the pattern:

6. $27 \div 3 = 9$	8. $36 \div 4 = 9$
$270 \div 30 = 9$	$360 \div 40 = 9$
$2,700 \div 300 = 9$	$3,600 \div 400 = 9$
$27,000 \div 3,000 = 9$	$36,000 \div 4,000 = 9$

Find the quotient.

7. $640 \div 80 = 8$	9. $63,000 \div 700 = 90$
8. $3,600 \div 7 = 514$	10. $28,000 \div 400 = 70$

11. There are 52,000 quarters to sell (40¢). How many sets of quarters are there?
 1300 sets of quarters

12. A school has 24,000 square feet of space and each class has 60 square feet of space. How many classes can the school have?
 400 square feet

Math in Home Activity

Divide each other's equations and check the work. Then check the answer and explain to the other person if there is a mistake. Write down the correct answer and explain to the other person if there is a mistake.

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Differentiation Resource Book, p. 64

Lesson 7-6: Extend Thinking

Division Patterns with Multi-Digit Numbers

Name: _____

Calculate the quotient for each equation. Then write the quotients in order from least to greatest.

1. $4200 \div 10 = 420$	8. $3700 \div 90 = 41$
2. $8200 \div 900 = 9$	9. $33,000 \div 800 = 41$
3. $3500 \div 700 = 5$	10. $1800 \div 20 = 90$
4. $33,000 \div 7000 = 4.7$	11. $94,000 \div 4,000 = 23.5$

Quotients in order from least to greatest:
 $9 < 4.7 < 5 < 40 < 41 < 50 < 100 < 700$

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Estimate Quotients

Learning Targets

- I can explain how to estimate quotients of multi-digit numbers.
- I can estimate quotients of multi-digit numbers to determine if calculations are reasonable.
- I can use an estimated quotient to make predictions about a calculated solution.

Standards • Major • Supporting • Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Math Practices and Processes

- **MPP** Reason abstractly and quantitatively.
- **MPP** Use appropriate tools strategically.

Focus

Content Objectives

- Students estimate quotients of multi-digit numbers using strategies they used to estimate quotients of lesser numbers.
- Students use estimated quotients to make predictions and assess the reasonableness of a calculated solution.

Language Objectives

- Students talk about estimating quotients, using the terms *greater than*, *less than*, and *about*.
- To support optimizing output, ELs participate in MLR7: Compare and Connect.

SEL Objective

- Students set learning goals and initiate work on tasks to accomplish their goals.

Coherence

Previous

- Students used place-value strategies to find quotients of multi-digit numbers (Grade 4).
- Students used place-value patterns to determine quotients when dividing by multiples of 10 (Lesson 1).

Now

- Students use compatible numbers to estimate quotients of two whole numbers.

Next

- Students will use the relationship between multiplication and division to divide (Lesson 3).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build their understanding of division through estimating quotients.

Procedural Skill & Fluency

- Students use estimation strategies to begin to build proficiency with division.

Application

- Students apply their understanding of estimating quotients to solve problems.

Application is not a specific element of rigor for this standard.

Vocabulary

Math Term

estimate

Academic Terms

suggest
variation

Materials

The materials may be for any part of the lesson.

- digit cards

Number Routine

Which Benchmark Is It Closest To?



5–7 min

Build Fluency

Students build number sense as they determine which of three benchmarks is closest to given decimal numbers.

These prompts encourage students to talk about their reasoning:

- What do you notice about the numbers?
- How did you compare each value to the benchmark numbers?
- Why is 1.075 closer to 1 than to 2?
- Which numbers were easiest to place?
- What other numbers are close to that benchmark?
- How could you adjust the number so that it is closer to a different benchmark?

Purpose Students look at large numbers of groups and start to think about how they could figure out the number of groups.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may want to have students work on their own as they notice and wonder. Encourage students to notice the groupings in each picture and wonder about how the water bottles are grouped rather than the number of water bottles in all.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of estimating quotients using compatible numbers and are based on possible comments and questions that students may make during the share out.

- How are the water bottles grouped?
- How could you figure out how many bottles there are?
- How could you figure out how many groups there are?

Math is... Mindset

- What helps you be motivated to do your best work?

Self-Regulation: Initiative

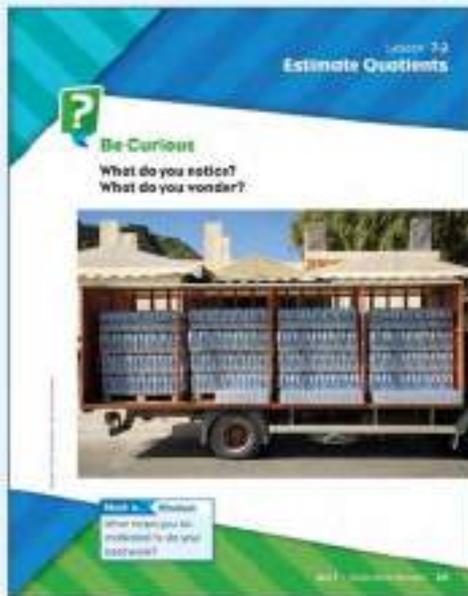
Before beginning the Notice & Wonder routine, guide students to make their own specific and attainable goal for the day. Goals may be centered around estimating quotients or may be focused on strong behaviors, such as active listening or staying on task. Creating a personal goal can allow students to practice self-motivation as they work toward achieving that goal.

Transition to Explore & Develop

Encourage students to understand that it would be more efficient for them to estimate how many groups of water bottles there are rather than to try counting each one.

Establish Goals to Focus Learning

- Let's think about how we can use compatible numbers to estimate quotients.

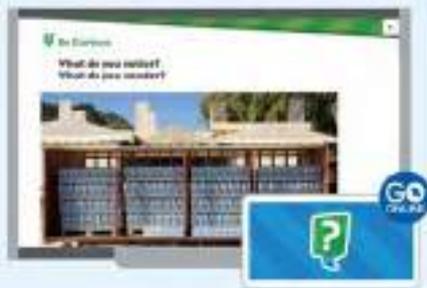


Lesson 7-2
Estimate Quotients

Be Curious
What do you notice?
What do you wonder?

Math is... Mindset
What helps you be motivated to do your best work?

Self-Regulation: Initiative
Before beginning the Notice & Wonder routine, guide students to make their own specific and attainable goal for the day. Goals may be centered around estimating quotients or may be focused on strong behaviors, such as active listening or staying on task. Creating a personal goal can allow students to practice self-motivation as they work toward achieving that goal.



Be Curious
What do you notice?
What do you wonder?

GO ON!

Learn

6 school children 2,000 bottles of water to be recycled this year.

What are some ways to estimate the number of boxes needed?



You can use different strategies to solve problems.

1. Round Up Use compatible numbers.

$$2,000 \div 24 \approx 100$$

$$2,200 \div 20 = 110$$

The answer will need about 100 boxes.

2. Round Up Use compatible numbers.

$$2,000 \div 24 \approx 100$$

$$2,200 \div 24 \approx 100$$

The answer will need about 100 boxes.

3,000 \div 24 = 125 (estimated answer)

The estimated answer is reasonable because it is close to the estimated quotients.

Made It... Estimating Quotients
 Write equations that use compatible numbers to estimate quotients. How do you know your estimate is reasonable?

Estimated quotients correctly give students whether calculations are reasonable.

Work Together

Estimate the quotient of $4,000 \div 10$ for different ways.

Sample answer: $4,000 \div 20 = 200$; $4,000 \div 10 = 400$

1 Pose the Problem

LEP Pose Purposeful Questions

- What are you trying to figure out?
- Do you need an exact answer? How do you know?

2 Develop the Math

Choose the option that best meets your instructional goals.

LEP Compare and Connect

Pair students and have them both work on the same problem, similar to the one on the Learn page, and then have them compare their work with their partner. Revisit this routine throughout the lesson to help students build proficiency.



3 Bring It Together

LEP Elicit Evidence of Student Thinking

- How is estimating quotients useful?
- How would you explain to a classmate how to estimate a quotient?

Key Takeaways

- Estimating quotients can help make predictions about a calculated solution.
- Estimating quotients helps assess the reasonableness of a calculated solution.
- Strategies used to estimate quotients of lesser numbers, such as compatible numbers, can also be used to estimate quotients of multi-digit numbers.

Work Together

As students determine what numbers to use for estimating with compatible numbers, ask them to predict whether the calculated quotient will be greater than or less than each estimated quotient.

Common Error Remind students to make sure their estimate has the correct number of zeroes, especially if they used what they know about place value patterns to estimate. For example, they may have used the numbers $4,000 \div 20$ to estimate.

LEP Language of Math

Remind students that *compatible* means “working well together.” Compatible numbers are easy to divide mentally because they are related to a basic division fact. For example, while $3,000 \div 24$ is not easy to calculate mentally, $3,000 \div 30$ is because it is related to $30 \div 3$.

Activity-Based Exploration

Students explore strategies for estimating quotients.

Materials: *Show and Explain Your Strategies* Teaching Resource

Directions: Distribute copies of the *Show and Explain Your Strategies* Teaching Resource. Have students solve the Pose the Problem using two different estimation strategies. Students should complete the Show and Explain boxes on the Teaching Resource. For the Check box, tell students that the calculated quotient is 125. Have students use their estimates to estimate the reasonableness of the calculated quotient.

Support Productive Struggle

- How could you make the dividend and the divisor easier to divide mentally?
- How can you use what you know about strategies for estimating products to estimate quotients?
- How can you use what you know about basic division facts and place-value patterns to estimate the quotient?

Math is... Choosing Tools

- Why might you estimate a quotient more than one way?

Students strategically use estimation as a tool to help them solve problems. For example, they might use several estimates to get a range of reasonable calculated quotients.

Activity Debrief: Invite volunteers to share the estimated quotients and the strategy they used to determine their estimate. Have students compare the different strategies by identifying similarities and differences.

A PDF of the Teaching Resource is available in the Digital Teacher Center.



Guided Exploration

Students estimate quotients and compare the estimates to a calculated quotient to assess if it is reasonable.

Facilitate Meaningful Discourse

- **Think About It:** Why is 20 used to estimate the quotient?
- How can basic facts and place-value patterns help you determine $3,000 \div 20$?

Discuss why rounding and front-end estimation are not viable strategies for estimating quotients. Ask:

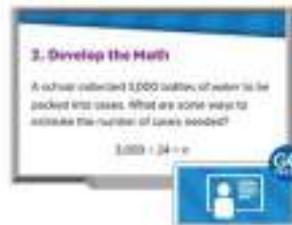
- Why wouldn't rounding work to estimate $3,000 \div 44$?
- Why wouldn't front-end estimation work to estimate $5,000 \div 37$?

Have students work in pairs or small groups to determine how the estimated quotient relates to the actual quotient. Students should use the meaning of division to help explain their reasoning, such as since both have the same total number of objects (3,000) and we are dividing them into a greater number of groups ($30 > 24$), the number in each group will be less.

Math is... Choosing Tools

- Why might you estimate a quotient more than one way?

Students strategically use estimation as a tool to help them solve problems. For example, they might use several estimates to get a range of reasonable calculated quotients.



English Learner Scaffolds

Entering/Emerging Support students' understanding of the adjective *needed*. Use crayons to color a picture. Say *I colored this picture*. Point to the crayons you used. Say *These were needed to color the picture*. Repeat with a new task using new materials. Then repeat again with another task, and ask two questions, one prompting a Yes answer and one a No. Ask *Were these / Was this needed to [task]?*

Developing/Expanding Ensure understanding of the adjective *needed*. Say *I want to color a picture*. Ask *What do I need?* Students respond with something needed (paper, markers, etc.) Say *That's right. [Markers] are needed*. Repeat with a new task using new materials. Then instruct students to think about the last school or home task they worked on. Ask *What materials were needed to complete it?*

Bridging/Reaching Ask students to talk about the last school or home task they worked on, and to discuss what materials were needed to complete it. Then have them brainstorm and list similar words to *needed* and share their list with the class (*required, necessary, etc.*). Allow students to use a dictionary or thesaurus if desired.

On My Own

Name: _____

Estimate the quotient. Sample answers are given.

1. $2,400 \div 34$ **80** 3. $1,100 \div 65$ **60**

2. $1,600 \div 62$ **20** 4. $4,800 \div 80$ **60**

5. $3,200 \div 31$ **300** 6. $3,000 \div 45$ **250**

7. $600 \div 40$ **30** 8. $3,000 \div 7$ **550**

9. **Think Aloud:** The writer has questions to help students understand. Explain.
No. Sample answer: an estimated quotient is 300 so 3,850 is not reasonable.

10. A gas station increases the fuel tank to a total of 3,800 gallons to 10 gallons. About how many gallons of fuel is each gas?
Sample answer: about 200 gal

11. Describe how 123 Furbies cost the same as a pair. About how many pawns did Owen use each month?
Sample answer: about 900 pawns

12. **Extend Your Thinking** Which of these equations has a reasonable estimate to 523 \div 571 before you multiply?
 $340 \div 60 \approx 9$ $520 \div 50 \approx 10$ $420 \div 60 \approx 7$
 $420 \div 60 \approx 7$. **Sample answer: 420 and 60 are compatible numbers, but 420 is not close to the actual dividend.**

Reflect

How can you use estimates to determine if calculations are reasonable?
Answers may vary.

Math is... 1indset
 What helped you be confident in your best work?

Practice

Build Fluency from Understanding

Common Error: Exercises 1–8 Students may attempt rounding or front-end estimation to estimate quotients but doing so may not result in compatible numbers. While rounding and front-end estimation are strategies that work well for other operations such as adding and multiplication, they are not useful strategies for division.

Practice Item Analysis

Item	DOK	Rigor
1–8	1	Procedural Skill and Fluency
9	2	Conceptual Understanding
10–11	2	Application
12	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you use estimates to determine if calculations are reasonable?

Ask students to share their reflections with their classmates.

Math is... 1indset

- How can you help yourself to start your work independently?

Students reflect on how they practiced self-management.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can explain how to estimate quotients of multi-digit numbers.
- I can estimate quotients of multi-digit numbers to determine if calculations are reasonable.
- I can use an estimated quotient to make predictions about a calculated solution.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Estimate quotients	5.NBT.B.6
2	1	Estimate quotients	5.NBT.B.6
3	2	Estimate quotients	5.NBT.B.6
4	2	Estimate quotients	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the 1 or 2 activities
3 of 4	<i>Take Another Look</i> or any of the 3 activities
2 or fewer of 4	Small Group Intervention or any of the 4 activities

Key for Differentiation

- 1** Reinforce Understanding
- 2** Build Proficiency
- 3** Extend Thinking



Lesson 7-2
Exit Ticket

Name: _____

- The school bought 400 baseball bats for \$32,000. How much did each bat cost?
 A. $320 \div 4$
 B. $400 \div 32$
 C. $320 \div 400$
 D. $400 \div 320$
 E. $32,000 \div 400$
- Which is a reasonable estimate of the quotient $2,332 \div 100$?
 A. 4 B. 30
 C. 23 D. 300
- A basketball player scored 320 points during the season. If the player played in 32 games, about how many points did the player score each game?
about 20 points
- If a class collected 3,200 cans for recycling in 32 weeks, about how many cans were collected each week?
about 200 cans

Reflect On Your Learning

How confident are you about your learning? Circle the number that best describes your confidence.

1 2 3 4

100% Confident Fairly Confident Somewhat Confident Not Confident at All

100% 75% 50% 25%

R Reinforce Understanding

SMALL GROUP

Flip It

Work with students in pairs. Have students flip over digit cards and work together to create a division equation with a 3-digit dividend and a 2-digit divisor. Have one student estimate a quotient using rounding and the other students estimate an answer using compatible numbers. Discuss with students whether each estimate is greater than or less than the solution and which they expect to be closer to the actual quotient.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Estimate Quotients (Whole Number)



WORKSTATIONS

B Build Proficiency

Practice It! Game Station

Estimating Quotients Showdown
Students practice estimating quotients.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Differentiation Resource Book, p. 65

UNIT 7 • Reinforce Understanding
Estimate Quotients

Name _____

Review
When estimating a quotient, you may find it helpful to use compatible numbers that are multiples of 10.
 $6,200 \div 10 = 620$
 $6,200$ is 200 more than $6,000$ and 70 is 10 more than 60 .
 $6,200 \div 70 \approx 90$ so the quotient is $6,200 \div 70 \approx 90$.

Estimate the quotient. Simple answers given.

1. $6,300 \div 30 = 210$	6. $6,037 \div 30 = 201$
2. $2,700 \div 30 = 90$	7. $3,907 \div 30 = 130$
3. $9,000 \div 90 = 100$	8. $3,400 \div 20 = 170$
4. $1,500 \div 30 = 50$	9. $600 \div 10 = 60$

Differentiation Resource Book

INDEPENDENT WORK

Student Practice Book, pp. 65–66

UNIT 7 •
Additional Practice

Name _____

Review
You can use compatible numbers to estimate quotients.
A round number is called a compatible number for another number.
How many cars were collected each day?
 70 cars in 40 days
 30 cars in 30 days

Estimate the quotient. Simple answers given.

1. $3,000 \div 40 = 75$	6. $4,000 \div 50 = 80$
2. $6,000 \div 30 = 200$	7. $4,000 \div 80 = 50$
3. $800 \div 20 = 40$	8. $2,000 \div 50 = 40$
4. $3,000 \div 30 = 100$	9. $2,000 \div 70 = 28$

Student Practice Book

Relate Multiplication and Division of Multi-Digit Numbers

Learning Target

- I can use the relationship between multiplication and division to determine the quotient when dividing by a 2-digit divisor.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Math Practices and Processes

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Terms

dividend
divisor

Academic Terms

analyze
establish

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- number cubes

Focus

Content Objective

- Students use the relationship between multiplication and division to determine the quotient when dividing by a 2-digit divisor.

Language Objective

- Students describe the relationship between multiplication and division that helps them to find the quotient when dividing by a multiple of 10 using the verb *determine* and the adjectives *same* and *different*.
- To support sense-making, ELs participate in MLR2: Collect and Display.

SEL Objective

- Students collaborate with peers and contribute to group effort to achieve a collective mathematical goal.

Coherence

Previous

- Students used place value strategies to find quotients with up to 4-digit dividends and 1-digit divisors (Grade 4).
- Students estimated quotients using rounding (Lesson 3).

Now

- Students use the relationship between multiplication and division to divide multi-digit numbers.

Next

- Students will extend their understanding to divide using an area model using partial quotients (Lesson 4).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build their understanding of multiplication and division using basic facts to divide multi-digit numbers.

Procedural Skill & Fluency

- Students build proficiency with multi-digit division using basic multiplication facts.

Application

- Students solve real-world division problems.

Application is not a specific element of rigor for this standard.

Number Routine

Which Benchmark Is It Closest To?



5–7 min

Build Fluency

Students build number sense as they determine which of four benchmarks is closest to given decimal numbers.

These prompts encourage students to talk about their reasoning:

- What do you notice about the numbers?
- How did you compare each value to the benchmark numbers?
- How do you know if 2.035 is closer to 2 or 2.25?
- Were some numbers easier to compare than others? Explain.

Purpose Students study a picture of groups of objects to think about how they might use multiplication to determine how many objects there are, or division to determine how many groups there are.

Notice & Wonder

- What do you notice?
- What do you wonder?

Teaching Tip You may have students work in pairs or small groups as they discuss the image. Hearing other students' thinking may give students more insight into what they notice and wonder about the image.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of how the relationship between multiplication and division can help us divide and are based on possible comments and questions that students may make during the share out.

- How could you find the total number of pieces of fruit?
- If you knew the total number of pieces of fruit, how could you find the number of pieces in each crate?

Math is... Mindset

- What are some ways you can contribute to your group today?

Relationship Skills: Teamwork

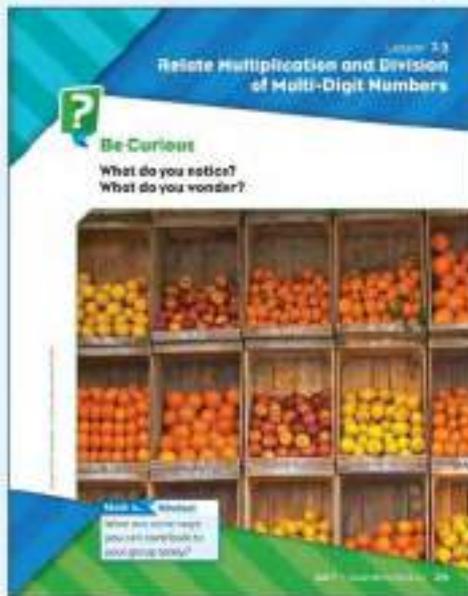
Establish a positive classroom culture by providing students opportunities to work together to complete collective tasks. As students notice and wonder, encourage them to work together and build off the ideas of their peers. Invite students to participate in different ways so that each student can actively contribute to the team effort.

Transition to Explore & Develop

Ask questions to encourage students to think about the relationship between multiplication and division.

Establish Goals to Focus Learning

- Let's think about how our knowledge of the relationship between multiplication and division can help us solve division equations.



Learn
 2. Use the relationship between multiplication and division to determine the quotient.

How many boxes of tea will the cafe owner receive?

8. Another way to solve this problem is $360 \div 25 = ?$
 9. Another equation with an unknown factor that also represents the problem is $14 \cdot 25 = 350$.

Start With	Number of Boxes	Amount of Tea
$6 \times 25 = 150$	6	150
$8 \times 25 = 200$	8	200
$6 \times 25 = 150$	6	150
$2 \times 25 = 50$	2	50
$6 + 8 + 6 + 2 = 16$	16	400
$14 \times 25 = 350$	14	350
$360 \div 25 = 14.4$		

Math In Context
 Write an equation with an unknown factor that also represents the problem. Why is this equation not helpful?

Work Together
 Use multiplication to solve for n . Show your work.
 $1,000 \div 22 = n$
 $n = 75$. Check students' work.

1 Pose the Problem

Collect and Display

As students discuss the questions, record relevant words and phrases they may use such as *operations*, *unknown factor*, *same*, and *groups* of. Display the words for student reference. Use the student-generated expressions to help students make connections between student language and math vocabulary.

Pose Purposeful Questions

- What is happening in the problem?
- What are you trying to find? How do you know?
- What operations can you use to solve the problem?

2 Develop the Math

Choose the option that best meets your instructional goals.

3 Bring It Together

Elicit Evidence of Student Thinking

- How can your knowledge of multiplication help you solve division equations?
- What are some different ways you can use multiplication to solve division equations?
- How is the quotient of a division equation related to a multiplication equation?

Key Takeaway

- One way to determine the quotient of a whole number divided by a 2-digit divisor is using the relationship between multiplication and division.

Work Together

Students work together to solve a division equation using multiplication. Have them multiply 22 by different factors to see if they find any patterns.

Common Error Students may be confused initially as 22 does not seem as simple a factor to multiply by as 25. However, remind them that they can use patterns of multiplication to more easily find the products.

Language of Math

Remind students that while two numbers being multiplied can both be called factors, in a division equation there is a specific *dividend* and *divisor*. The terms are not “commutative.”

Activity-Based Exploration

Students explore using multiplication concepts, such as equal groups, to solve a division equation.

Materials: number cube

Directions: Before having students start the activity, facilitate a discussion to ensure students understand that both $350 \div 25 = t$ and $t \times 25 = 350$ can be used to represent the problem. Provide each pair or small group a number cube. Explain that their goal is to be the first person to reach 350. Students will roll the number cube. This is the number of groups of 25. Students should use multiplication to determine the total number and subtraction to determine how much is left. If a student rolls a number that creates a total number that is too many, they lose their turn. Have students record how many groups of 25 it takes to reach 350.

Implement Tasks That Promote Reasoning and Problem Solving

- How does making groups of 25 help you solve for t ?
- How is your answer is the same as your classmates' answer? How is it different?
- Is your solution reasonable? How do you know?

Math is... Generalizations

- Will this strategy work for all division situations? Why or why not?

Students consider using multiplication as a general method to divide.

Activity Debrief: Have students share their recorded solutions. Facilitate a discussion to ensure students understand that there are multiple strategies for solving $350 \div 25 = t$, but that all strategies result in a total number of 14 groups of 25 to make 350. Discuss the benefits of starting with a greater number of groups of 25, such as 10 groups of 25, in that 10×25 is easy to multiply mentally.

English Learner Scaffolds

Entering/Emerging Ensure understanding of *hold*. Try to put objects into a container that isn't big enough. Say *This [box] can't hold all of my [art supplies]*. Then get a larger container and put the items in it. Say *This [box] holds all of my art supplies*. Repeat again with new containers and/or items. Then repeat once more, asking students *Does this [box] hold all of my [books]?*

Developing/Expanding Ensure understanding of *hold*. Try to put objects into a container that isn't big enough. Say *This [box] can't hold all of my [art supplies]*. Then get a larger container and put the items in it. Say *This [box] holds all of my art supplies*. Repeat again with new containers and/or items. Then ask students to use *hold* in a sentence, demonstrating with new items. Provide sentence frames if needed.

Bridging/Reaching Ask students to look at the Learn page and to use *hold* in a similar way in their own sentence. Then ask them to come up with other meanings and uses of the word (*hold something with your hands, hold a baby, hold a meeting*, etc.). Allow students to use a dictionary to help them if needed.

Guided Exploration

Students solve a division problem using the relationship between multiplication and division.

Facilitate Meaningful Discourse

- Have the students create the division equation. Ask:
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - What compatible numbers will you use to estimate the solution? Why?
 - How will basic facts and place-value patterns help you estimate the solution?
 - Why might writing a related multiplication equation be helpful?
 - **Think About It:** What numbers are compatible with 25? Why?
 - Why is 4 a good choice to start with?
- Have students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?
 - Why is 10 a good choice to start with?
 - Which way do you think is more efficient? Why?

Math is... Generalizations

- Will this strategy work for all division situations? Why or why not?

Students consider using multiplication as a general method to divide.



On My Own

Name _____

- How many groups of 25 can you make from 500? **20**
- How many groups of 48 can you make from 480? **10**
- How many groups of 12 can you make from 192? **16**
- How many groups of 18 can you make from 324? **18**

Solve for the unknowns.

6. $200 = 52 \times \square$	7. $48 = 16 \times \square$
8. $12 = 3 \times \square$	9. $30 = 6 \times \square$
10. $18 = 6 \times \square$	11. $24 = 8 \times \square$
12. $36 = 12 \times \square$	13. $54 = 9 \times \square$
14. $72 = 12 \times \square$	15. $63 = 7 \times \square$

16. The 8th grade class is getting ready for a performance. They need to sell 400 sheets of paper for 200 sheets. The sheets are sold in boxes of 20. How many boxes will they need?
20 boxes

17. Monica needs to prepare for a cooking class. She needs to buy 100 sheets of paper for 100 sheets. The sheets are sold in boxes of 20. How many boxes will she need?
50 plastic sheets



18. **11th-Grade Connection:** How can you look at a number line to see how many groups of 100 are in 1,000? How many groups of 100 are in 1,000? How many groups of 100 are in 1,000?
10 groups of 100



19. A family has 3,000 columns and 7 different programs of 7 different sizes. All of the programs have the same number of columns. How many columns are in each program?
6,000 = 7 × □ = 6,000, 900 columns

20. **Stand Your Ground:** Why does the sum of a dividend equal to the sum of the multiplier times the divisor plus the remainder?
Sample answer: When you know a multiplication equation, such as $25 \times 4 = 900$, it can be more difficult to find how many groups of the divisor are in the dividend by using multiplication and subtracting from the dividend.

Reflect

How can you use the relationship between multiplication and division to solve problems? How can you use the quotient of multi-digit whole numbers?
Answers may vary.

Math is... Mindset
How do you think you will do on this problem?

Practice

Build Fluency from Understanding

Common Error: Exercises 1–8 Remind students to consider numbers that are compatible with the divisors before they begin solving. For example, for Exercise 3, students may know that $12 \times 4 = 48$, so can use groups of 4 to see how many groups of 12 are in 192.

Practice Item Analysis

Item	DOK	Rigor
1–8	1	Procedural Skill and Fluency
9–12	2	Application
13	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can using the relationship between multiplication and division help you determine the quotient of multi-digit whole numbers?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How can working as a team help us achieve our goals?

Students reflect on how they developed stronger relationship skills.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can use the relationship between multiplication and division to determine the quotient when dividing by a 2-digit divisor.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Relate multiplication and division	5.NBT.B.6
2	1	Relate multiplication and division	5.NBT.B.6
3	2	Relate multiplication and division	5.NBT.B.6
4	2	Relate multiplication and division	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the 1 or 2 activities
3 of 4	<i>Take Another Look</i> or any of the 1 activities
2 or fewer of 4	Small Group Intervention or any of the 1 activities

Key for Differentiation

- 1 Reinforce Understanding
- 2 Build Proficiency
- 3 Extend Thinking



Lesson 7-3
Exit Ticket

Name: _____

- Which equation can be used to help you solve $272 \div 12 = n$?
 - A. $n \div 12 = 272$
 - B. $n \div 272 = 12$
 - C. $n \times 272 = 12$
 - D. $n \times 12 = 272$
- How many groups of 80 oranges were from 200?
 - A. 15
 - B. 14
 - C. 16
 - D. 17
- There are 284 seats left up in the auditorium. They are arranged with 24 seats in each row. How many seats are in each row?

16 seats
- Last week, all 400 people had the 200 pages. How did each of 22 people each have how many pages did they get to read?

17 hours

Reflect On Your Learning

No confidence
Low confidence
I understand
I can teach someone else.

Assessment Review Book 189

R Reinforce Understanding

SMALL GROUP

Swap It

Work with students in pairs. Partners use number cubes to create and solve a multiplication equation with a 3-digit product and a 1-digit factor. Partners work together to write and solve a related division equation. If students are struggling suggest them use a model to help. Have partners check their work with a calculator.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Relate Multiplication and Division (Whole Numbers)



INDEPENDENT WORK

Differentiation Resource Book, p. 67

Lesson 3.3 • Reinforce Understanding

Relate Multiplication and Division of Multi-Digit Numbers

Name _____

Review

Complete the equations. $240 \div 10 = 24$

So how many times 100 will go into 240? $240 \div 100 = 2.4$

How many times will 100 go into 240? $240 \div 100 = 2.4$

$10 \div 10 = 100$
 $3 \div 3 = 90$

$100 \div 10 = 1000$, so $100 \div 10 = 10000$, $10 \div 10 = 100000$, $10 \div 10 = 1000000$, $10 \div 10 = 10000000$

Determine how many groups of each unknown factor you can make in each equation. Show your work. **Simple work sheet.**

<p>1. $270 \div 10 = 27$</p> <p>$270 \div 10 = 270$</p> <p>$27 \times 10 = 270$, $270 \div 10 = 27$</p> <p>$10 \times 15 = 150$</p> <p>$4 \times 15 = 60$</p> <p>$4 \times 35 = 140$</p>	<p>2. $600 \div 21 = 28$</p> <p>$600 \div 21 = 28$</p> <p>$28 \times 21 = 588$</p> <p>$30 \times 21 = 630$</p> <p>$3 \times 21 = 63$</p>
<p>3. $180 \div 62 = 2.9$</p> <p>$180 \div 62 = 2.9$</p> <p>$2.9 \times 62 = 180$</p> <p>$6 \times 62 = 372$</p> <p>$3 \times 62 = 186$</p>	<p>4. $450 \div 17 = 26$</p> <p>$450 \div 17 = 26$</p> <p>$26 \times 17 = 442$</p> <p>$30 \times 17 = 510$</p> <p>$6 \times 17 = 102$</p>

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Multi-Digit Division Tic Tac Toe

Students find quotients of expressions that include multiples of 10 and 100.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 67–68

Lesson 3.3

Additional Practice

Name _____

Review

You can use multiplication to help you find a quotient.

Get a ball of yarn. Use it to make 240 loops over 10 days. How many loops did they use each day?

10 loops, find the quotient $240 \div 10 = 24$

Write a related multiplication equation. $24 \times 10 = 240$. Find how many groups of 10 there are in 240.

$50 \times 70 = 3500$	341
	-350
	3061
$50 \times 50 = 2500$	991
	-250
	741
$3 \times 70 = 210$	41
	-41
	0

There are 24 + 10 + 10 = 44 groups of 10. So $240 \div 10 = 24$. There are 24 groups of 10 there are 4 days.

- How many groups of 70 can you make from 280? **4**
- How many groups of 22 can you make from 484? **22**
- How many groups of 11 can you make from 990? **90**
- How many groups of 33 can you make from 1320? **40**

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with addition and subtraction of decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 67–68

Write the related multiplication equation. Then solve.

1. $442 \div 11 = 40$ $473 \div 11 = 43$
 $11 \times 41 = 442$, $n = 25$ $11 \times 43 = 473$, $q = 42$

2. $320 \div 24 = 13$ $320 \div 12 = 8$
 $24 \times 24 = 456$, $q = 18$ $6 \times 12 = 72$, $h = 25$

3. A landscaper plants 240 flowers. The flowers are planted in 12 equal rows. How many flowers are in each row?
20 flowers

4. A contractor has 2700 pounds of bulk. He builds a rough wooden deck for his job. If he divides the bulk in equal parts, how many pounds does the deck hold?
90 pounds

Math
Fluency
Activity

Student Practice Book

M

Extend Thinking

Use It! Application Station

That Is Astronomical Students practice finding quotients, rounding, and writing equations by researching the hours in a day for each planet. *The content of this card has concepts covered later in Lesson 7-7. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 68

Lesson 7-3 • Extend Thinking

Relate Multiplication and Division of Multi-Digit Numbers

Name: _____

You can make 24 groups of 24 from 584.

1. How many groups of 12 can you make from 584? **72**

2. $58 \times 24 = 1392$ and $72 \times 12 = 864$. Describe any pattern you see. **Notice: $58 \times 24 = 2 \times 29 \times 24 = 1392$. In problem 1, 72 groups of 12 make 864. I noticed that $24 \div 12 = 2$ and 26×24 was easier for problem 5.**

3. How many groups of 18 can you make from 584? **8**

4. $18 \times 24 = 432$ and $24 \times 8 = 192$. Describe any pattern you see. **Notice: $18 \times 24 = 2 \times 9 \times 24 = 432$. In problem 2, 8 groups of 18 make 144. I noticed that $24 \div 3 = 8$ and $24 \div 3$ is the answer for problem 3.**

Use patterns to quickly solve these problems.

5. You can make 6 groups of 11 from 66. How many groups of 7 can you make?
66; $66 \div 11 = 6$ and $12 \div 3 = 4$

6. You can make 6 groups of 27 from 162. How many groups of 18 can you make?
14; $27 \div 3 = 9$ and $40 \div 5 = 8$

7. You can make 20 groups of 34 from 680. How many groups of 5 can you make?
68; $68 \div 34 = 2$ and $22 \div 4 = 5.5$

INDEPENDENT WORK

Represent Division of 2-Digit Divisors

Learning Target

- I can use an area model to determine partial quotients and add partial quotients to calculate the quotient.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Math Practices and Processes

MPP Model with mathematics.

MPP Look for and make use of structure.

Vocabulary

Math Term

partial quotient

Academic Terms

reflect

speculate

Materials

The materials may be for any part of the lesson.

- base-ten blocks
- calculators

Focus

Content Objective

- Students use an area model to determine partial quotients and add partial quotients to calculate the quotient.

Language Objectives

- Students explain how to use an area model to determine and add partial quotients using comparatives *more useful*, *less useful*, *more helpful*, and *less helpful*.
- To support optimizing output, ELs participate in MLR1: Stronger and Clearer Each Time.

SEL Objective

- Students discuss how a rule or routine can help develop mathematical skills and knowledge and be responsible contributors.

Coherence

Previous

- Students used place-value strategies to find quotients (Grade 4).
- Students used the relationship between multiplication and division to divide (Lesson 3).

Now

- Students extend their understanding of division to divide using an area model and partial quotients.

Next

- Students will use partial quotients to divide by 2-digit divisors (Lesson 5).
- Students will fluently divide using an algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of division as they begin to divide with 2-digit divisors using area models.

Procedural Skill & Fluency

- Students build proficiency with division facts for dividing with 2-digit divisors.

Application

- Students apply their understanding of division to solve real-world problems.

Application is not a specific element of rigor for this standard.

Number Routine

Find the Pattern, Make a Pattern

5–7 min

Build Fluency Students build reasoning skills as they determine a given pattern, find missing terms, and repeat the pattern with different numbers.

These prompts encourage students to talk about their reasoning:

- What do you notice about the numbers?
- How did you determine the pattern used?
- What is another way to think about the pattern?
- How did you determine the missing value?
- What do you notice about the new patterns?

Purpose Students think about what they know about the image and what math they can use to describe it.

Notice & Wonder

- Tell me everything you can.

Teaching Tip You may want to have students work in pairs as they notice and wonder. This can help build a collaborative classroom culture. It also allows for greater participation among students as they work with their partners.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of representing division using area models and are based on possible comments and questions that students may make during the share out.

- How are area, length, and width related?
- How does this image remind you of problems you have solved before?

Math is... Mindset

- What is your responsibility in building a safe classroom culture?

Responsible Decision-Making: Ethical Responsibility

Invite students to discuss the rules or routines they will follow while working through the Notice & Wonder routine. Have them consider how these rules or routines help them be responsible contributors to their classroom community. As students work through the lesson, have them consider how they can work ethically and responsibly with others, giving credit to others and acknowledging the contributions of others, while also contributing their own thoughts and ideas.

Transition to Explore & Develop

Ask questions that get students thinking about the use of division to solve problems. Guide the discussion to have students think about how they could represent the division.

Establish Goals to Focus Learning

- Let's think about how we can represent division using area models.

Lesson 7-4
Represent Division of
2-Digit Divisors

 **Be Curious**
Tell me everything you can.



Math is... Mindset
What is your responsibility in building a safe classroom culture?

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 **Be Curious**
Tell me everything you can.



GO ONLINE



Activity-Based Exploration

Students explore using an area model to divide by 2-digit divisors by extending their understanding of using an area model to divide by 1-digit divisors.

Directions: Write the division equation $1,550 \div 5 = m$. In pairs, have students solve using an area model. Then, write the equation $1,550 \div 25 = t$. With their partner, have students first discuss a plan on how they could use an area model to represent division with a 2-digit divisor. Have students test their plan to divide by a 2-digit divisor.

Implement Tasks That Promote Reasoning and Problem Solving

- What steps did you take to solve the equation with a 1-digit divisor?
- Do you think you could extend this understanding to solve a division equation with a 2-digit divisor?
- How was solving a division equation with a 2-digit divisor similar to solving a division equation with a 1-digit divisor? How was it different?

Math is... Modeling

- What did the area model tell you and how did it help you understand the problem?

Students interpret their mathematical results in the context of the situation and consider if the representation used served their purposes.

Activity Debrief: Ensure that students understand that using an area model to divide by a 2-digit divisor is an extension of their understanding of using an area model to divide by a 1-digit divisor.

Have students revisit the Pose the Problem question to solve and discuss answers.

- The Parthenon, in Athens, Greece covers an area of about 2,139 square meters. What is the length of the Parthenon?

English Learner Scaffolds

Entering/Emerging Support students in understanding the word *solution*. Write an equation on the board. Say *I need to solve this equation*. Solve the equation and then say *I solved the equation. I determined the solution*. Point to the solution. Repeat twice with new equations, once showing a solution, and once not. Ask *Did I determine the solution?*

Developing/Expanding Support students in understanding the word *solution*. Write an equation on the board. Say *I need to solve this equation*. Solve the equation and then say *I solved the equation. I determined the solution*. Solve another equation, but this time, ask students to tell you what the solution is using the word *solution*. Provide sentence frames for students who need more guidance.

Bridging/Reaching Ask students to explain how *solution* is related to *solve*. Then ask students to come up with a list of similar words to *solution* (*answer, result, etc.*) and to share their list with the class. Finally, support students in discussing the similarities and differences in meaning between *solve* and *resolve*. Allow students to use a dictionary or thesaurus if desired.

Guided Exploration

Students extend their understanding of division to dividing by 2-digit divisors. They use area models to divide.

Use and Connect Mathematical Representations

- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - What compatible numbers will you use to estimate the solution? Why?
 - How will basic facts and place-value patterns help you estimate the solution?
 - **Think About It:** Why was 60 used instead of the estimate of 70?
- After finding the area represented by the each partial quotient, have students determine how much area is remaining.
- Have students use their estimates to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Modeling

- What did the area model tell you and how did it help you understand the problem?

Students interpret their mathematical results in the context of the situation and consider if the representation used served their purposes.



On My Own JUST GO

Name: _____

What is the quotient? Use an area model and partial quotients to solve.
Check students' models.

1. $176 \div 4 = 44$ 3. $330 \div 6 = 55$

2. $220 \div 4 = 55$ 4. $1269 \div 9 = 141$

8. STEM Connection: Steve is trying to understand computer games. The game costs \$1.64 for every minute. He has 48 minutes. How many minutes does each quarter hour? **63 blocks**



9. The floor in a large classroom has an area of 1804 square feet and is 22 feet wide. How long is the classroom? **82 ft**

10. A factory is making ice cream. It has an amount of 222 square inches and 300 inches long. How wide is the factory? **18 in.**

11. The height of a new office building is 17 stories tall with a total of 238 square meters. How long is the building? **23 m**

12. A parking lot is 1000 ft long with an area of 4000 square feet. How wide is the parking lot? **50 ft**

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10. What is the quotient of $576 \div 8$?

A. 72 B. 71
 C. 70 D. 50

11. Mr. Maxwell drove 128 miles on the highway over a 16-day period. He had a constant speed of 80 miles per hour. How fast did he drive?
24 hours

12. Tom pays \$11 per hour working at a store. How many hours does he need to work to afford a new \$100 smart phone?
47 hours

13. **Found Your Funding:** Over 10 days, a 4th-grade class of 71 students collected \$24 each. Each student collected the same number of cans each day. How many cans did they collect per day? How many did each student collect per day? Write your work.
Sample answer: Divide to find that $4,914 \div 18 = 273$. There are 273 cans per day. Each student collected 12 cans per day.

Reflect

How can you represent division using 2-digit dividend boxes?
Answers may vary.

Maths **Mindset**
 How can you represent long division using 2-digit dividend boxes?

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Practice

Build Fluency from Understanding

Common Error: Exercises 1–12 When using an area model to divide, students may often choose partial quotients that yield a product greater than the remaining area. Instead, students should choose partial quotients that yield products that are significantly less than the remaining area.

Practice Item Analysis

Item	DOK	Rigor
1–4	1	Procedural Skill and Fluency
5–9	2	Application
10	1	Conceptual Understanding
11–12	2	Application
13	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you represent division involving 2-digit divisors?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What is your responsibility in building a safe classroom culture?

Students reflect on how they practiced responsible decision-making.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can use an area model to determine partial quotients and add partial quotients to calculate the quotient.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Represent division of 2-digit divisors	5.NBT.B.6
2	2	Represent division of 2-digit divisors	5.NBT.B.6
3	2	Represent division of 2-digit divisors	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the D or F activities
2 of 3	<i>Take Another Look</i> or any of the D activities
1 or fewer of 3	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- D Build Proficiency
- F Extend Thinking



Lesson 7-4
Exit Ticket

Name: _____

- What is the quotient for 2,380 ÷ 57? Use an area model to solve.

R 41

D 42

F 43

R 44

- The area of the rectangular gym floor is 3,344 square meters. The width of the gym floor is 28 meters. What is the length of the gym floor? Use an area model to solve.

R 121 meters

- A high school football stadium can hold 69,000 people. There are 46 sections, and each section has seats for the same number of people. How many people can sit in each section? Use an area model to solve.

R 1,478 people

Reflect On Your Learning

How confident? D F R P

How well learning? D F R P

I understand D F R P

Open math resources D F R P

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R Reinforce Understanding

SMALL GROUP

Apply It!

Work with students in groups. Provide students with base ten blocks. Write a few division expressions (that have no remainder) that represents a 3- or 4-digit number divided by a 2-digit number. Students should work together to model the expression by dividing base ten blocks into equal groups of that size, or equally into that many groups. Help students write the division expression that goes with the base ten blocks.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Divide by 2-Digits (Area Models)



INDEPENDENT WORK

Differentiation Resource Book, p. 69

Lesson 7.6 • Division Understanding

Represent Division of 2-Digit Divisors

Name _____

Review

Use base ten blocks with divisors that are multiples of 10 when making your area models to find a quotient.

$182 \div 14 = 13$

$30 \times 3 = 90$	40	$= 120$
$70 \times 3 = 210$	10	$= 280$
$150 \times 3 = 450$	20	$= 630$

$700 \div 50 = 14$

Find each quotient. Use an area model to solve. **Sample answers given. Check students' models.**

1. $600 \div 24 = 25$

$30 \times 24 = 720$	20	$30 \times 24 = 720$	30
$6 \times 24 = 144$	+ 5	$3 \times 24 = 72$	+ 3

2. $4,512 \div 7 = 644$

$60 \times 74 = 4,380$	30	$30 \times 74 = 2,220$	30
$10 \times 74 = 740$	+ 2	$9 \times 74 = 666$	+ 1

3. $2,718 \div 54 = 50$

$30 \times 54 = 1,620$	30	$30 \times 54 = 1,620$	30
$9 \times 54 = 486$	+ 10	$9 \times 54 = 486$	+ 10

4. $1,154 \div 23 = 50$

$30 \times 23 = 690$	20	$30 \times 23 = 690$	30
$6 \times 23 = 138$	+ 3	$6 \times 23 = 138$	+ 3

Differentiation Resource Book

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Division with 2-Digit Divisors Task Cards
Students practice dividing with 2-digit divisors by using base-ten blocks.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 69–70

Lesson 7.6

Additional Practice

Name _____

Review

You can use multiplication to help you find a quotient. An area model can help you to keep track of the partial products.

The area of a rectangle is 1,566 square feet. The width of the rectangle is 36 feet. What is the length?

To solve, find the quotient $1,566 \div 36 = 43$. Use an area model.

$30 \times 36 = 1,080$	30	$30 \times 36 = 1,080$	30
$6 \times 36 = 216$	+ 6	$6 \times 36 = 216$	+ 6
$1 \times 36 = 36$	+ 1	$1 \times 36 = 36$	+ 1

The partial products add to 1,566. The factors used add to equal the quotient of 43.

The length of the rectangle is 43 feet.

Find the quotient. Use an area model to solve. **Sample area models shown.**

1. $1,101 \div 41 = 27$

$30 \times 41 = 1,230$	20	$30 \times 41 = 1,230$	30
$3 \times 41 = 123$	+ 3	$6 \times 41 = 246$	+ 6

2. $1,754 \div 23 = 76$

$30 \times 23 = 690$	20	$30 \times 23 = 690$	30
$6 \times 23 = 138$	+ 3	$6 \times 23 = 138$	+ 3

Student Practice Book

Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with addition and subtraction of decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



Student Practice Book, pp. 69–70

Find each quotient. Use an area model to solve.

1. $270 \div 12 = \underline{25}$ 2. $180 \div 24 = \underline{34}$

3. $270 \div 12 = \underline{47}$ 4. $442 \div 14 = \underline{82}$

3. The width of a rectangular park is 652 meters long. The park is 40 feet long. How wide is the park?
 $\underline{49}$ feet

4. The perimeter of a square is 4,164 meters. The perimeter of a square is 4 times the length of one side. How long is one side of the square?
 $\underline{74}$ feet

Math in Motion Activity

Use a number line to solve each problem. Show your work. Record your answer on the number line.

1. $270 \div 12 = 25$

2. $180 \div 24 = 34$

3. $270 \div 12 = 47$

4. $442 \div 14 = 82$

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M

Extend Thinking

Use It! Application Station

Online Learning: Is It Safe? Students write rules for safely using electronic devices and practice their rules by researching how to divide multi-digit numbers. *The content of this card has concepts covered later in Lesson 7-6. You may want to assign this card to students ready to explore content covered later in this unit.*



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



GO ONLINE

Differentiation Resource Book, p. 70

Lesson 7-4: Extend Thinking

Represent Division of 2-Digit Divisors

Divide.

Complete each area model. Write the resulting quotient.

1. $388 \div 16 = 24 \text{ R } 8$ 2. $508 \div 17 = 29 \text{ R } 15$

3. $2,205 \div 35 = 63$ 4. $2,908 \div 74 = 39 \text{ R } 12$

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INDEPENDENT WORK

Use Partial Quotients to Divide

Learning Target

- I can record partial quotients using a strategy.

Standards • Major • Supporting • Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations rectangular arrays, and/or area models.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Look for and express regularity in repeated reasoning.

Vocabulary

Math Term

partial quotients condition

Academic Terms

drawback

Materials

The materials may be for any part of the lesson.

- Blank Partial Quotients Teaching Resource*

Focus

Content Objective

- Students record partial quotients using a strategy.

Language Objectives

- Students discuss recording partial quotients while using the verb *relate*.
- To support optimizing output, students participate in MLR4: Info Gap.

SEL Objective

- Students exchange ideas for mathematical problem-solving with a peer, listening attentively and providing thoughtful and constructive feedback.

Coherence

Previous

- Students used place-value strategies to find quotients with up to 4-digit dividends and 1-digit divisor (Grade 4).
- Students extended their understanding of division to divide using an area model and partial quotients (Lesson 4).

Now

- Students use partial quotients to divide multi-digit dividends by 2-digit divisors to find quotients.

Next

- Students will divide multi-digit numbers by 2-digit numbers to find quotients with remainders (Lesson 6).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students understanding of division is enhanced as they divide multi-digit numbers using partial quotients.

Procedural Skill & Fluency

- Students gain skills and fluency with division as they repeat the process for using partial products throughout the lesson.

Application

- Students apply their understanding of division to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.



Number Routine

Find the Pattern, Make a Pattern

5–7 min

Build Fluency Students build reasoning skills as they determine a given pattern, find missing terms, and repeat the pattern with different numbers.

These prompts encourage students to talk about their reasoning:

- What do you notice about the numbers?
- To find a pattern, what did you consider first?
- What is another way to think about the pattern?
- How can you be sure your pattern is correct?



Purpose Students read a numberless word problem as they engage in contextual sense-making. They share thoughts on what math they see in the problem and describe the relationship between the quantities.

Numberless Word Problem

- What math do you see in this problem?

Teaching Tip You may want to have students work in pairs as they make sense of the context. Encourage them to think about quantities and their relationship.

1-17 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' thinking about the partial quotients strategy and are based on possible comments and questions that students may make during the share out.

- How can you describe this situation in your own words?
- How do you know what operation to use to solve the problem?
- What do you need to know to determine the solution?

Math is... Mindset

- What behaviors show respect towards someone?

1-18 Social Awareness: Ethical Responsibility

As students work with partners to complete the Numberless Word Problem routine, remind them to show respect by listening attentively when others are sharing their ideas. Provide models of constructive and respectful feedback to guide students. As students share the math they saw in the problem, encourage classmates to provide thoughtful feedback to one another. Remind students that respecting others is an important part of being a member of the class community.

Transition to Explore & Develop

Have students share their thoughts on what they think the quantities may be in the problem. Ask them to describe the relationship between the quantities in the problem. Explain that they are going to consider the same problem but with numbers this time.

1-19 Establish Goals to Focus Learning

- Let's think about a strategy we can use to divide multi-digit numbers.

Lesson 7-5
Use Partial Quotients to Divide

Be Curious
What math do you see in this problem?
An adult bison weighs 1,000 pounds. A calf weighs 200 pounds. How many calf weights fit into the weight of the adult bison?

Math is... Mindset
What behaviors show respect towards someone?

1-18 Social Awareness: Ethical Responsibility

Be Curious
What math do you see in this problem?
An adult bison weighs 1,000 pounds. A calf weighs 200 pounds. How many calf weights fit into the weight of the adult bison?

GO ONLINE

Learn
 Six adult bison weigh 1,752 pounds combined.
 How much does the larger calf weigh?
 You can use the bar quotients to solve division equations.



At the bottom left, a bar quotient is shown for $1,752 \div 12 = 146$. The bar is divided into 12 equal parts, with 146 written in each part. A box labeled 'MATH CONNECTION' asks 'When is another way to check multiplication appropriate?'.

Work Together
 What is the quotient of $2,052 \div 36$? Use the partial quotients strategy to help you solve the problem.

36	
$56 \times 36 = 1,296$	56
$12 \times 36 = 432$	12
$3 \times 36 = 108$	3
$1,056 + 432 + 108 = 1,596$	

At the bottom left, a bar quotient is shown for $2,052 \div 36 = 57$. The bar is divided into 36 equal parts, with 57 written in each part.

1 Pose the Problem

Pose Purposeful Questions

- Have you seen problems like this before? How were they similar? How were they different?
- What operation do you think you will use to solve this problem? Why do you think so?

2 Develop the Math

Choose the option that best meets your instructional goals.

Info Gap

Pair students. Provide Partner A with a problem like the one on the Learn page. Provide Partner B with the information to carry out the problem. Instruct Partner B to ask A what information they need, and for A to respond, explaining why they need it. Have students continue until the problem is completed.

3 Bring It Together

Elicit Evidence of Student Thinking

- What do you need to consider when choosing what partial quotient to use next?
- Could you use this model if the divisor was only 1-digit or was 3 or more digits? Explain.

Key Takeaway

- The quotients of multi-digit dividends and 2-digit divisors can be found using partial quotients.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of using the partial quotients strategy to find the quotient of whole numbers with a 2-digit divisor.

Common Error Students need to make sure to add all of the partial quotients to find the quotient of the division problem when using the partial quotients strategy.

Language of Math

The division symbol \div is called an *obelus*, and was first used as a symbol for division in 1659 by Swiss mathematician Johann Rahn. The division symbol in this strategy separating the dividend and divisor has no name.

Activity-Based Exploration

Students explore using the *partial quotients* strategy to divide by 2-digit divisors by extending their understanding of using the partial quotients strategy to divide by 1-digit divisors.

Directions: Write the division equation $1,752 \div 4 = r$. In pairs, have students solve using the partial quotients strategy. Then, write the equation $1,752 \div 24 = w$. With their partner, have students first discuss a plan on how they could use the partial quotients strategy to solve a division problem with a 2-digit divisor. Have students test their plan to divide by a 2-digit divisor.

Implement Tasks That Promote Reasoning and Problem Solving

- What steps did you take to solve the equation?
- Do you think you could extend this understanding to solve a division equation with a 2-digit divisor?
- How was solving a division equation with a 2-digit divisor using the partial products strategy similar to solving a division equation with a 1-digit divisor? How was it different?

Math is... Generalizations

- How does using an area model relate to the partial quotients strategy?

Students use a representation to understand a strategy.

Activity Debrief: Ensure that students understand that using the partial quotients strategy to divide by a 2-digit divisor is an extension of their understanding of using partial quotients to divide by a 1-digit divisor.

Have students revisit the Pose the Problem question and discuss answers.

- How can you find the weight of the bison calf?

English Learner Scaffolds

Entering/Emerging Ensure understanding of (x) times as great as.... Using two containers and 24 counters, say *I have 24 counters*. Count them out. Say *I have 2 containers*. Say *The number of counters is 12 times as great as the number of containers*. Write $2 \times 12 = 24$. Then write $2 \times 7 = 14$. Point to each part as you ask *Is 7 fourteen times as great as 2?* (no) *Is 14 seven times as great as 2?* (yes)

Developing/Expanding Ensure understanding of (x) times as great as.... Using two containers and 24 counters, say *I have 24 counters*. Count them out. Say *I have 2 containers*. Say *The number of counters is 12 times as great as the number of containers*. Write $2 \times 12 = 24$. Then write $2 \times 7 = 14$. Say *Tell me about 14*. (It's seven times as great as 2). Provide a sentence frame if needed.

Guided Exploration

Students extend their understanding of division by 2-digit divisors. They use the *partial quotients* strategy to divide.

Use and Connect Mathematical Representations

- **Think About It:** How can you use a representation to help you make sense of the problem?
- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- Have the students estimate the solution. Ask:
 - What compatible numbers will you use to estimate the solution? Why?
 - How will basic facts and place-value patterns help you estimate the solution?
- Have students follow along using the *Blank Partial Quotients Teaching Resource*.
 - Why do you subtract each product from the dividend?
- Have students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

Math is... Generalizations

- How does the area model relate to the partial quotients strategy?

Students use a representation to understand a strategy.



Bridging/Reaching Ask students to demonstrate and say a sentence using (x) times as great as. Then ask students to list other phrases that are similar in meaning (*more*, *greater than*, etc.), and to share their list with the class. Allow students to use a dictionary or thesaurus if desired.

On My Own

Name _____

What is the quotient? Use partial quotients to solve.

1. $354 \div 18 = 19$ 2. $388 \div 16 = 24$

3. $175 \div 21 = 8$ 4. $343 \div 14 = 24$

5. **2014 Summer Sea** An environmentalist is studying bird numbers. Corbin & his son sailed back a 187 miles. Corbin's legs are 48 inches long. How long is the leg of the Corbin's?
31 years



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6. Would you have taken 2,500 photographs in the last 4 days? Explain how the same number of photos can be taken each day, and how many photos you can take each day.

63 photographs

7. Give three examples of the Appalachian Trail in any 50 miles. How many kilometers are there? How many miles are there? How many kilometers are there? How many miles are there?



64 kilometers a day

8. What partial quotient would you use to find the quotient of $1,218 \div 6$? **Sample answer: $2,000 \div 6 = 333$, $130 \div 6 = 21$, and $18 \div 6 = 3$. The quotient is 204.**

9. **Extend Your Thinking** Over 17 weeks last year, Emily worked 2,004 hours. She earned \$4 per hour. Emily worked the same number of hours each week. How much did she earn each week? How many hours per week did she work? Show your work. **Sample answer: Divide to find that $2,004 \div 17 = 364$. Then divide to find $364 \times 4 = 1,456$. Emily worked 364 hours per week.**

Reflect

How does using the partial quotients strategy help you divide?
Answers may vary.

Math is... Mindset

Remember your mathematical abilities. You are capable. You are a problem solver.

Practice

Build Fluency from Understanding

Common Error: Exercises 1–4 When using the partial quotients strategy to solve division problems, students may make subtraction or place value errors. They should always assess the reasonableness of their calculated quotients using estimates or check their calculated quotients by multiplying the quotient by the divisor.

Practice Item Analysis

Item	DOK	Rigor
1–4	2	Procedural Skill and Fluency
5–7	1	Application
8	2	Conceptual Understanding
9	3	Application

Reflect

Students complete the Reflect question.

- How does using the partial quotients strategy help you divide?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How have you behaved flexibly while working with others?

Students reflect on how they practiced social awareness.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can record the calculation of a multi-digit number divided by a 2-digit divisor using a partial quotients strategy.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Use partial quotients	5.NBT.B.6
2	2	Use partial quotients	5.NBT.B.6
3	3	Use partial quotients	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score 3		Then have students do	
3 of 3		Additional Practice	or any of the 1 or 2 activities
2 of 3		<i>Take Another Look</i>	or any of the 2 activities
1 or fewer of 3		Small Group Intervention	or any of the 3 activities

Key for Differentiation

- 1 Reinforce Understanding
- 2 Build Proficiency
- 3 Extend Thinking



Lesson 7-5
Exit Ticket

Name: _____

1. What quotient is shown by the partial quotients algorithm?

A. $47 \div 232 = 20$

B. $1,234 \div 41 = 30$

C. $1,234 \div 41 = 30$

D. $1,234 \div 41 = 30$

2. What is the quotient for $3,052 \div 37$ use the partial quotients algorithm.

A. 80 B. 70 C. 70 D. 81

3. The cost of a rectangular board is 2,352 square inches. The area of the board is 49 inches. What is the length of the board? Use the partial quotients algorithm.

62 inches

Reflect On Your Learning

No confidence The job is getting I understand I can teach someone else

○ ————— ○ ————— ○ ————— ○

Assessment Source: Eureka Math

R Reinforce Understanding

SMALL GROUP

Pass It On!

Work with students in groups. Provide each student with a division problem with a 3- or 4-digit dividend and a 2-digit divisor such that there will be no remainder. Each student finds the first partial quotient for their problem before passing the paper to the left. If students are unsure about the previous result, help them check and, if necessary, correct it before they complete the next step. Continue until all solutions are reached.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Divide by 1-Digit (Partial Quotients)



INDEPENDENT WORK

Differentiation Resource Book, p. 71

Lesson 7.6 • Reinforce Understanding
Use Partial Quotients

Name: _____

Review
You can use partial quotients to divide.

$3468 \div 64 = 54$

$3468 \div 64 = 54$

Find each quotient. Use the partial quotients algorithm to solve.
Sample partial quotients given.

1. $782 \div 34 = 23$

2. $2,070 \div 45 = 46$

3. $885 \div 45 = 19$

4. $1,680 \div 28 = 60$

5. $1,500 \div 25 = 60$

6. $1,500 \div 25 = 60$

7. $1,500 \div 25 = 60$

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99. $1,500 \div 25 = 60$

100. $1,500 \div 25 = 60$

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Division with 2-Digit Divisors Race
Students practice dividing by 2-digit divisors.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 71–72

Lesson 7.6
Additional Practice

Name: _____

Review
You can use the partial quotients algorithm to help you find a quotient.

The area of a rectangular field is 1,275 square feet. The width of the field is 45 feet. What is the length?

To solve, find the quotient $2,796 \div 48 = 58$. Use the partial quotients algorithm.

If the factors don't match along the side, subtract to find the quotient.

The length of the field is 58 feet.

Find the quotient. Use the partial quotients algorithm to solve.
Sample work is shown.

1. $812 \div 28 = 29$

2. $3,440 \div 40 = 86$

3. $812 \div 28 = 29$

4. $3,440 \div 40 = 86$

5. $812 \div 28 = 29$

6. $3,440 \div 40 = 86$

7. $812 \div 28 = 29$

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9. $812 \div 28 = 29$

10. $3,440 \div 40 = 86$

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95. $812 \div 28 = 29$

96. $3,440 \div 40 = 86$

97. $812 \div 28 = 29$

98. $3,440 \div 40 = 86$

99. $812 \div 28 = 29$

100. $3,440 \div 40 = 86$

E

Extend Thinking

Use It! Application Station

Estimate High School Density Students research the density of schools in 10 U.S. states.



Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with addition and subtraction of decimals.



WORKSTATIONS

Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



GO ONLINE

STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Student Practice Book, pp. 71–72

Find the quotient. Use the partial quotients algorithm to solve.
Check students' work.

1. $120 \div 30 = \underline{4}$ 2. $150 \div 30 = \underline{5}$

3. $1,200 \div 60 = \underline{20}$ 4. $3,000 \div 30 = \underline{100}$

5. Write the division cycle for $120 \div 30$. Show the steps. Use the steps to solve $1,200 \div 60$. Show the steps. Use the steps to solve $3,000 \div 30$. Show the steps.

96 points

Math @ Home Activity

With a partner, take a set of math cards and solve for each problem. Use the steps to solve each problem.

Student Practice Book

INDEPENDENT WORK

Differentiation Resource Book, p. 72

Lesson 3.5 • Extend Thinking
Use Partial Quotients

Find each quotient. Check your answers in the number line.
Answers can be written horizontally, vertically, or diagonally.

1. $90 \div 30 = \underline{3}$ 2. $180 \div 20 = \underline{9}$

3. $1,200 \div 60 = \underline{20}$ 4. $3,000 \div 30 = \underline{100}$

5. $24 \div 4 = \underline{6}$ 6. $1,200 \div 60 = \underline{20}$

7. $3,000 \div 30 = \underline{100}$ 8. $180 \div 20 = \underline{9}$

Complete the table below with your grid numbers.
Possible answers:

1. 120 ÷ 30	2. 150 ÷ 30	3. 1,200 ÷ 60	4. 3,000 ÷ 30
24, 30, 60	21, 24, 27	24, 60, 60	60, 75
60	60, 75		

Write the number and tell the part of the number. **75**

Differentiation Resource Book

Divide Multi-Digit Whole Numbers

Learning Target

- I can use partial quotients to solve division problems, which sometimes include a remainder.

Standards

Major Supporting Additional

Content

- 5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- 5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or models.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Use appropriate tools strategically.

Vocabulary

Math Terms Academic Terms

partial quotients address

remainder

advantage

Materials

The materials may be for any part of the lesson.

- base-ten blocks

Focus

Content Objective

- Students solve division problems using partial quotients, which sometimes include remainders.

Language Objectives

- Students explain how to solve division problems using partial quotients, which sometimes include remainders, using *If...then*.
- To support maximizing linguistic and cognitive meta-awareness, ELs participate in MLR5: Co-Craft Questions and Problems.

SEL Objective

- Students set a focused mathematical goal and make a plan for achieving that goal.

Coherence

Previous

- Students used place-value strategies to find quotients with up to 4-digit dividends and 1-digit divisors (Grade 4).
- Students used partial quotients to divide multi-digit numbers by 2-digit divisors to find quotients (Lesson 5).

Now

- Students divide multi-digit numbers by 2-digit numbers to find quotients with remainders.

Next

- Students will solve word problems involving division by 2-digit numbers and interpreting remainders (Lesson 7).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of division as they represent multi-digit division by 2-digit divisors.

Procedural Skill & Fluency

- Students build proficiency by using partial quotients to represent division with remainders.

Application

- Students apply their understanding of division to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine

Decompose It 5-7 min

Build Fluency Students build number sense as they decompose the number 1,125 in at least 3 different ways.

These prompts encourage students to talk about their reasoning:

- What do you notice about the number?
- How did you determine the different decompositions?
- How could you use this decomposition to create another decomposition?





Purpose Students focus their thinking on what it means when a remainder is present in division by considering two completed partial quotients algorithms – one with a remainder, and one without.

Numberless Word Problem

- What math do you see in this problem?

Teaching Tip You may want to have students work in pairs as they discuss the situation and the math they see in the problem. Encourage them to think about what a remainder is, and how the algorithm shows remainders.

1.1 Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of remainders and the partial quotients strategy and are based on possible comments and questions that students may make during the share out.

- What operation could be used to solve this problem?
- How does “left over” sound like something you have already seen in division problems?

Math is... Mindset

- What actions can help you achieve your day's goal?

1.2 Self-Management: Goal Setting

Before students begin the Numberless Word Problem routine, invite them to share or write down one mathematical goal they have for the day. Have students create a plan for how they will work toward achieving their goal. Encourage students to focus their goals around dividing multi-digit whole numbers.

Transition to Explore & Develop

To make sure students are ready to focus on remainders rather than the strategy, have them as a class summarize the partial quotients algorithm.

1.3 Establish Goals to Focus Learning

- Let's talk about situations where the partial quotients strategy leaves a remainder, and what that means.

Lesson 7-6
Divide Multi-Digit Whole Numbers

Be Curious

What math do you see in this problem?

What are some things you notice about the stack of tortillas?

Math is... Mindset

Be Curious

What math do you see in this problem?

What are some things you notice about the stack of tortillas?

GO ON!

Learn

Rahim had 10 bags of tortillas. He has eaten half of the tortillas and gave the other half to his friends.

What are two ways to find out how many tortillas he has left?



Problem 1: If Rahim uses the bags that hold 10 tortillas, $20 \div 10 = 2$

Problem 2: If Rahim uses the bags that hold 10 tortillas, $20 \div 10 = 2$

He will have 2 tortillas left over.

He will have 10 tortillas left over.

Work Together

What is the quotient?

$16 \div 4 = 4$

1 Pose the Problem

Pose Purposeful Questions

- What does it mean to have “none left over”?
- In this problem, why might Rahim not want to have any left over tortillas?
- Have you seen a problem like this before? How is this problem different?

2 Develop the Math

Choose the option that best meets your instructional goals.

Co-Craft Questions and Problems

Pair students and have them co-create a problem similar to the one on the Learn page. Have them work together to solve their problem and then trade their problem with another pair. After each pair solves the other pair’s problems, have them form a group of four to check solutions and correct any mistakes that may have been made. Revisit the routine throughout the lesson for reinforcement.

3 Bring It Together

Elicit Evidence of Student Thinking

- How do you know when a quotient includes a remainder?
- How could you describe to a friend what a remainder is?

Key Takeaway

- When dividing multi-digit dividends and 2-digit divisors, the quotient sometimes includes a remainder.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students’ understanding of using the partial quotients algorithm to find the quotient of whole numbers with a 2-digit divisor including where there is a remainder.

Common Error Students need to make sure to add all of the partial quotients to find the quotient of the division problem when using the partial quotients algorithm.

Language of Math

In mathematics, a *remainder* is the amount left over. Here, it is the amount left over in a division problem. In a subtraction problem, the amount left over, or the remainder, is called the *difference*.

Activity-Based Exploration

Students explore using the *partial quotients* strategy with remainders.

Directions: Have students work together to solve the Pose the Problem. Students may use any strategy to divide.

Support Productive Struggle

- How is your solution method similar to a classmate's solution method? How is it different?
- When dividing using the partial quotients strategy how do you know what to do next?
- How do you know when to stop dividing when using partial quotients?
- How can you explain to a classmate what it means when you have a remainder?
- Is your calculated quotient reasonable? How do you know?

Math is... Choosing Tools

- How can you check your solution when there is a remainder?

Students detect possible errors by strategically using mathematical knowledge.

Activity Debrief: Have students share their solutions. Encourage students to defend their argument using mathematically precise language.

Guided Exploration

Students extend their understanding of division by 2-digit divisors. They use the *partial quotients* strategy to divide.

Facilitate Meaningful Discourse

- Have the students create the equation for the larger bags. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- **Think About It:** Would estimating the quotient help you solve this problem? Why or why not?
- Have the students create the equation for the smaller bags. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?
- **Think About It:** What multiples of 12 can you use to help you divide?

Math is... Choosing Tools

- How can you check your solution when there is a remainder?

Students detect possible errors by strategically using mathematical knowledge.



English Learner Scaffolds

Entering/Emerging Ensure understanding of *(none) left over* using counting chips. Say *I have 20 chips*. Then hand out 15 to different students. Say *I have five left over*. Hand out the rest of your chips. Show your empty hands. Say *I have no chips. I have none left over*. Repeat twice with a new amount of chips, once giving away all your chips, and once keeping a few. Say *I have none left over*. Yes or No?

Developing/Expanding Ensure understanding of *(none) left over* using counting chips. Say *I have 20 chips*. Then hand out 15 to different students. Say *I have five left over*. Hand out the rest of your chips. Show your empty hands. Say *I have no chips. I have none left over*. Repeat once. Then ask students to demonstrate none left over, providing sentence frames for students who need more guidance.

Bridging/Reaching Ask students to demonstrate and use *none left over* in a sentence. Then have students come up with similar words and phrases to *none* (*zero, not any, etc.*) and *left over* (*remaining, more, etc.*). Allow students to use a dictionary or thesaurus if desired.

On My Own

Name _____

What is the quotient?

1. $754 \div 14 = \underline{53}$ 3. $5,029 \div 42 = \underline{120}$

2. $975 \div 44 = \underline{22 \text{ R}15}$ 4. $2,244 \div 27 = \underline{83 \text{ R}6}$

3. Error Analysis In this division problem, explain the error and show the correct quotient.

$$\begin{array}{r} 32 \overline{) 1,175} \\ \underline{-6,400} \\ 5,350 \\ \underline{-5,280} \\ 70 \\ \underline{-70} \\ 0 \end{array}$$

The remainder is greater than the divisor, so the division cannot be correct. The quotient should be 32 R15.

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4. Jay's team is having a race that lasts 1,023 yards over 18 laps. How long is the course. They agree to distribute the race equally to 18 equal laps. How far, in yards, does they get swimming? **57 laps**

5. One bridge is designed to carry 4,320 tons. It is 48 miles in long as another nearby bridge. How long is the second bridge? **The second bridge is 180 miles long. Divide 4,320 by 48 using the partial quotients strategy to find the length of the shorter bridge.**

6. Ann has a collection of 200 trading cards. Her friends Ayud and Sam have 20 trading cards in each box. How many boxes will Sam and Ayud have if they trade cards with her? **10 boxes with 10 left over**

7. **Second-Step Thinking** A farmer has 475 chickens. She wants to put the same number of chickens in each cage with 10 chickens left over. How many cages will she need? Explain your answer. **58. Divide 475 by 10 and 475 by 15. When you divide 475 by 10, there are 47 quotients left over and 75 full cages. When you divide 475 by 15, there are 31 quotients left over and 55 full cages.**

Reflect

How can you tell if there is a remainder when dividing using a partial quotients strategy?

Answer: They vary.

Math is... Mindset

What does your answer suggest you will do next time you do this problem?

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Practice

Build Fluency from Understanding

Common Error: Exercises 3–4 Students may have difficulty determining the remainder. Remind students to keep finding partial quotients until the number remaining is less than the divisor.

Practice Item Analysis

Item	DOK	Rigor
1–4	1	Procedural Skill and Fluency
5	2	Conceptual Understanding
6–8	2	Application
9	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- How can you tell if there is a remainder when dividing using the partial quotients strategy?

Ask students to share their reflections with their classmates.

Math is... Mindset

- What actions helped you achieve your day's goals?

Students reflect on how they practiced self-management.

Learning Target

Ask students to reflect on the Learning Target of the lesson.

- I can use partial quotients to solve division problems, which sometimes include a remainder.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	1	Divide multi-digit whole numbers with remainders	5.NB.B.6
2	2	Divide multi-digit whole numbers with remainders	5.NBT.B.6
3	2	Divide multi-digit whole numbers with remainders	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
3 of 3	Additional Practice or any of the P or E activities
2 of 3	<i>Take Another Look</i> or any of the P activities
1 or fewer of 3	Small Group Intervention or any of the R activities

Key for Differentiation

- R Reinforce Understanding
- P Build Proficiency
- E Extend Thinking



Lesson 7-6
Exit Ticket

Name _____

- Which quotient is shown by the partial quotient strategy?
 - A. $73 \div 4275 = 42$
 - B. $4275 \div 73 = 42$
 - C. $4275 \div 73 = 42R12$
 - D. $4275 \div 73 = 42R12$
- What is the quotient for $2,887 \div 487$ using the partial quotient strategy?
 - A. 59 R55
 - B. 59
 - C. 59 R17
 - D. 59 R12
- 48 apples cost \$1.20. 420 apples cost \$1.08. Each bag holds 36 apples. How many bags are in the left order? How many apples were left over? Use the partial quotient strategy.

122 bags were filled with 3 apples left over.

Reflect On Your Learning

How confident? 1 2 3 4

How well learning? 1 2 3 4

How much practice will? 1 2 3 4

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R Reinforce Understanding

SMALL GROUP

Partial Quotients Division

Work with pairs of students. Have students work together to write a word problem in which a 3-digit number is divided by a 2-digit divisor, then use partial quotients to solve the problem. Make sure students recognize that there may be more than one way to write the problem using partial quotients.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Divide by 2-Digit (Partial Quotients)



INDEPENDENT WORK

Differentiation Resource Book, p. 73

Lesson 3-6 • Reinforce Understanding
Divide Multi-Digit Whole Numbers
 Name: _____

Review
 You can use partial quotients to divide.

$175 \div 10 = 17$

$175 \div 10 = 10 + 75$

Use partial quotients to solve. Find the answers with these numbers. **Sample partial quotients shown.**

$\begin{array}{r} 17 \\ 10 \overline{) 175} \\ \underline{-70} \\ 10 \\ \underline{-10} \\ 0 \end{array}$	$\begin{array}{r} 17 \\ 20 \overline{) 340} \\ \underline{-200} \\ 140 \\ \underline{-140} \\ 0 \end{array}$
$\begin{array}{r} 17 \\ 10 \overline{) 175} \\ \underline{-10} \\ 75 \\ \underline{-70} \\ 5 \\ \underline{-5} \\ 0 \end{array}$	$\begin{array}{r} 17 \\ 20 \overline{) 340} \\ \underline{-200} \\ 140 \\ \underline{-140} \\ 0 \end{array}$

1. $175 \div 10 = 17$ **2. $340 \div 20 = 17$**

3. $615 \div 10 = 61$ R 5 **4. $320 \div 10 = 32$ R 0**

5. $615 \div 10 = 61$ R 5 **6. $320 \div 10 = 32$ R 0**

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B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Remainder Showdown

Students practice dividing by 2-digit numbers.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



INDEPENDENT WORK

Student Practice Book, pp. 73–74

Lesson 3-6
Additional Practice
 Name: _____

Review
 You can use the partial quotients algorithm to help you find a quotient and any remainder.

Jerry had 275 marbles. He gives them 10 bags with 10 marbles in each bag. How many bags will Jerry have? How many marbles will he have left over?

To solve, find the quotient $275 \div 10 = 27$ R 5. Use the partial quotients algorithm.

$$\begin{array}{r} 27 \\ 10 \overline{) 275} \\ \underline{-200} \\ 75 \\ \underline{-70} \\ 5 \end{array}$$

Practice using different strategies to solve each problem. If you can't do the problem, try it again.

1. $275 \div 10 = 27$ R 5 **2. $340 \div 20 = 17$ R 0**

3. $615 \div 10 = 61$ R 5 **4. $320 \div 10 = 32$ R 0**

5. $615 \div 10 = 61$ R 5 **6. $320 \div 10 = 32$ R 0**

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97. $615 \div 10 = 61$ R 5 **98. $320 \div 10 = 32$ R 0**

99. $615 \div 10 = 61$ R 5 **100. $320 \div 10 = 32$ R 0**

Solve Problems Involving Division

Learning Targets

- I can use solve word problems involving division.
- I can interpret the remainder when solving word problems.

Standards Major Supporting Additional

Content

- **5.NBT.B** Perform operations with multi-digit whole numbers and with decimals to hundredths.
- **5.NBT.B.6** Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or models.

Math Practices and Processes

MPP Make sense of problems and persevere in solving them.

MPP Reason abstractly and quantitatively.

Vocabulary

Math Term

remainder

Academic Terms

note

transition

Materials

The materials may be for any part of the lesson.

- none

Focus

Content Objectives

- Students solve word problems involving division.
- Students interpret the remainder, when necessary, to solve problems.

Language Objectives

- Students talk about solving word problems involving division while using the modals *can* and *could*.
- To support sense-making, ELs participate in MLR6: Three Reads.

SEL Objective

- Students break down a situation to identify the problem at hand.

Coherence

Previous

- Students used place-value strategies to find quotients with up to 4-digit dividends and 1-digit divisors (Grade 4).
- Students divided multi-digit numbers by 2-digit numbers to find quotients with remainders (Lesson 6).

Now

- Students solve word problems involving division by 2-digit numbers and interpreting remainders.

Next

- Students will solve problems involving division with decimals to hundredths (Unit 8).
- Students will fluently divide multi-digit numbers using the standard algorithm (Grade 6).

Rigor

Conceptual Understanding

- Students build on their understanding of division as they represent multi-digit division by 2-digit divisors.

Procedural Skill & Fluency

- Students build proficiency by using partial quotients to represent division with remainders.

Application

- Students will apply their understanding of division to solve problems with real-world contexts.

Application is not a specific element of rigor for this standard.

Number Routine
Decompose It  5–7 min

Build Fluency

Students build number sense as they decompose the number 4.53 in at least 3 different ways.

These prompts encourage students to talk about their reasoning:

- What do you notice about the number?
- How did you think about the number before decomposing it?
- How could you use one way to decompose to create another one?
- What other ways have you decomposed the number?
- Do you notice any patterns in your list of decomposed examples? Explain.



Purpose Students make sense of a situation without focusing on the numbers.

Numberless Word Problem

- What's the question?

Teaching Tip Encourage students to discuss their understanding of the numberless word problem, and what information would be needed to solve such a problem.

Pose Purposeful Questions

The questions that follow may be asked in any order. They are meant to help advance students' understanding of remainders and the partial quotients algorithm in the context of word problems and are based on possible comments and questions students may make during the share out.

- What information do you need to determine how many nights Javier can afford to stay at the hotel?
- What operation could you use to solve a problem like this?

Math is... Mindset

- How can you help identify a problem in your class or community?

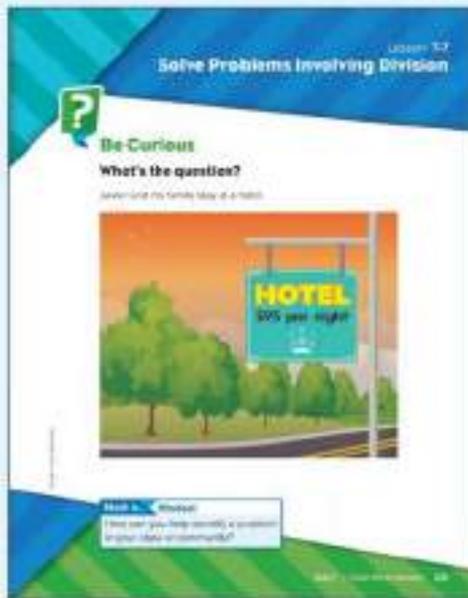
Responsible Decision Making: Identify Problems

Help students develop strong learning habits by providing them opportunities to practice responsible decision-making skills. As students consider the Numberless Word Problem routine, invite them to share what information is most useful to identify the mathematical task at hand.

To make sure students are ready, have them as a class summarize the types of questions that a division word problem could ask.

Establish Goals to Focus Learning

- Let's think about how to identify what to do with the remainder in a division word problem.



Lesson 7-7
Solve Problems Involving Division

Be Curious
What's the question?
Javier and his family stay at a hotel.

Think In... **Wonder**
Does your family usually go to hotels? How often?



Be Curious
What's the question?
Javier and his family stay at a hotel.

GO ON!

Learn

Clara and her family have \$120.00 to pay for their vacation hotel.

Will they be able to stay at the hotel for 12 nights?

A division equation can represent the problem.

Problem Solving

What are some different ways you can solve this problem?

$120 \div 10 = 12$

One strategy is to use partial quotients.

$\begin{array}{r} 10 \overline{) 120} \\ \underline{100} \\ 20 \\ \underline{20} \\ 0 \end{array}$

The remainder is 0. The quotient is 12.

Clara and her family can stay at the hotel for 12 nights only. They will have \$0 left.

Summarize it by making up the longest remainder to solve problems.

Work Together

There are 1200 guests attending a city park race the track for 75 seats.

How many seats will they need to seat everyone? Will all the seats from the same number of seats?

22 Jaws: Sample answer: Not all the rows will have the same number of seats because the quotient has a remainder of 2.

1 Pose the Problem

Pose Purposeful Questions

- Are you trying to find the number of groups or the size of each group?
- How is this problem similar to others you have solved in this unit? How is it different?

2 Develop the Math

Choose the option that best meets your instructional goals.

Three Reads

1st read: Instruct students to look at the Work Together problem on the Learn page. Ensure students understand the situation and key words: *attend*, *row*, and *seat*.

2nd read: Focus students' attention on the *How many...* question.

3rd read: Brainstorm with students ways to solve the problem.

3 Bring It Together

Elicit Evidence of Student Thinking

- Why might it be important to be able to interpret the remainder when solving problems?
- How do you know whether the quotient, 1 more than the quotient, or the remainder is the answer?

Key Takeaways

- Problems involving division can be solved using known strategies for division.
- Some problems require interpreting the remainder when determining the solution.

Work Together

The Work Together activity can be used as a formative assessment opportunity to check students' understanding of how to interpret the quotient of a division word problem when there is a remainder.

Common Error Students may always round a quotient to the nearest whole, instead of considering whether they may need to round up or down given the situation.

Language of Math

Remainder comes from the word *remain*. A part that has not been destroyed, taken, or used up is something that remains. The ruins are all that remains of old buildings that are mostly destroyed.

Activity-Based Exploration

Students solve division word problems.

Materials: *Problem-Solving Tool* Teaching Resource

Directions: Provide copies of the *Problem-Solving Tool* Teaching Resource. Have students work together to solve the Pose the Problem.

Math is... Planning

- What are some different ways you know to determine a quotient?

Support Productive Struggle

- What strategies have you tried to use to solve the problem? Why do you think those strategies did not work?
- How does your solution method compare to others?
- How else could you have arrived at your answer?
- Does your answer seem reasonable? How do you know?

Students look for entry points for a problem's solution.

Activity Debrief: Have students share their solutions and strategies to solving the problem. Encourage students to find similarities and differences among the solution methods.

A PDF of the Teaching Resource is available in the Digital Teacher Center.

Guided Exploration

Students extend their understanding of solving division word problems.

Facilitate Meaningful Discourse

- Why might it be important for Javier to determine how many nights he can stay at the hotel before booking his trip?
- Have the students create the equation. Ask:
 - What should the operation be? Why?
 - How should the numbers appear in the equation? Why?
 - How should the unknown appear in the equation? Why?

Math is... Planning

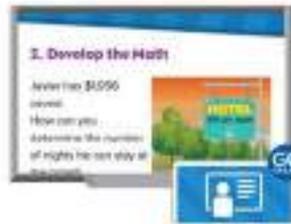
- What are some different ways you know to determine a quotient?

Students look for entry points for a problem's solution.

- Have the students estimate the solution. Ask:
 - What compatible numbers will you use to estimate the solution? Why?
 - How will basic facts and place-value patterns help you estimate the solution?
 - Why is 10 a good choice for the first partial quotient?
 - **Think About It:** How are the quotient of 11 and the remainder of 11 represented in the partial quotients algorithm?

- Have the students use their estimate to assess the reasonableness of the calculated solution. Ask:
 - Is the calculated solution reasonable? Why or why not?

- Have the students check if their calculated solution is correct. Ask:
 - How do you check if a quotient with a remainder is correct?



English Learner Scaffolds

Entering/Emerging Ensure understanding of *saved* with play money. Say *I want to save money to buy a new coat. It costs \$50. Show \$10. Say I'm going to save \$10 for my coat.* Put it aside. Show \$15. Say *I'm going to save \$15 more for my coat.* Put it aside. Say *I saved \$25 so far. I need \$25 more.* Repeat with a new item to save for. This time, ask *How much have I saved?*

Developing/Expanding Ensure understanding of *saved* with play money. Say *I want to save money to buy a new coat. It costs \$50. Show \$10. Say I'm going to save \$10 for my coat.* Put it aside. Show \$15. Say *I'm going to save \$15 more for my coat.* Put it aside. Say *I saved \$25 so far. I need \$25 more.* Repeat with a new item to save for. This time, ask students to tell you how much you have saved.

Bridging/Reaching Ask students what they would buy if they had any money saved. Then have them come up with synonyms (i.e., *set aside*) and antonyms (i.e., *spent*) for *saved*, and to share their list with the class. Allow students to use a dictionary or thesaurus if desired.

On My Own

Name: _____

What is the quotient? Use pencil and paper to solve.

1. $483 \div 23 = 21 \text{ R}12$ 2. $1,042 \div 22 = 47 \text{ R}18$

3. Aya is a restaurant chef. She has given a budget of \$500 each year to buy \$100 worth of aprons. How many aprons can she buy each year? Explain your answer.

Aya can receive 50 aprons. Sample explanation:
 $500 \div 10 = 50 \text{ R}0$. She will have \$0 left over, which is not enough to receive another apron.

4. **STRA+PowerUpLearner** shows video of a producer program collecting 120 items. Each page contains 60 items. How many full pages of items does the producer have? Explain your answer.

2 full pages; Sample explanation: Since $120 \div 60 = 2 \text{ R}0$, the quotient tells the number of full pages. The remainder tells the number of items on the next page.



Unit 7 • Division Review 233

5. A farmer packs 1200 peaches in bins to take to the market. Each bin holds 30 peaches. How many bins will the farmer use to transport the fruit? Explain your answer. **71 bins; Sample answer:** 70 bins will hold most of the peaches, but 4 are left over so another bin is needed.

6. A farmer has 2,100 chickens. She puts the same number of chickens into 24 different pens. How many chickens are in each pen? Will she use all the pens? Explain your answer.

87.5 chickens; She will not use all her stickers. There are 15 stickers left over.

7. My uncle has to take 1,680 boxes to the store. One of his workers can take 40 boxes at a time. How many workers does he need to transport the boxes? Explain your answer.

42 workers; Sample answer: $1,680 \div 40 = 42 \text{ R}0$. There will be 0 boxes left, so no other bins are needed.

8. **Shared Your Thinking** There are 6,300 runners participating in a marathon. The runners will be divided into 12 groups with about the same number of runners in each group. How many runners will be in each group? Explain.

Sample answer: Because $6,300 \div 12 = 525 \text{ R}0$, there will be 525 groups of 12 runners with 0 runners remaining. One option for grouping is to have 120 groups with 52 runners and 1 group with 10 runners.

Reflect

What does this remainder tell you?
Answers may vary.

Check Your Work
 Check for accuracy, especially in problems that have a remainder.

Unit 7 • Division Review 234

Practice

Build Fluency from Understanding

Common Error: Exercises 3–7 Students may have difficulty interpreting the remainder. Remind students to consider the context of each problem. In Exercises 3 and 4, the context suggests rounding down (eliminating the remainder). In Exercise 7, the context suggests rounding up (if there is a remainder).

Practice Item Analysis

Item	DOK	Rigor
1–2	1	Procedural Skill and Fluency
3–7	2	Application
8	3	Conceptual Understanding

Reflect

Students complete the Reflect question.

- What does the remainder tell you?

Ask students to share their reflections with their classmates.

Math is... Mindset

- How did you help identify a problem in your class or community?

Students reflect on how they practiced responsible decision-making.

Learning Targets

Ask students to reflect on the Learning Targets of the lesson.

- I can solve word problems involving division.
- I can interpret the remainder when solving word problems.

To review today's lesson, have students watch the Math Replay video in their Digital Student Center.

Assign the On My Own practice to students from the Digital Teacher Center.



Exit Ticket ✔ Formative Assessment

The *Exit Ticket* assesses students' understanding of lesson concepts.

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Exit Ticket Skill Tracker

Item	DOK	Skill	Standard
1	2	Interpret remainders in division	5.NBT.B.6
2	2	Interpret remainders in division	5.NBT.B.6
3	2	Interpret remainders in division	5.NBT.B.6
4	2	Interpret remainders in division	5.NBT.B.6

Data Use students' scores on the *Exit Ticket* to assign the differentiated resources available. When students complete the *Exit Ticket* in the digital workspace, their responses are auto-scored.

Exit Ticket Recommendations

If students score	Then have students do
4 of 4	Additional Practice or any of the or activities
3 of 4	<i>Take Another Look</i> or any of the activities
2 or fewer of 4	Small Group Intervention or any of the activities

Key for Differentiation

- Reinforce Understanding
- Build Proficiency
- Extend Thinking



Lesson 7-7
Exit Ticket

Name: _____

- What is the quotient for $832 \div 487$? Give a word problem to help you solve.
15 R26
- Do you think a number divided by 100 is always evenly divided? Why or why not? Explain. How many colored pencils do you have? How many colored pencils do you have? **16 colored pencils**
- A company prints marketing copies and bundles in cartons of 48. How many cartons of marketing copies does the company need to print 4,800 copies? How many full cartons are able to be shipped out? **100 cartons**
- Why is it important for a teacher to have a plan for L2/L3 students and students in special needs? How do you plan? **45 buses**

Reflect On Your Learning

1 (not confident) 2 (not confident) 3 (confident) 4 (not confident)

Assessment Practice Book 188

R Reinforce Understanding

SMALL GROUP

Reminders

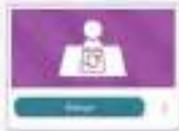
Work with students in pairs. Have students work together to write a word problem in which a 4-digit number is divided by a 2-digit divisor and the remainder matters, then solve the problem. Then work with students to adjust the problem to use different numbers to see how different remainders affect the solution.

GO ONLINE

Take Another Look Lesson

Assign the interactive lesson to reinforce targeted skills.

- Interpret Remainders in Word Problems



INDEPENDENT WORK

Differentiation Resource Book, p. 75

Lesson 3.7 • Reinforce Understanding
Solve Problems Involving Division

Review

A company is packaging a total of 1,037 balloons into bags which hold 32 balloons each. How many bags will the company use to package the balloons?

$$\begin{array}{r} 32 \overline{) 1037} \\ \underline{960} \\ 77 \\ \underline{64} \\ 137 \\ \underline{96} \\ 417 \\ \underline{320} \\ 97 \end{array}$$

Start by dividing from the group of 10 (one 1,000, 32 = 31 × 32) which is less than 1,000, 32 = 31 × 32 which is more than 1,000. So use 31 with 32. Then use the left up figure and how many times 32 will divide into 77. The result is 2 (two), leaving a remainder of 13.

Use partial quotients to help you solve. Record your thinking.

- A company is packaging balloons for sale. The company has a total of 1,037 balloons. Each package holds 32 balloons. How many packages of balloons will the company use to solve?

102 packages. Sample answer: There are 12 balloons left over after putting 2,448 balloons into 762 bags.
- What if the company puts packages that hold 25 balloons? How many packages of balloons will the company use to solve?

70 packages. Sample answer: There are 17 balloons left over after putting 2,450 balloons into 98 bags.
- The company wants to put the same number of balloons in each package with no balloons left over. Should the company use 30 or 35 balloons in each package?

30 balloons in each package. Sample answer: There are 34 balloons left over after putting 2,430 balloons into 76 bags. There are no balloons left over after putting 2,400 balloons into 75 bags.

Illustration: © iStockphoto.com

B Build Proficiency

WORKSTATIONS

Practice It! Game Station

Dividing with Remainders Bump
 Students practice identifying remainders in division problems.



GO ONLINE

Interactive Additional Practice

Assign the digital version of the Student Practice Book.



Student Practice Book, pp. 75–76

Lesson 3.7
Additional Practice

Review

You can use the partial quotients method to help you find a quotient and any remainder. Then you can interpret the remainder in the context of the problem to answer the question.

There are 322 chairs to be set up for a party. Each table holds 18 chairs. How many tables are needed to set up all of the chairs?

To solve, find how many 18's fit into 322 to find the quotient and remainder.

$$\begin{array}{r} 18 \overline{) 322} \\ \underline{180} \\ 142 \\ \underline{144} \\ -2 \end{array}$$

The tables are arranged along the side, and 2 will be the quotient. The 2 remaining chairs are remainder.

There will be 18 rows of 18 tables and 2 extra chairs. So 18 rows of tables are needed to arrange all the chairs.

- Roger wants to give the new computers. He has a budget of \$350 and can spend \$45 on each computer. How many computers can he buy? Explain your answer.

Roger can't buy 21 because Sample explanation: $350 \div 45 = 7 \text{ R } 35$. He will have \$35 left over, which is not enough to buy another computer.

Illustration: © iStockphoto.com

Use It! Application Station

That Is Astronomical Students practice finding quotients, rounding, and writing equations by researching the hours in a day for each planet.



Own It! Digital Station

Build Fluency Games

Assign the digital game to develop fluency with addition and subtraction of decimals.



Spiral Review

Assign the digital Spiral Review Practice to students or download and print PDFs of the Spiral Review from the Digital Teacher Center.



STEM Adventure

Assign a digital simulation to apply skills and extend thinking.



Student Practice Book, pp. 75–76

2. Write down and simplify. 20% eggs are collected. They are packaged into containers of 10 each. How many whole containers will they be able to fill?
34. Sample explanation: $255 \div 12 = 21 \text{ R } 3$. So 21 containers will be filled with 7 eggs left over, so only 24 containers will be filled.
3. A factory packs computer monitors. 1,400 extra balls need to be shipped out. They are packaged into containers of 20 balls each. How many whole containers will they be able to fill? How many extra balls will be left to ship out the next day?
- To solve this, sample explanation: $1,400 \div 20 = 70 \text{ R } 0$. So all full containers can be shipped out, and the remaining 0 extra balls will be part of the next day's shipment.
4. A farmer needs to collect 2,000 extra eggs. He has 100 extra eggs in each box. How many whole boxes will he need to collect all 2,000 extra eggs? Sample explanation: $2,000 \div 100 = 20 \text{ R } 0$. So there will be 20 full boxes, but the farmer needs another box for the remaining 0 extra eggs. So there needs to be 21 boxes.



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Differentiation Resource Book, p. 76

Lesson 7-7 • Extend Thinking

Solve Problems Involving Division

1. 100

1. There is going to be a party for 100 people. The caterer charges \$12.50 per person for the food. How much money will the caterer need to provide the food for 100 people? Sample answer: $100 \times 12.50 = 1,250$. So the caterer will need \$1,250.

All the packaging options result in a remainder of 2 cents. $1,354 \div 12 = 112 \text{ R } 2$. $1,354 \div 15 = 90 \text{ R } 4$. $1,354 \div 18 = 75 \text{ R } 4$.

2. Each student is making paper planes for the state science fair. They have 100 sheets of paper and need to make 100 planes. How many sheets of paper will they need to make 100 planes? Sample answer: $100 \div 1 = 100$. So they will need 100 sheets of paper.

The company with buses making 43 people. $125 \div 42 = 2 \text{ R } 41$, resulting in one bus with 41 empty seats. $125 \div 30 = 4 \text{ R } 5$, resulting in one bus with 5 empty seats.

3. A number divided by 27 results in a quotient of 16 with a remainder of 9. What is the number? Sample answer: 459 . Sample answer: $27 \times 16 + 9 = 459$.

4. A number divided by 12 results in a quotient of 16 with a remainder of 8. What is the number? Sample answer: 457 . Sample answer: $12 \times 16 + 8 = 457$.

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Collect and Assess Student Work

Collect and review student response to determine possible misconceptions. See examples in If-Then chart.

IF incorrect...	THEN the student likely ...	Sample Misconceptions
1. c 2. c	solves the division problem without applying an understanding of how the remainder connects to the context by keeping the remainder as part of the answer.	
1. b 2. a	solves the division problem without applying an understanding of how the remainder connects to the context by rounding up or down incorrectly.	
1. d 2. d	makes an error in the division process; OR does not recognize the problem context as a division situation.	
<p>has difficulty representing 1-digit or 2-digit division; OR solves the division problem correctly and interprets the remainder correctly, but considers more than one answer as correct; OR justifies both rounding down and rounding up. For example, in Item B, a student may circle both choice a for how many full cartons there are and choice b for how many total cartons there are.</p>		

Take Action

Choose from the following resources or suggestions:

- Revisit representing division with 2-digit divisors in Lessons 7-4–7-6.
- Use structured approaches that include asking students to estimate before computing, making a drawing to represent the situation, and comparing their final answer to their estimate.
- Discuss the meaning of a remainder by making explicit connections between a visual representation (such as area models) and the numeric representation.
- Discuss what the dividend, divisor, and quotient mean in the context of a real-world problem. Discuss the best way to describe the answer based on the problem context when there is a nonzero remainder. Ask, “Should we express the answer with a remainder, or should we round down or round up to the next whole number?” Ask students to write their own contexts for division problems.

Revisit the Probe After additional instruction, have students review their initial answers. Use these questions for discussion:

- *Are there any answers you would like to change? Explain.*
- *Are there any questions that you still have about any of the items on this probe?*

Metacognitive Check *Reflect on Your Learning* allows students to think about their level of understanding of the lesson content on a scale of 1 to 4 with 4 being the highest confidence.

Item Analysis (continued)

Item	DOK	Lesson	Standard
13	2	7-7	5.NBT.B.6
14	1	7-4	5.NBT.B.6
15	1	7-2	5.NBT.B.6
16	2	7-7	5.NBT.B.6
17	2	7-7	5.NBT.B.6

16. Jenney wants \$12 each hour working after she earned \$280 last month. For her monthly income she has multi-digit bills, mostly \$100 bills. How many bills will she need to cash? *Lesson 7-7*

17. Jenney has the best estimate of $1200 \div 28$ is 43. *Lesson 7-4*

18. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

19. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

20. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

21. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

22. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

23. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

24. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

25. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

26. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

27. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

28. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

29. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

30. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

31. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

32. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

33. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

34. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

35. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

36. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

37. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

38. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

39. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

40. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

41. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

42. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

43. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

44. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

45. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

46. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

47. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

48. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

49. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

50. Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

Performance Task

Standard: 5.NBT.AB.6

Rubric (4 points)

Part A (DOK 2) – 2 points

- 2 POINTS** Student's work reflects a proficiency with estimating quotients. The student's estimates are reasonable.
- 1 POINT** Student's work reflects developing proficiency with estimating quotients. One of the estimates is reasonable.
- 0 POINTS** Student's work reflects a poor understanding of estimating quotients. No estimates are reasonable.

Part B (DOK 2) – 2 points

- 2 POINTS** Student's work reflects a proficiency with multi-digit whole number division using partial quotients algorithm. The solution is accurate.
- 1 POINT** Student's work reflects developing proficiency with multi-digit whole number division using partial quotients algorithm. The solution is incorrect due to computational errors, not conceptual weakness.
- 0 POINTS** Student's work reflects a poor understanding of multi-digit whole number division using partial quotients algorithm. The solution is incorrect.

Reflect

The Reflect question provides an opportunity for students to express their understanding of the unit level focus question.

Performance Task

Jenny has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

Part A Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

Sample answer: about 50 bills

Part B Jenney has a budget of \$1000 to buy some multi-digit bills. She has some \$100 bills and some \$20 bills. How many \$20 bills can she buy? *Lesson 7-2*

Sample explanation: It is close to the estimate. Therefore, it is reasonable.

Reflect

How can I check multi-digit whole number division?

Answers may vary.

Unit 7
Fluency Practice

Name: _____

Fluency Strategy

You can use place value and properties of operations to multiply by multiples of 10.

$12 \times 7 = 84$ $120 \times 7 = 840$
 $12 \times 70 = 840$
 $120 \times 7 = 840$

Use place value to multiply by multiples of 10.

$12 \times 10 = 120$ $12 \times 100 = 1,200$
 $12 \times 1,000 = 12,000$

Use place value and properties of operations to multiply by multiples of 10.

$12 \times 4 = 48$ $12 \times 40 = 480$
 $12 \times 400 = 4,800$
 $12 \times 4,000 = 48,000$

Fluency Flash

Use the models to complete the multiplication equations.

$2 \times 3 = 6$
 $2 \times 30 = 60$
 $2 \times 300 = 600$

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Fluency Check

What is the sum, difference, or product?

1. $2 \times 40 =$ <u>80</u>	11. $18 \times 27 =$ <u>486</u>
2. $5 \times 30 =$ <u>150</u>	12. $2 \times 70 =$ <u>140</u>
3. $347 - 225 =$ <u>122</u>	13. $80 \times 5 =$ <u>400</u>
4. $7 \times 60 =$ <u>420</u>	14. $481 - 425 =$ <u>56</u>
5. $371 + 189 =$ <u>560</u>	15. $90 \times 3 =$ <u>270</u>
6. $1,023 + 456 =$ <u>1,479</u>	16. $4,015 + 225 =$ <u>4,240</u>
7. $63 \times 3 =$ <u>189</u>	17. $80 \times 8 =$ <u>640</u>

Fluency Talk

Explain how you can use properties of operations to find the product of a number and a multiple of 10.

Explanations may vary.

Describe what you can do to multiply when multiplying using place value.

Explanations may vary.

Fluency practice helps students develop procedural fluency, that is, the “ability to apply procedures accurately, efficiently, and flexibly.” Because there is no expectation of speed, students should not be timed when completing the practice activity.

Build Fluency Objective Students practice multiplying by multiples of 10.

Fluency Progression

Unit	Skill	Standard
1	Use Partial Sums to Add	4.NBT.B.4
2	Decompose by Place Value to Subtract	4.NBT.B.4
3	Use an Algorithm to Add	4.NBT.B.4
4	Use an Algorithm to Subtract	4.NBT.B.4
5	Choose a Strategy to Add	4.NBT.B.4
6	Choose a Strategy to Subtract	4.NBT.B.4
7	Multiply by Multiples of 10	5.NBT.B.5
8	Multiply by Multiples of 100	5.NBT.B.5
9	Divide Multiples of 10	5.NBT.B.6
10	Divide Multiples of 100	5.NBT.B.6
11	Use an Algorithm to Multiply (2- and 3-Digit Numbers by 1-Digit Numbers)	5.NBT.B.5
12	Use an Algorithm to Multiply (2-Digit Numbers by 2-Digit Numbers)	5.NBT.B.5
13	Choose a Strategy to Multiply	5.NBT.B.5
14	Choose a Strategy to Multiply	5.NBT.B.5

Fluency Expectations

Grade 4

- Add and subtract within 1,000,000.

Grade 5

- Multiply multi-digit whole numbers.

Grade 6

- Divide multi-digit numbers using the standard algorithm.
- Add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Performance Task

Locked Cashbox

Students draw on their understanding of dividing whole numbers. Use the rubric shown to evaluate students' work.

Standards: 5.NBT.B.6

Rubric (10 points)

Part A (DOK 3) – 2 points

2 POINTS Student's work reflects a proficiency in dividing multi-digit factors. The student was able to accurately provide 3 possible breakdowns.

1 POINT Student's work reflects a developing proficiency in dividing multi-digit factors. The student was able to accurately provide 2 possible breakdowns.

0 POINTS Student's work reflects a weak proficiency of dividing multi-digit factors. The student was able to accurately provide 1 or 0 possible breakdowns.

Parts B, C, and D (DOK 2) – 6 points

2 POINTS Student's work reflects a proficiency in dividing multi-digit factors. The student was able to accurately calculate an answer and given an explanation.

1 POINT Student's work reflects a developing proficiency in dividing multi-digit factors. The student was able to accurately calculate an answer but has given an incorrect explanation.

0 POINTS Student's work reflects a weak proficiency of dividing multi-digit factors. The student was able to accurately calculate an answer and has given a correct explanation.

Part E (DOK 3) – 2 points

2 POINTS Student's work reflects a proficiency in dividing multi-digit factors. The student's work, answer, and list are all correct.

1 POINT Student's work reflects a developing proficiency in dividing multi-digit factors. Some of the student's work, answer, and list are incorrect.

0 POINTS Student's work reflects a weak proficiency of dividing multi-digit factors. The student's work, answer, and list are all incorrect.

Unit 7
Performance Task

Name _____

Locked Cashbox

The Federal Reserve currently issues \$1, \$2, \$5, \$10, \$20, \$50, and \$100 bills. A cashbox has \$2,844 tucked into stacks up of 50¢ to 100-dollar denominations.

Part A

Lawrence is trying to give donations from different denominations (breakdowns) of the \$2,844 into at least 200 donations. How much cash will each denomination get? Consider all ways to meet conditions. For example, the cashbox contains 20 \$100 bills, 45 \$20 bills, and 44 \$1 bills.

Sample answer: 25 \$100 bills, 6 \$20 bills, and 4 \$1 bills;
40 \$50 bills, 8 \$100 bills, 44 \$1 bills;
20 \$100 bills, 100 \$5 bills, 4 \$1 bills.

Part B

It is possible for the cashbox to contain \$20 bills, \$20 bills, and \$100? Explain.

Yes: Sample answer: 70 \$20 bills, 3 \$20 bills, and 4 \$1 bills.

Part C

It is possible for the cashbox to only contain \$20 and \$1 bills?

No: Sample answer: There is a remainder of 4 when 2,844 is divided by 5.

Part D

It is possible for the cashbox to contain one bill of each 20 denominations? Explain.

Yes: Sample answer: 20 \$100 bills, 16 \$50 bills, 2 \$20 bills, 4 \$10 bills, 8 \$5 bills, and 4 \$1 bills.

Part E

The owner of the cashbox is missing the \$2,844 (see the boxed number of bills) possible. Determine the breakdown as well as the total number of bills used.

2844 = 100 + 20 = 28 with remainders of 44. 44 + 20 = 2 with remainder of 4. 4 + 1 = 4. The cashbox contains a total of 45 bills. There are 20 \$100 bills, 2 \$20 bills, and 9 \$1 bills.

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Unit Assessments

Two forms of the Unit Assessment, Form A and Form B, are available for either print or digital administration. The items on the two assessments are parallel items, assessing the same concept and standard. The table below provides the item analysis for both forms.

Both Unit Assessments are available in the Assessment Resource Book or as downloadable files from the Digital Teacher Center.

Data When students complete the Unit Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Lesson	Guided Support Intervention Lesson	Standard
1	2	7-1	Divide by Multiples of 10	5.NBT.B.6
2	2	7-1	Divide by Multiples of 10	5.NBT.B.6
3	2	7-2	Estimate Quotients (Whole Number)	5.NBT.B.6
4	2	7-3	Relate Multiplication and Division (Whole Numbers)	5.NBT.B.6
5	2	7-3	Relate Multiplication and Division (Whole Numbers)	5.NBT.B.6
6	2	7-4	Divide by 2-Digits (Area Models)	5.NBT.B.6
7	2	7-4	Divide by 2-Digits (Area Models)	5.NBT.B.6
8	2	7-5	Divide by 1-Digit (Partial Quotients)	5.NBT.B.6
9	2	7-5	Divide by 1-Digit (Partial Quotients)	5.NBT.B.6
10	2	7-6	Divide by 2-Digit (Partial Quotients)	5.NBT.B.6
11	2	7-6	Divide by 2-Digit (Partial Quotients)	5.NBT.B.6
12	3	7-2	Estimate Quotients (Whole Number)	5.NBT.B.6
13	3	7-7	Interpret Remainders in Word Problems	5.NBT.B.6
14	3	7-7	Interpret Remainders in Word Problems	5.NBT.B.6

Assign the digital Unit Assessment (Form A or B) to students or download and print PDFs from the Digital Teacher Center.



Unit 7 Unit Assessment, Form A

Name: _____

- Answer the $30 \div 3 = 4$ when quotient is not chosen of that divs.
 - A. $30 \div 3 = 4$
 - B. $30 \div 3 = 10$
 - C. $3000 \div 3 = 10$
 - D. $3000 \div 3 = 100$
 - E. $30000 \div 3 = 1000$
 - F. $30000 \div 3 = 10000$
- A company has 10,000 square feet of land to build 50 identical storage units. What is the area of each storage unit?

200 square feet
- If a store orders 4 1/2 of a certain amount of product in this order:
 - A. $4 \frac{1}{2} \times 2$
 - B. $1000 \div 4 \frac{1}{2}$
 - C. $1000 \times 4 \frac{1}{2}$
 - D. $1000 \div 4$
 - E. $4 \times 1000 \div 2$
- Which equation can be used to solve the problem $48 \div 12 = 4$?
 - A. $4 \times 12 = 48$
 - B. $4 \times 48 = 12$
 - C. $4 \times 12 = 12$
 - D. $4 \times 48 = 48$

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- A building has a height of 10 stories. Each story has a height of 200 feet. How many floors of area are there?

15 floors of area
- Which equation is correct by the area model?

$$\begin{array}{r} 10 \\ 10 \times 40 = 400 \end{array}$$

 - A. $2000 \div 40 = 50$
 - B. $5000 \div 40 = 125$
 - C. $5000 \div 10 = 500$
 - D. $5000 \div 10 = 50$
- The area of a rectangular garden is 2250 square feet. The length of the garden is 54 feet. What is the width of the garden? Use an area model to solve.

58 feet

Assessment Resource Book

Unit 7

Unit Assessment, Form A, continued

Name _____

8. Which equation is solved by the partial quotients algorithm?

$$\begin{array}{r} 45 \overline{) 210} \\ \underline{90} \\ 120 \\ \underline{90} \\ 30 \\ \underline{30} \\ 0 \end{array}$$

- A. $45 \div 210 = 45$
 B. $210 \div 45 = 45$
 C. $210 \div 45 = 4$
 D. $210 \div 45 = 450$

9. The area of a square wall is 1,210 square inches. The width of the wall is 11 inches. How long is the square wall? Use the partial quotients algorithm.

30 inches

10. What is the remainder for the quotient $140 \div 47$?

- A. 7
 B. 11
 C. 53
 D. 93

Assessment Answer Key 127

11. Peter has 174 markers in his desk. Each box holds 12 markers. How many boxes does Peter need to hold all his markers? How many markers does he have left over?

15 boxes were filled and 6 markers left over

12. A school team scored 877 points during the season. They played 17 games. How many points did the team score each game? Explain how you found your answer.

Sample answer: about 52 points. I used compatible numbers and changed 877 to 400 and 17 to 10, then $400 \div 10 = 40$.

13. Maria's pet has 12 eggs in 2 open containers. She is allowed to take home any eggs that are left over. Today Maria has 50 eggs in 2 packages. How did she do today? Any eggs hatched? Explain how many? Explain your answer.

Yes, 2 eggs. Sample answer: I divided 500 by 12 to get 54 R2. This means that she will get 54 containers and have 2 eggs left over, so she can take these home.

14. Peter has a collection of 1,800 baseball cards. He wants them in packs of 40. How many packs can he buy? How many cards will he have left over? Explain your answer.

45 packs of cards. Sample answer: I divided 1,800 by 40 and got 45 R0. So there will be 45 full packs and 0 more cards, so he will need 45 packs of cards for all of his cards.

100 Assessment Answer Key

Unit 7

Unit Assessment, Form B

Name _____

1. How many times does 4 go into 1,200? Use the partial quotients algorithm to solve.

- A. $300 \div 4 = 75$
 B. $400 \div 75 = 4$
 C. $1,200 \div 4 = 4$
 D. $1,200 \div 4 = 400$
 E. $4,000 \div 75 = 40$
 F. $2,000 \div 75 = 400$

2. A number has 2,250 square feet of area and is 150 feet wide. How long is the number? Use the partial quotients algorithm.

150 square feet

3. Use the partial quotients algorithm to solve $1,200 \div 40$.

- A. $30 \div 4$
 B. $300 \div 4$
 C. $300 \div 40$
 D. $300 \div 400$

4. What number is 45 more than the product of 4 and 4?

- A. $4 \times 4 + 45$
 B. $4 \times 45 + 4$
 C. $4 \times 45 + 4$
 D. $4 \times 4 + 45$

Assessment Answer Key 128

- A. $2,250 \div 15 = 15$
 B. $1,500 \div 15 = 100$

5. The area of a square is 1,210 square inches. The width of the square is 11 inches. How long is the square? Use the partial quotients algorithm to solve.

110 feet

100 Assessment Answer Key

6. The area of a rectangular garden is 1,200 square meters. The length of the garden is 30 meters. How wide is the garden? Use the partial quotients algorithm to solve.

40 meters

7. What is the remainder for the quotient $140 \div 47$?

- A. 7
 B. 11
 C. 53
 D. 93

Assessment Answer Key 129

WRITING: Explain how you found the answer to Question 1. How many times does 4 go into 1,200? Use the partial quotients algorithm to solve.

8. What is the remainder for the quotient $1,200 \div 40$? Use the partial quotients algorithm to solve.

40 packs of cards. Sample answer: I divided 1,200 by 40 and got 30 R0. So there will be 30 full packs and 0 more cards, so he will need 30 packs of cards for all of his cards.

100 Assessment Answer Key

Benchmark Assessment 2

The Benchmark Assessment 2 is available in both print and digital.

Data When students complete the Benchmark Assessment in the Digital Student Center, their responses are auto-scored.

Item Analysis

Item	DOK	Skill	Standard
1	2	Use unit cubes to determine volume	5.MD.C.4
2	2	Multiply multi-digit numbers	5.NBT.B.5
3	2	Round decimals	5.NBT.A.4
4	2	Add decimals	5.NBT.B.7
5	1	Relate multiplication and division	5.NBT.B.6
6	2	Represent multiplication of decimals	5.NBT.B.7
7	2	Divide multi-digit numbers	5.NBT.B.6
8	2	Multiply decimals	5.NBT.B.7
9	1	Multiply decimals by powers of 10	5.NBT.A.2
10	2	Subtract decimals	5.NBT.B.7
11	2	Multiply multi-digit numbers using an algorithm	5.NBT.B.5
12	2	Solve volume word problems	5.MD.C.5
13	2	Represent decimals in different ways	5.NBT.A.3.a
14	1	Understand powers and exponents	5.NBT.A.2
15	3	Understand place value	5.NBT.A.1
16	2	Use strategies to multiply multi-digit numbers	5.NBT.B.5
17	2	Compare decimals	5.NBT.A.3.b
18	2	Determine volume	5.MD.C.5
19	2	Represent subtraction of decimals	5.NBT.B.7
20a	3	Represent division of multi-digit numbers	5.NBT.B.6
20b	2	Divide multi-digit numbers	5.NBT.B.6
21	2	Solve multiplication word problems	5.NBT.B.5

Assign the digital Benchmark Assessment to students or download and print PDFs from the Digital Teacher Center.



Grade 5
Benchmark Assessment 2

Name: _____

1. One face of the rectangular prism is given.

What are the number of faces needed to make a rectangular prism of each volume, in cubic units?

40 cubic units 68 cubic units 92 cubic units 124 cubic units

4 faces 6 faces 8 faces 10 faces 12 faces 14 faces

2. What is the product?
 $52 \times 34 = \underline{1,768}$

3. What is 2,576 rounded to the nearest hundred?
A. 2,500 B. 2,570 C. 2,600 D. 2,580

4. Show your work to solve $5.05 \div 0.27$ in your missing notebook to complete Chen's equations.

$5 \div 2 = 2$
 $5.05 - 5.4 = -0.35$
 $0.05 + 0.30 = 0.35$
 $0 + 0.6 = 0.62 = 5.72$

5. Which equation has the same unknown as $1002 \div 38 = \square$?

A. $38 \times \square = 1002$ B. $\square \times 1002 = 38$
 C. $1002 \times \square = 38$ D. $\square \times 38 = 1002$

6. Look at the decimal grid.

Which product is represented by the decimal grid?

A. 2.4×10 B. 2.4×0.5
 C. 2.4×10 D. 0.31×10

7. What is the quotient?
 $552 \div 38 = \underline{14}$

8. Look at the expression:
 $5.24 \div 0$
What is the order of the expression?
 $\underline{0.02}$

9. Sam is solving $27 \div 37$.
How many times does the decimal point?

A. 4 places to the right
 B. 4 places to the left
 C. 0 places to the right
 D. 3 places to the left

10. Answer the question.

Appendix

Sense-Making Routines	A2
Number Routines	A3
Math Language Routines	A4
Key Concepts and Learning Objectives	A6

Sense-Making Routines

Notice & Wonder™

Students are presented with an image or situation and are asked to share what they notice and wonder about the image or situation. To increase student participation in this whole-class brainstorming activity, allow students adequate time to write or draw any noticings and wonderings. This will help students control their impulses, and expand their thinking. As you record students' thoughts, thank or acknowledge each student equally. Record all student suggestions, however resist praising, restating, clarifying, or asking questions.

This is primarily a whole-class, discussion-based brainstorming activity, one in which the noticings and wonderings of one student help spark additional noticings and wonderings among other students. Students should not be expected to write down what they notice and wonder; rather, the routine works better when students are more spontaneous and can respond to one another's comments.

As students share, the teacher may want to record students' noticings and wonderings for all to see and to avoid redundancy of ideas. Allow for some non-math-related observations and questions, but eventually pose questions to get students thinking about a math focus. The support in the Teacher Edition offers prompts that can focus students' thinking on a math focus.

These activities are low floor-high ceiling activities and it is important that all students feel comfortable participating and valued for their participation.

Variations of the *Notice & Wonder* routine include:

- Tell me everything you can.
- What question could you ask?
- What could the question be?

How are they the same? How are they different?

In this variation of the routine, students are presented with two or more images or situations and consider how the images or situations are similar and different. The students share similarities and differences, some of which may be mathematical in nature, others non-mathematical.

As with the *Notice & Wonder* routine, this is also primarily a whole-class, discussion-based activity. As students can share both mathematical and non-mathematical similarities and differences, the teacher can record these for reference. If students do not bring up the intended math focus, prompts in the Teacher Edition can get students thinking about the focus.

Which Doesn't Belong?

Students are presented with a series of images, quantities, or numbers – usually four, and think about the question, “Which doesn't belong?” The activity has been designed to have multiple responses depending on which criteria or attribute the student is considering. Students are encouraged to think about as many different ways to identify the one that does not belong.

As students share their responses, they should be encouraged to share their reasoning for which one does not belong.

Guidance in the Teacher Edition can help the teacher direct students' thinking to the specific math focus for the lesson.

Is It Always True?

Students are presented with one or more images or situations and think about the relationship among the objects in the image or situation. Students then consider whether the relationship always holds or whether it/they are unique to the image or situation.

As with the other sense-making routines, this is primarily a whole-class, discussion-based brainstorming activity, one in which students share their thoughts around the generalizability of the relationship and their reasoning for their claims. As with other routines, allow students adequate time for them to reason through their own thinking. Students should be encouraged to write down or draw their thoughts and reasoning. This additional think time allows students to process the information presented. However, some learners may need to make written notes to capture their thoughts and should feel free to do so.

Guidance in the Teacher Edition can help the teacher direct students' thinking to the specific math focus for the lesson that the sense-making routine is targeting.

Numberless Word Problems

Students are presented with a scenario or problem situation that suggests operations, but with no numbers. That is, instead of specifying quantities, the scenario or problem would indicate “some.” For example, “Some dogs are in the dog park. Some dogs come into the dog park. Then some dogs leave the dog park.” Students are expected to make sense of what is being described in the situation and explain which operations it represents. Without numbers, students are able to develop a better understanding of the underlying structure of the problem itself.

The prompts in the Teacher Edition offer options to extend and expand the discussion about the situation presented.

Number Routines

About How Much?

Purpose Build estimating skills.

Overview Students estimate the value of expressions (with operations) shown, explaining their strategies and thinking. The teacher records students' estimates, then reveals the value of the expression. Students analyze the estimates and discuss which are closest to the actual value of the expression.

Can You Make the Number?

Purpose Build flexible thinking and efficiency with operations.

Overview Students use all the given numbers to build expressions with a value of the given target number. Students can use a range of operations in their expressions. The teacher records students' expressions, then facilitates a discussion about students' expressions.

Decompose It

Purpose Build flexibility with numbers.

Overview Students come up with multiple (at least 3) ways to decompose given numbers and share their thinking for each decomposition. Teacher records decompositions then facilitates a discussion of patterns in the decompositions.

Find the Missing Values

Purpose Build their identification of patterns and their efficiency with solving equations as they examine a list of related equations.

Overview Students analyze a series of equations to look for patterns that they can use to determine the missing values in the equations. As students share their analyses and solutions, the teacher can reveal the missing values.

Find the Pattern, Make a Pattern

Purpose Build efficiency with recognizing and building patterns.

Overview Students determine the rule(s) for a given pattern, then use the rule(s) to continue the pattern or create a new pattern. The teacher records students' new patterns and facilitates a discussion to validate the pattern and its rules.

Greater Than, Less Than

Purpose Build proficiency with number and place value sense; estimating and comparing skills.

Overview Students use mental math to estimate or evaluate the value of given expressions and then compare the value of the expressions to a target benchmark number. Students share their solutions and thinking.

Math Pictures

Purpose Build number sense and mathematical awareness.

Overview Students respond to a prompt about an image.

What's Another Way to Write It?

Purpose Build flexibility with number sense and mental math operations.

Overview Given an expression, students come up with alternative expressions using the same or different operations that, when evaluated, have the same value. The teacher records expressions as students share. Students then look for relationships amongst the shared expressions.

Where Does It Go?

Purpose Build estimating skills using benchmarks.

Overview Students place a target number on number lines with different endpoints and justify their placement. In some instances, as a challenge, the target number may not actually belong on one of the number lines.

Which Benchmark Is It Closest To?

Purpose Enhance rounding and reasoning skills.

Overview Students determine to which benchmark the given number is closest and explain their reasoning.

Would You Rather?

Purpose Build flexibility with number sense and mental math operations; enhance decision-making.

Overview Students choose between two options, both of which require mental computation. Students explain their choice and their rationale for their choice.



Math Language Routines

MLR 1 Stronger and Clearer Each Time

Purpose To provide opportunities for students to revise and refine both their ideas and their verbal and written output (Zwiers, 2014).

Successive Pair Shares Students respond to a prompt either verbally or in writing. Then, students share their responses and their reasoning through successive pair shares, refining and revising their response after each pair share. Student-pairs are expected to provide details and to press their partners to provide details around their thinking. Students revise their responses after each pair share, incorporating as appropriate new ideas or language.

Convince Yourself, a Friend, a Skeptic Students think about an argument for three different audiences. They first justify the argument in a way that makes sense to them, then they explain what they know and think and how they know their argument is true to a classmate. For their third audience, students explain why they know their argument is true to a different classmate. Students' arguments may include words, pictures, numbers, and examples. Students should be prepared to offer counter-arguments.

MLR 2 Collect and Display

Purpose To help students build vocabulary and language when engaging in mathematical discourse.

Gather and Show Student Discourse (Dieckmann, 2017) While students are working in pairs or small groups, the teacher circulates and listens to student talk, capturing common or important words and phrases. The teacher organizes words and phrases captured in a visual display that the teacher and students can reference throughout the unit of study. The teacher can update and add to the visual display to show refinement in language students are using to discuss key concepts.

Number Talks (Humphreys & Parker, 2015) Number Talks have four parts: (1) Students are presented with a numeracy problem that they consider without written solution for a few minutes; (2) Students share their strategy for solving and their thinking about their strategy; (3) As students share their strategies and thinking, the teacher creates a visual display of students' strategies and thinking, noting common or important words or phrases shared; (4) The teacher facilitates a discussion analyzing the strategies and thinking, their benefits and drawbacks in different types of situations.

MLR 3 Critique, Correct, and Clarify

Purpose To have students analyze and reflect on a written or verbal mathematical argument.

Critique a Partial or Flawed Response The teacher presents a partial or flawed argument, explanation, or solution and has students come up ways to complete or fix the argument. Students can work individually or in pairs to propose improvements and/or additions to the argument. Students share their responses with a partner and based on feedback from their partner, they refine and revise their responses.

Always, Sometimes, Never The teacher presents a mathematical statement that students analyze to decide whether it is always, sometimes, or never true. If possible, the teacher presents the statement in a graphic organizer that can then be used to assess students' reasoning.

MLR 4 Information Gap

Purpose To create a need for students to communicate (Gibbons, 2002).

Info Gap Cards Each student-pair has two cards, Student A has Card A with the problem statement and Student B has Card B with data or information needed to solve the problem. Student A asks Student B for specific information that is needed to solve the problem. Before providing the information, Student B asks Student A to justify the need for information before providing the information requested (if available). Student A then explains how he or she will use the information to solve the problem.

Info Gap Games Student-pairs play a guessing or matching game. Student A shares the information and Student B uses his or her understanding of math concepts to guess what Student A is describing. For example, Student A may identify objects in the classroom that share a shape and Student B guesses the shape.

MLR 5 Co-Craft Questions and Problems

Purpose To allow students to use conversation skills and mathematical language to generate questions, problems, and situations.

Co-Craft Questions The teacher presents a scenario or part of a problem context and students come up with math-related questions that could be asked about the situation. Student-pairs share their questions, comparing and contrasting the questions each asked. The teacher can then facilitate a share-out of questions from the class, after which the actual question students will look to answer is revealed.

Co-Craft Problems Student-pairs work together to co-create problems. Student-pairs then solve their problems, and trade problems with another student-pair. Student-pairs solve the problems of others, checking their solution against that of the co-creators.

Co-Craft Situations The teacher presents a mathematical representation with no labels. Students work individually to write a story or scenario that matches the representation. Students then work with a partner to share their scenarios or situations, each explaining how their situations reflect the mathematical representation. Based on feedback from their partners, students revise their situations, adding details as appropriate.

MLR 6 Three Reads

Purpose To ensure that students make sense of problem situations and equip them with tools used to negotiate meaning (Kelemanik, Lucenta & Creighton, 2016).

Three Reads Students read a problem situation or scenario three times, each time with a different focus (1) Students read for comprehension, to understand the problem situation; (2) Students focus on the language used to present the mathematics with the goal of understanding what mathematics is most appropriate to use; (3) students think about which strategy or solution method would be appropriate.

Values/Units Chart (1) Students read through text and underline any words or phrases that represent a known or unknown value or amount. (2) They list these numbers, unknowns, and variables in the left column of their graphic organizer (Values). (3) After reading a second time, students write the meaning of the values in the right column of the graphic organizer (Units). (4) After the third read, students work in pairs to create mathematical expressions using only the right column.

MLR 7 Compare and Connect

Purpose To foster students' meta-awareness as they identify, compare, and contrast different mathematical approaches, representations, concepts, examples, and language.

Compare and Contrast Solution Strategies Students are given a problem to solve on their own. Students are then paired up and share their solution strategies with their partners, relating and connecting their partner's approach to their own approach. Some options include:

- 1. Divide and conquer** Set students in pairs before they solve the problem. Each pair decides on two different ways to solve the problem; one partner does one way and the other partner does the other way.
- 2. What is similar, what is different** After student-pairs share solution strategies, they identify what is similar and what is different about the approaches. Students can also discuss what worked with each approach.
- 3. Mathematical focus** Student-pairs focus on specific mathematical relationships, operations, quantities and values.

Which One Doesn't Belong? Students are provided with sets of four numbers, equations, expressions, graphs, or geometric figures. Working in pairs, students decide together how to group the sets so that three of the items fit within a category they have created and one does not. Both partners should be prepared to explain to a different group how they agreed on a category and justify which item did not fit.

MLR 8 Discussion Supports

Purpose To facilitate rich discussions about mathematical ideas, representations, contexts, and strategies (Chapin, O'Connor, & Anderson, 2009).

Whole Class Discussion Supports During whole class discussion, the teacher can use these strategies to support mathematical discourse:

- **Restating** The teacher restates students' ideas as questions to clarify meaning and model appropriate mathematical language
- **Press for Details** The teacher asks students to elaborate on an idea, expand an argument, or give an example.
- **Think Alouds** The teacher talks through their thinking about a mathematical concept.
- **Use multiple modalities** The teacher uses different modalities to show concepts.
- **Choral responses** The teacher has students practice common or important words or phrases through choral repetition.

Numbered Heads Together (1) The teacher has students count off by 4s (or the number of students he or she wants to have in a group). (2) The teacher then presents a question or problem and has students work in their groups according to their number to come up with an explanation or justification. (3) Each group reporter shares the group explanation and/or agree or disagree with the previous group reporter. Other members of the group are not allowed to talk or write, but the reporter can use the notes from the group discussion. The correct answer, if there is one, is revealed once all groups have presented.

Key Concepts and Learning Objectives

KEY CONCEPT Habits of Mind and Classroom Norms for Productive

Math Learning

- Students make sense of problems and quantities and represent them different ways. (Unit 1)
- Students represent a real-world situation using mathematics. (Unit 1)
- Students construct an argument to explain their thinking with clear and appropriate terms. (Unit 1)
- Students use patterns to develop efficient strategies to solve problems. (Unit 1)
- Students tell their math biography and recognize the behaviors and attitudes that support a productive learning environment. (Unit 1)

KEY CONCEPT Operations with Fractions

- Students add, subtract, and multiply fractions, including mixed numbers, with unlike denominators. (Units 9, 10)
- Students find the area of a rectangle with fractional side lengths. (Unit 10)
- Students describe multiplication as scaling. (Unit 10)
- Students divide unit fractions by whole numbers and whole numbers by unit fractions. (Unit 11)

KEY CONCEPT Operations with Whole Numbers and Decimals

- Students describe the relationship between place value positions. (Unit 3)
- Students use an algorithm to multiply whole numbers. (Unit 5)
- Students divide multi-digit dividends by 2-digit divisors. (Unit 7)
- Students add, subtract, multiply, or divide decimals. (Units 4, 6, 8)
- Students solve word problems involving operations with whole numbers or decimals. (Units 4, 5, 6, 7, 8)

KEY CONCEPT Measurement and Data

- Students describe volume is an attribute of solid figures. (Unit 2)
- Students measure volume by counting unit cubes. (Unit 2)
- Students calculate the volume of rectangular prisms using formulas. (Unit 2)
- Students find the volume of composite solid figures. (Unit 2)
- Students convert measurement units within a given measurement system. (Unit 12)
- Students interpret data on a line plot. (Unit 12)

KEY CONCEPT Geometry

- Students identify and describe features of a coordinate plane. (Unit 13)
- Students graph points on the coordinate plane to solve problems. (Unit 13)
- Students classify 2-dimensional figures into categories based on their properties. (Unit 13)

KEY CONCEPT Algebraic Thinking

- Students write numerical expressions to represent calculations that are described using written statements. (Unit 14)
- Students interpret numerical expressions without evaluating them. (Unit 14)
- Students use the order of operations to evaluate numerical expressions. (Unit 14)
- Students generate two numerical patterns using two given rules. (Unit 14)
- Students identify apparent relationships between corresponding terms in the generated number patterns. (Unit 14)

Glossary/Glosario

English

Spanish/Español

BB

base The side of a prism figure or 3-dimensional solid that is used to find its height by drawing a line from the opposite angle.



base Lado de una figura prismática que se usa para encontrar la altura. Se traza una línea desde el ángulo opuesto.



CC

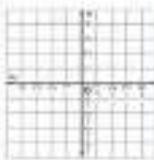
composite solid figure A solid figure that is made up of two or more solids.

coordinate plane A plane in which a horizontal number line and a vertical number line represent a right angle of 90 degrees. Each side of the angle is labeled with the same numerical values.



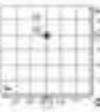
figura compuesta Figura conformada por dos o más figuras tridimensionales.

plano de coordenadas Plano en el que una línea horizontal horizontal y una línea vertical vertical se encuentran en un ángulo recto de 90 grados. Cada lado del ángulo se etiqueta con los mismos valores numéricos.



representing lines Numbers that are written inside parentheses in two numerical columns.

líneas representadas Números que están en la misma posición en dos columnas numéricas.

English	Spanish/Español
<p>Ex evaluate To find the value of an algebraic expression by replacing variables with numbers.</p> <p>expand To multiply out terms in an algebraic expression by removing brackets.</p> <p>exponent The number of times a base is multiplied by itself.</p> <p>in 2ⁿ The exponent is 2.</p> <p>operation A combination of numbers, variables, and operations.</p> <p>order 1-1-1</p>	<p>evaluar Calcular el valor de una expresión algebraica reemplazando variables por números.</p> <p>expandir Desarrollar los términos que están dentro de un paréntesis.</p> <p>en 2ⁿ El exponente es 2.</p> <p>operación Combinación de números, variables y símbolos de operaciones.</p> <p>orden 1-1-1</p>
<p>Eq equation symbol Parentheses () or equals (=) that let you know that two sides are equal. They usually balance the other when measuring numerical expressions.</p>	<p>simbol de igualdad Por los números que son iguales de un punto en un punto en un símbolo de igualdad o en un símbolo de igualdad o en un símbolo de igualdad, un número como en una balanza, coordenadas verticales.</p> <p>Ejemplo H-3</p> 
<p>Hi horizontal lines A combination of numbers, variables, and operations.</p>	<p>líneas horizontales Líneas que están en una línea horizontal.</p> <p>Ejemplo H-3</p> 
<p>Hi horizontal lines A combination of numbers, variables, and operations.</p>	<p>líneas horizontales Líneas que están en una línea horizontal.</p> <p>Ejemplo H-3</p> 
<p>Hi horizontal lines A combination of numbers, variables, and operations.</p>	<p>líneas horizontales Líneas que están en una línea horizontal.</p> <p>Ejemplo H-3</p> 

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